



Second 0⁺ state of unbound ¹²O via the (*p*, *t*) reaction

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¹²O (
$$Z = 8, N = 4$$
) mirrors ¹²Be with $N = 8$

N = 8







0_2^+ isomer in ¹²Be



S. Shimoura *et al.*, Phys. Lett. B 560, 31 ('03) S. Shimoura *et al.*, Phys. Lett. B 654, 87 ('07)

0_2^+ energies and shell quenching at N = 8



Intruder $2s_{1/2}$ component in 0_1^+ and 0_2^+



R. Kanungo et al., Phys. Lett. B 682, 391, 108 ('10)

¹²O and its mirror symmetry



- Shell breaking at Z = 8 ?
- Weakly-bound 2s_{1/2}
 - \rightarrow Reduces Coulomb energy ?
 - \rightarrow Enhances Thomas-Ehrman shift ?

Experimental history





S. Mordechai et al., Phys. Rev. C 32, 999 ('85)



R.A. Kryger et al., Phys. Rev. Lett. 74, 860 ('95)

Missing mass method with (p, t) reaction





CATS: S. Ottini-Hustache *et al.*, Nucl. Instr. Meth. A 431, 476 ('99). Target: P. Dolégiéviez *et al.*, Nucl. Instr. Meth. A 564, 32 ('06). MUST2: E. Pollacco *et al.*, Eur. Phys. J. A 25, 287 ('05).

First study (1 day) at SPEG/GANIL



D. Suzuki, H. Iwasaki, D. Beaumel *et al.*, Phys. Rev. Lett. 103, 152503 ('09). D. Suzuki, Euro. Phys. J. A 48, 130 ('12).

Second study (7 days) at LISE/GANIL



D. Suzuki, H. Iwasaki, D. Beaumel et al., Phys. Rev. C 93, 024316 ('16)

Mirror energy difference of the 0_2^+ state



$$0_1^+$$
 12Be 12O('09) 12O('16)

- How to quantify impact of weak binding to level shift?
- Systematics of 0⁺ mirror pairs' energy differences
- Scaling for charge and mass (= size)

Riisager's universal scaling for 2n halo radii

K. Riisager, D.V. Fedrov, A.S. Jensen, Europhys. Lett. 49, 547 ('00)



Scaling by 3-body hyperradii

$$\rho_0^2 = \sum_{i < k} \frac{m_i m_k}{m m_{\text{tot}}} R_{ik}^2$$

m: unit mass *R_{ik}*: length for *i*-th and *k*-th particles



Binding energy

*B: binding energy

Scaling of mirror energy differences



[1] K. Riisager, D.V. Fedrov, A.S. Jensen, Europhys. Lett. 49, 547 ('00)
[2] A. Muta, T. Otsuka, Prog. Theo. Phys. Suppl. 142, 355 ('01)

Universality of 0⁺ mirror energies



Summary

- Unbound ¹²O was studied by the (*p*, *t*) reaction at GANIL.
- Missing mass spectra were obtained from tritons detected by MUST2 telescopes.
- The 0₂⁺ state of ¹²O was discovered at 1.62(13) MeV.
 Shell closure disappearing at Z = 8
 Level energy shift -0.63 MeV relative to ¹²Be
- Systematics of known O⁺ states
 - Scaling relation of mirror energy differences and binding energies.
 - ¹²O 0₂⁺ state, under the influence of weak binding, represents the lowest energy difference.

Collaborators



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energie atomique • energies alternatives



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N. Keeley

Backup

Systematics of all known 0⁺ mirror pairs



Level mixing



Setup



CATS: S. Ottini-Hustache *et al.*, Nucl. Instr. Meth. A 431, 476 (1999). Target: P. Dolegieviez *et al.*, Nucl. Instr. Meth. A 564, 32 (2006). MUST2: E. Pollacco *et al.*, Eur. Phys. J. A 25, 287 (2005).

First study (1 day) at SPEG/GANIL





D. Suzuki *et al.*, Phys. Rev. Lett. 103, 152503 ('09).D. Suzuki, Euro. Phys. J. A 48, 130 ('12).

Z = 8 shell closure vanishes

Radius & hyperradius

$$\rho_0^2 = \frac{2(a-2)}{a}R_{cp}^2 + \frac{1}{a}R_{pp}^2$$

K. Riisager, D.V. Fedrov, A.S. Jensen, Europhys. Lett. 49, 547 ('00)

 $R_{cp} = 1.27 (a-2)^{1/3} {
m fm} \,$ $\,$ Assumed. Not given in the literatures.

 $R_{pp} = 2.65~{
m fm}~~$ C.V. Fedrov, A.S. Jensen, K. Riisager, Phys. Rev. C 49, 201 ('94)

a: mass number of the nucleus

| | ρ ₀ [fm] | S _{2n} [MeV] | B_{3BD} * |
|------------------|---------------------|-----------------------|--------------------------|
| ⁶ He | 2.57 | 0.975 | 0.321 |
| ¹¹ Li | 3.47 | 0.369 | 0.223 |
| ¹⁴ Be | 3.87 | 1.266 | 0.949 |
| ¹⁷ B | 4.21 | 1.330 | 1.178 |

*) Present work: $B_{3BD} = mS_{2n}\rho_0/h^2$

The calculated values in the table reasonably agree with the values in the literature.



MED & binding energies

Mirror energy difference (experimental values)

$$E_{c} = (S_{2n} - E_{x}^{n}) - (S_{2p} - E_{x}^{p})$$

 S_{2n} : 2*n* separation energy (neutron-rich partner) S_{2p} : 2*p* separation energy (proton-rich partner) E_x^n : excitation energy (neutron-rich state) E_x^p : excitation energy (proton-rich state)



Mirror energy difference (reference)

 $U_{\rm 3BD} = 2\alpha \frac{6(Z-2)}{5\rho_0}$

z: atomic number of proton-rich partner A. Muta, T. Otsuka,

Prog. Theo. Phys. Suppl. 142, 355 ('01)

Binding energy for 2p (unscaled)

$$B = U_{\text{barrier}} + S_{2p} - E_{\text{x}}^p$$

Coulomb barrier energy for 2*p*

$$U_{\text{barrier}} = 2\alpha \frac{Z-2}{\rho_0}$$

Assumed. Not given in the literatures.

Binding energy for 2p (scaled)

 $B_{\rm 3BD} = m B \rho_0^2 / \hbar^2$

m = 938.27 MeV/c² (unit mass)

K. Riisager, D.V. Fedrov, A.S. Jensen, Europhys. Lett. 49, 547 ('00)

For 2 body scaling, replace ρ_0 with R_{cp}