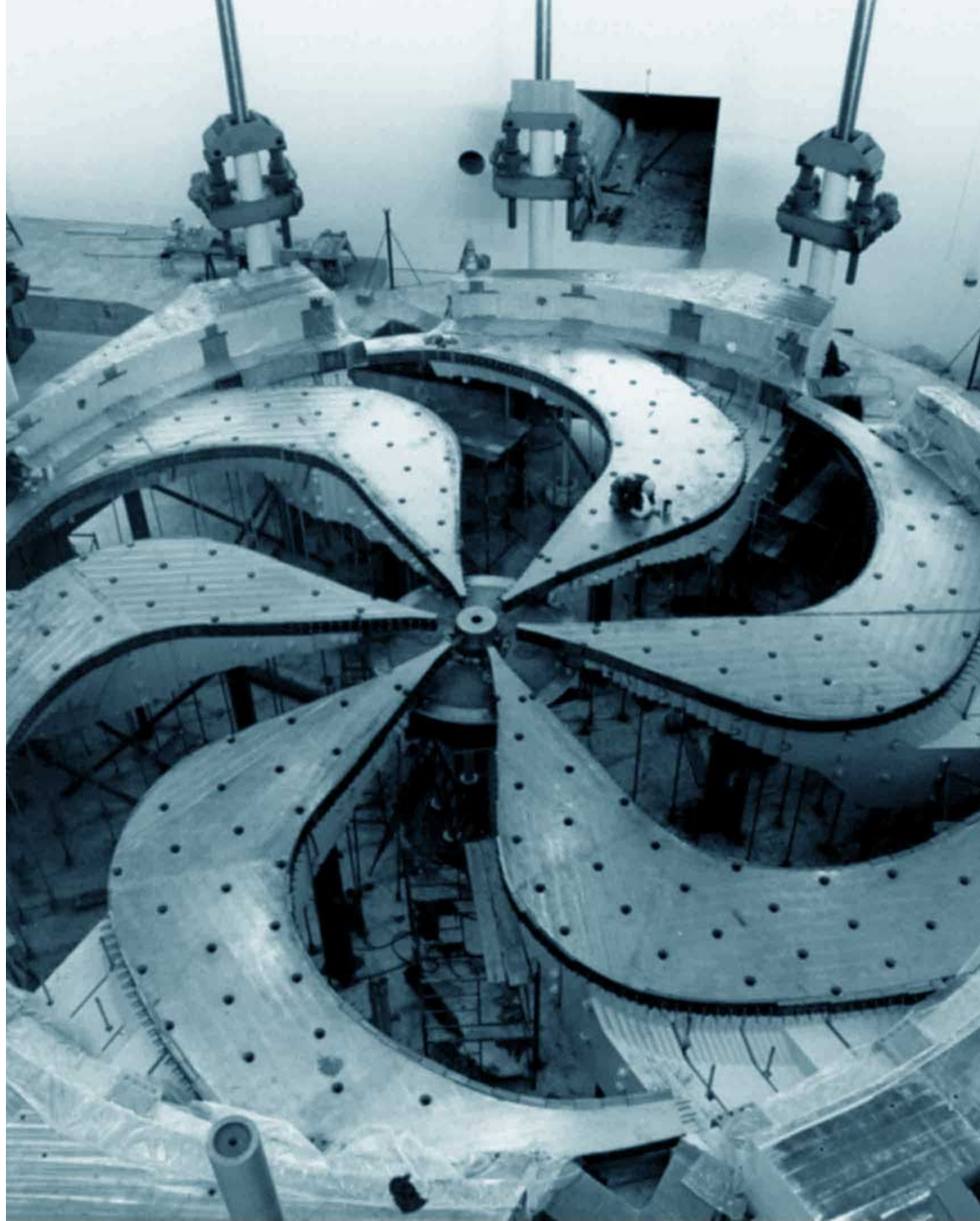




Exploring major nuclear structure issues with rare isotopes

Jason D. Holt
Scientist, Theory Department
Science Week
August 19, 2020



Arthur B. McDonald
Canadian Astroparticle Physics Research Institute



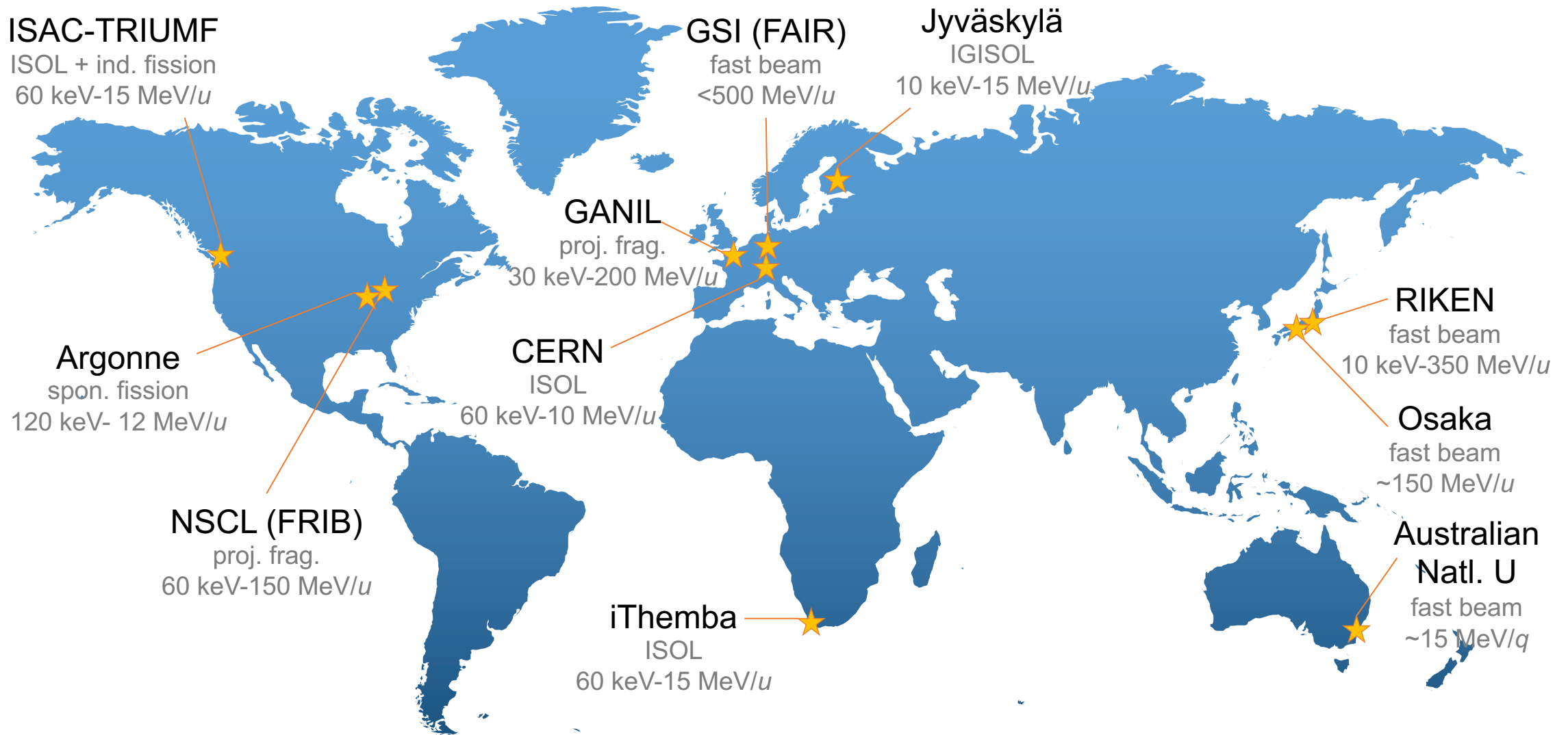
Discovery,
accelerated

Next-generation RIB facilities: unprecedented era of nuclear science

Major RIB Facilities

Thousands of new isotopes to be produced – need intense beams to probe essential properties

Q: How do we avoid “stamp collecting”?



Next-generation RIB facilities: unprecedented era of nuclear science

Major RIB Facilities

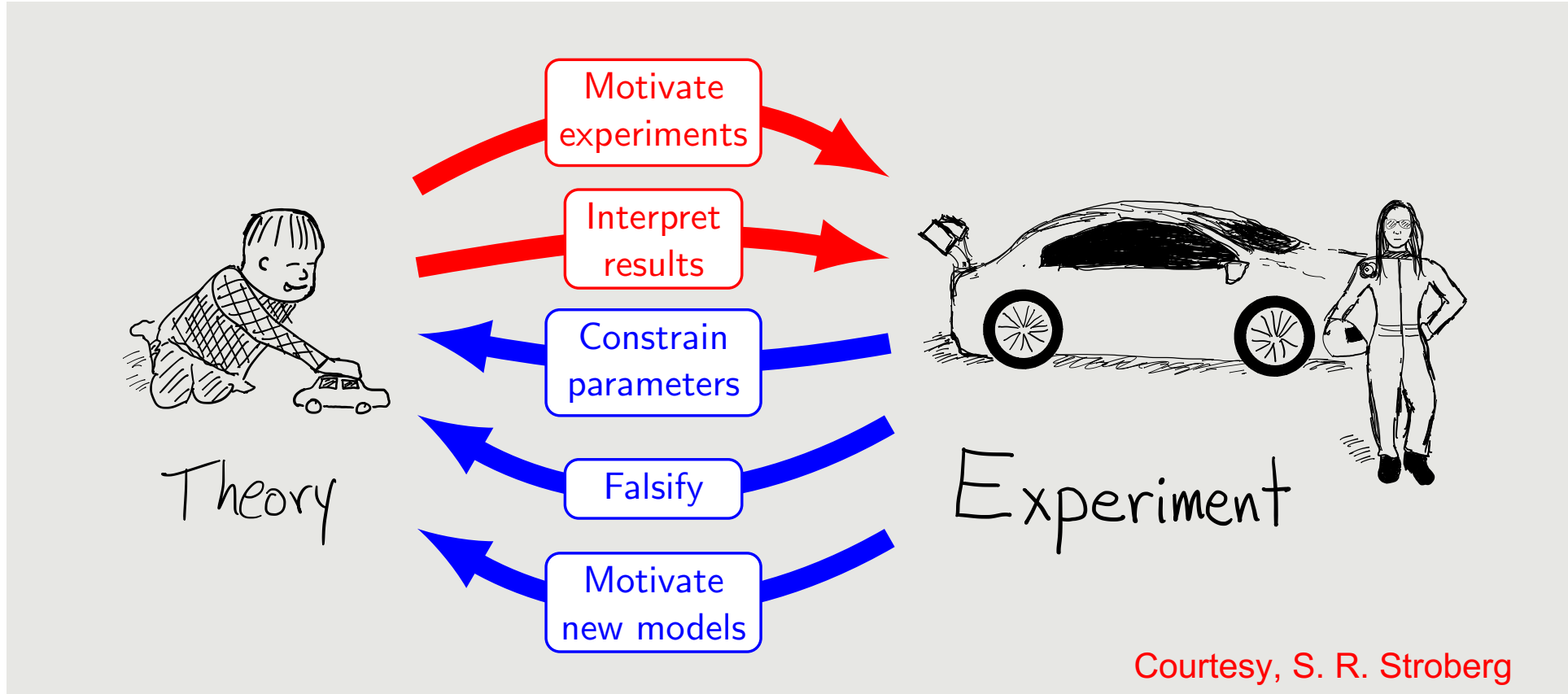
Thousands of new isotopes to be produced – need intense beams to probe essential properties

Q: How do we avoid “stamp collecting”? A: **Meaningful interplay with theory**



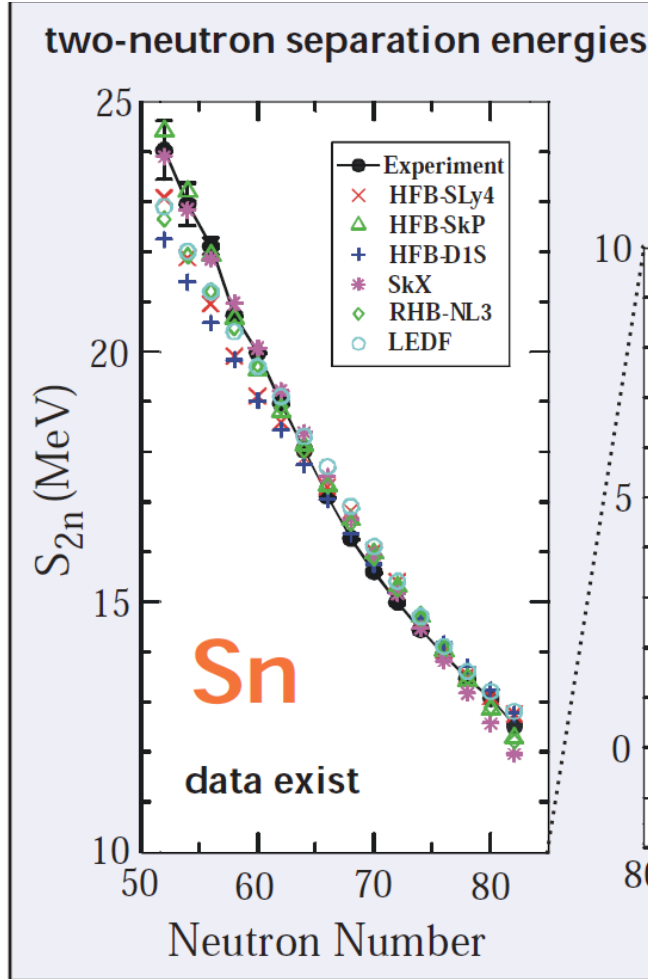
\$4-5 Billion worldwide investment
What is the exciting physics?

Big questions largely driven by theory; similar needs for all RIB facilities – is theory ready??



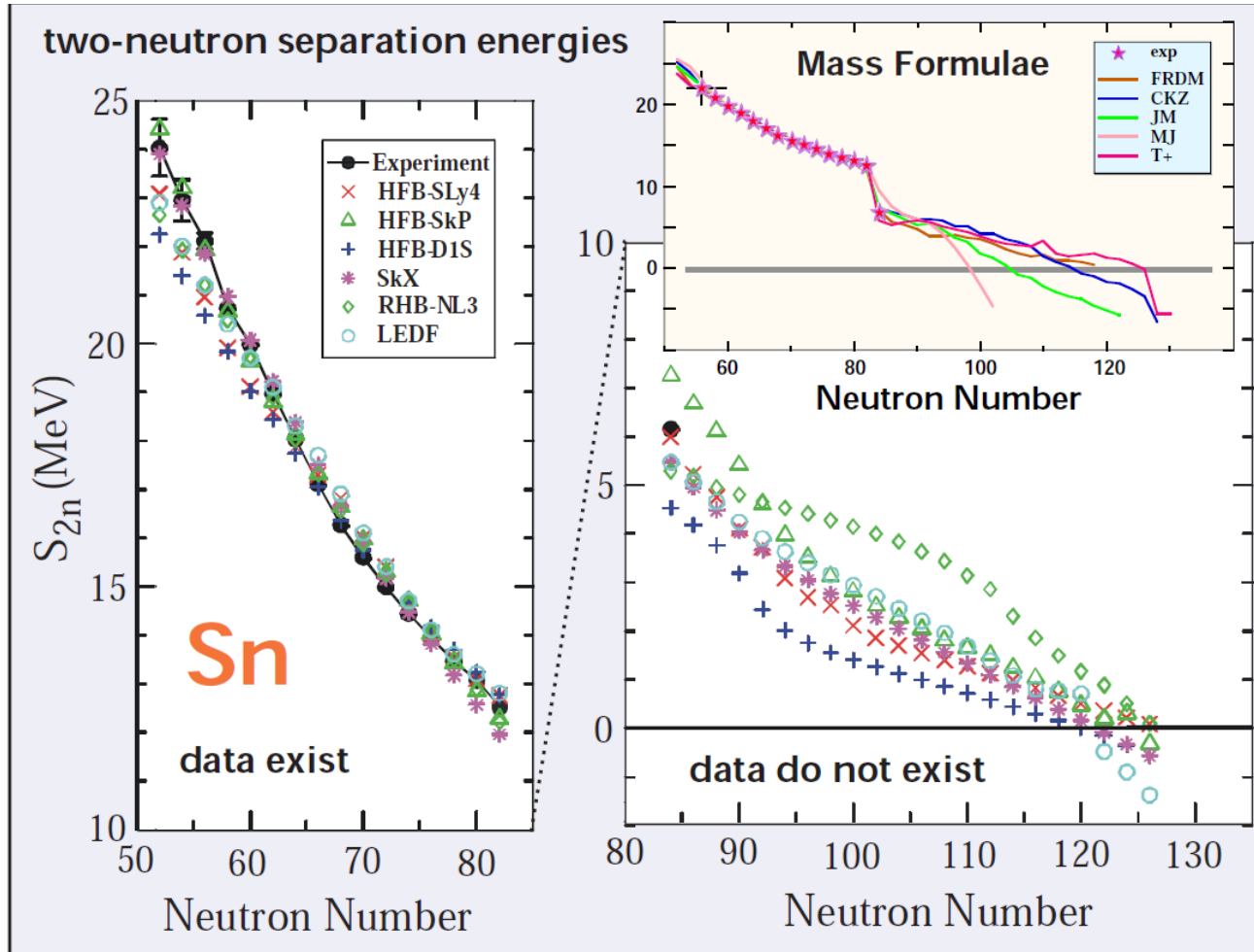
How do we currently approach nuclear theory?

How well can models motivate experiments?



Agreement good where data exists

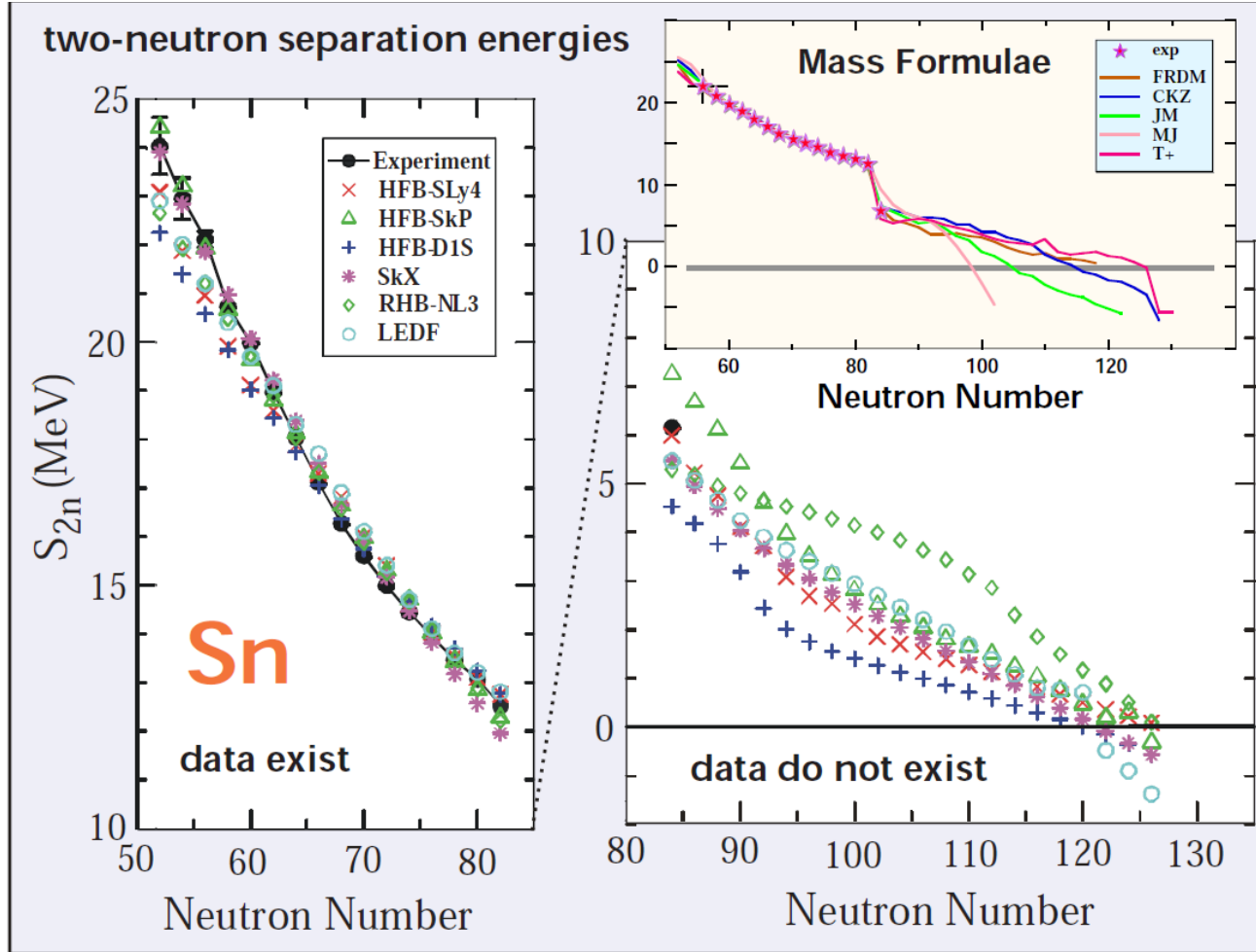
How well can models motivate experiments?



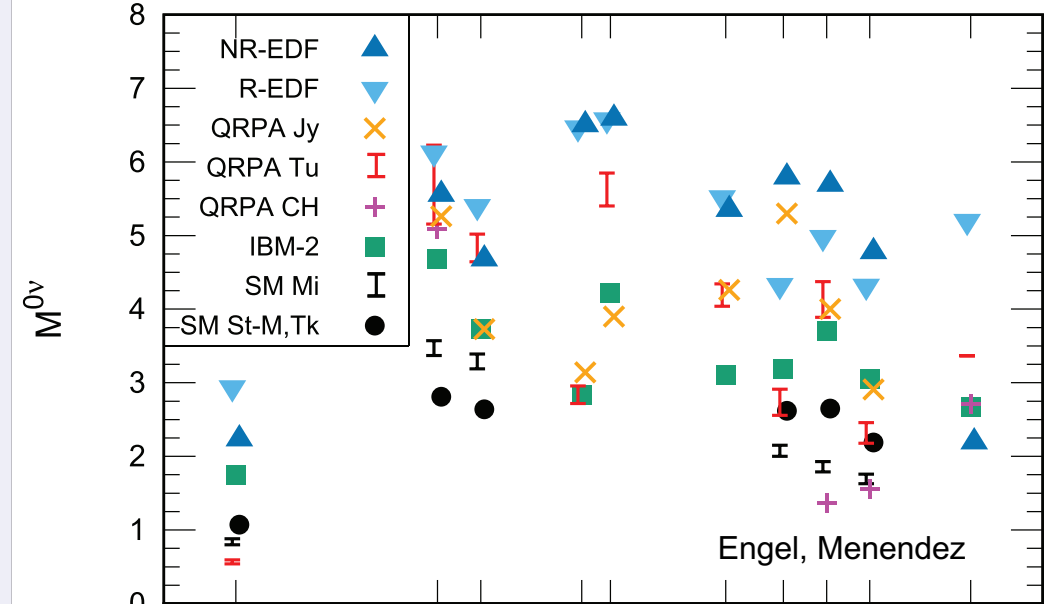
Often extrapolates unreliably

Spread in results = meaningful uncertainty?

How well can models motivate experiments?



Analogous picture in double beta decay



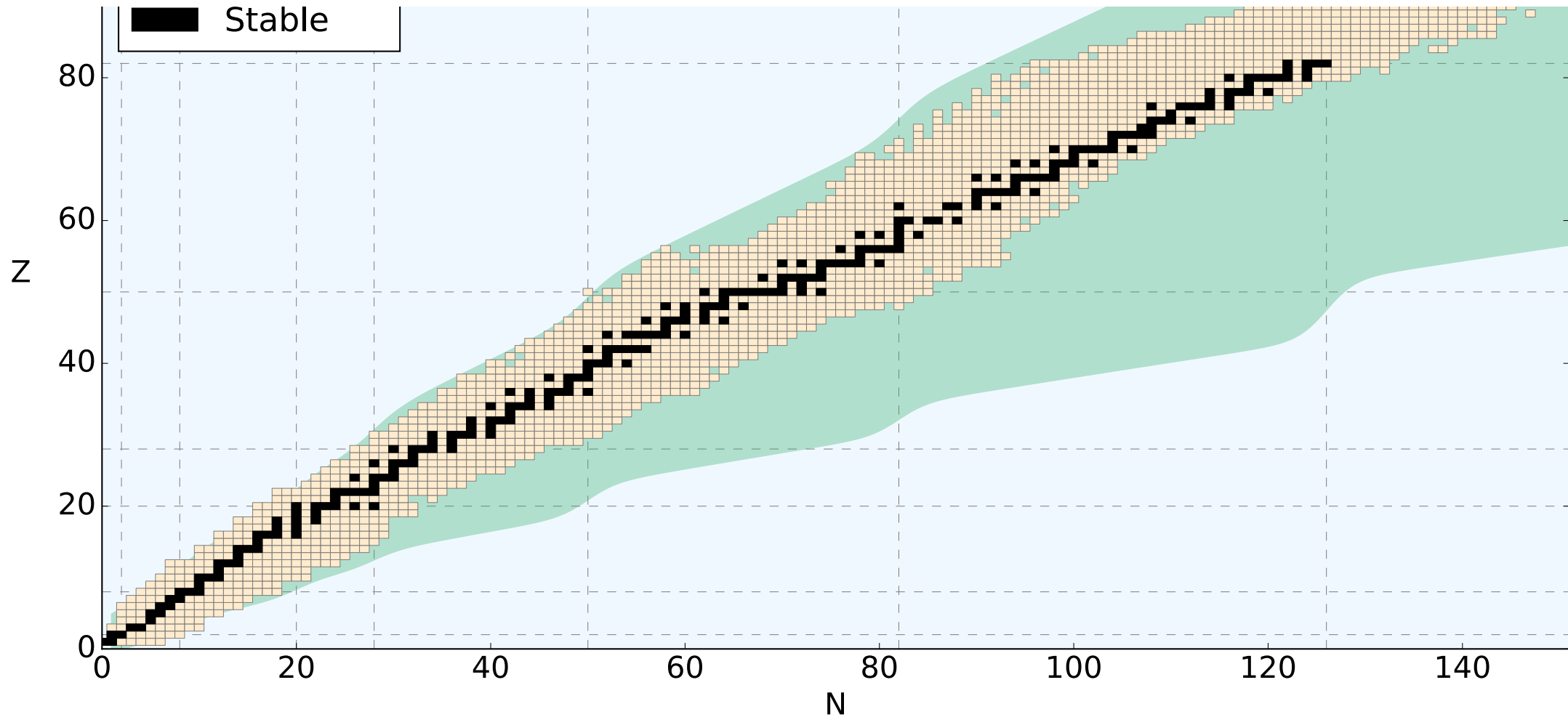
More billions invested worldwide

Often extrapolates unreliably

Spread in results = meaningful uncertainty?

Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

$$H\psi_n = E_n\psi_n$$

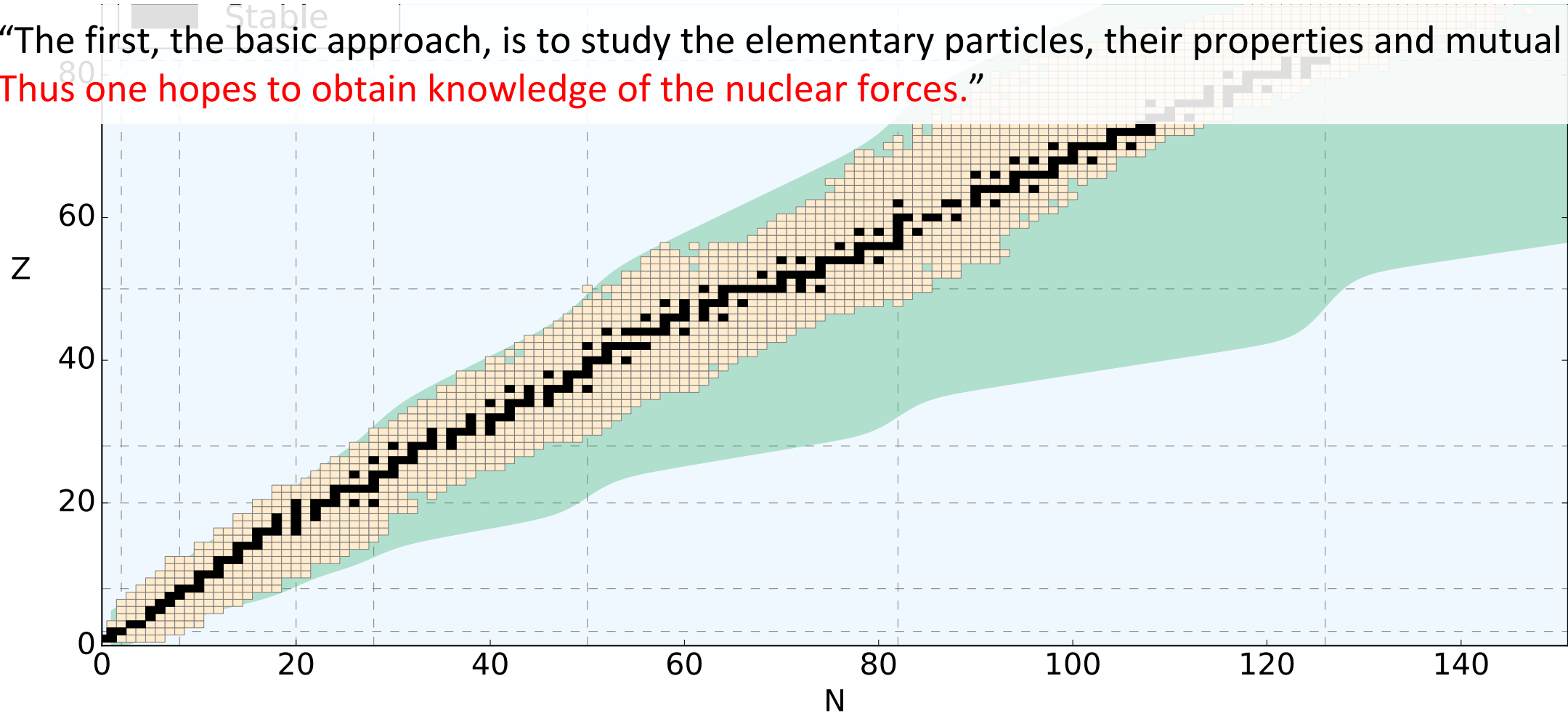


Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

- Nuclear forces (low-energy QCD)
- Electroweak physics

$$\boxed{H}\psi_n = E_n\psi_n$$

“The first, the basic approach, is to study the elementary particles, their properties and mutual interaction. Thus one hopes to obtain knowledge of the nuclear forces.”



Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

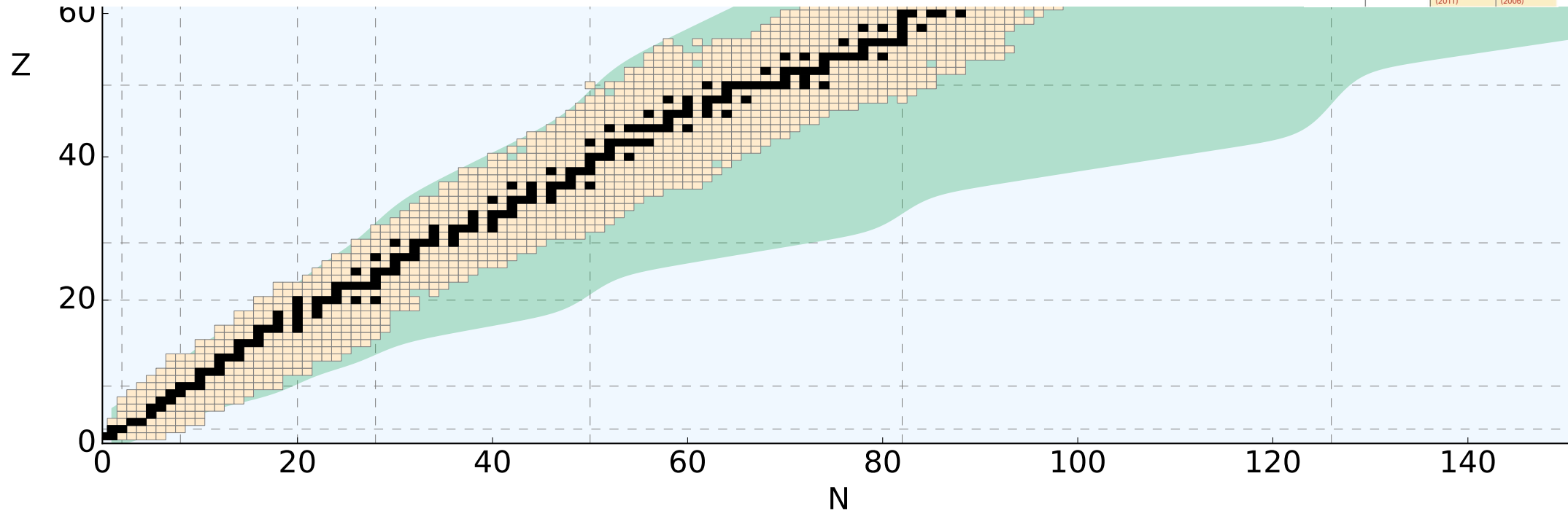
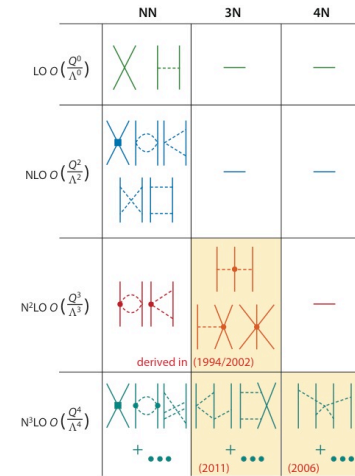
- Nuclear forces (low-energy QCD)
- Electroweak physics

$$\boxed{H}\psi_n = E_n\psi_n$$

Chiral effective field theory: systematic expansion of nuclear interactions

Consistent 3N forces, electroweak currents

Quantifiable uncertainties possible

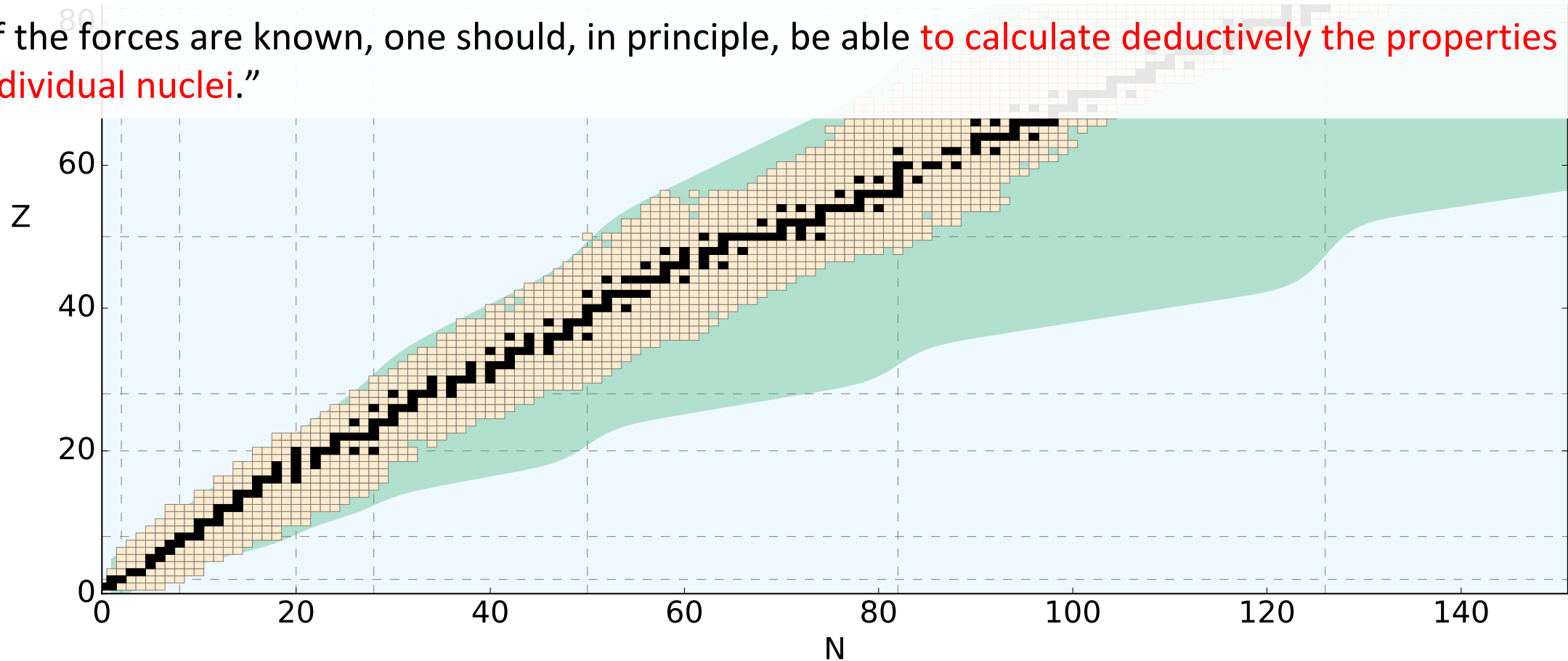


Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

- Nuclear forces (low-energy QCD)
- Electroweak physics
- **Nuclear many-body problem**

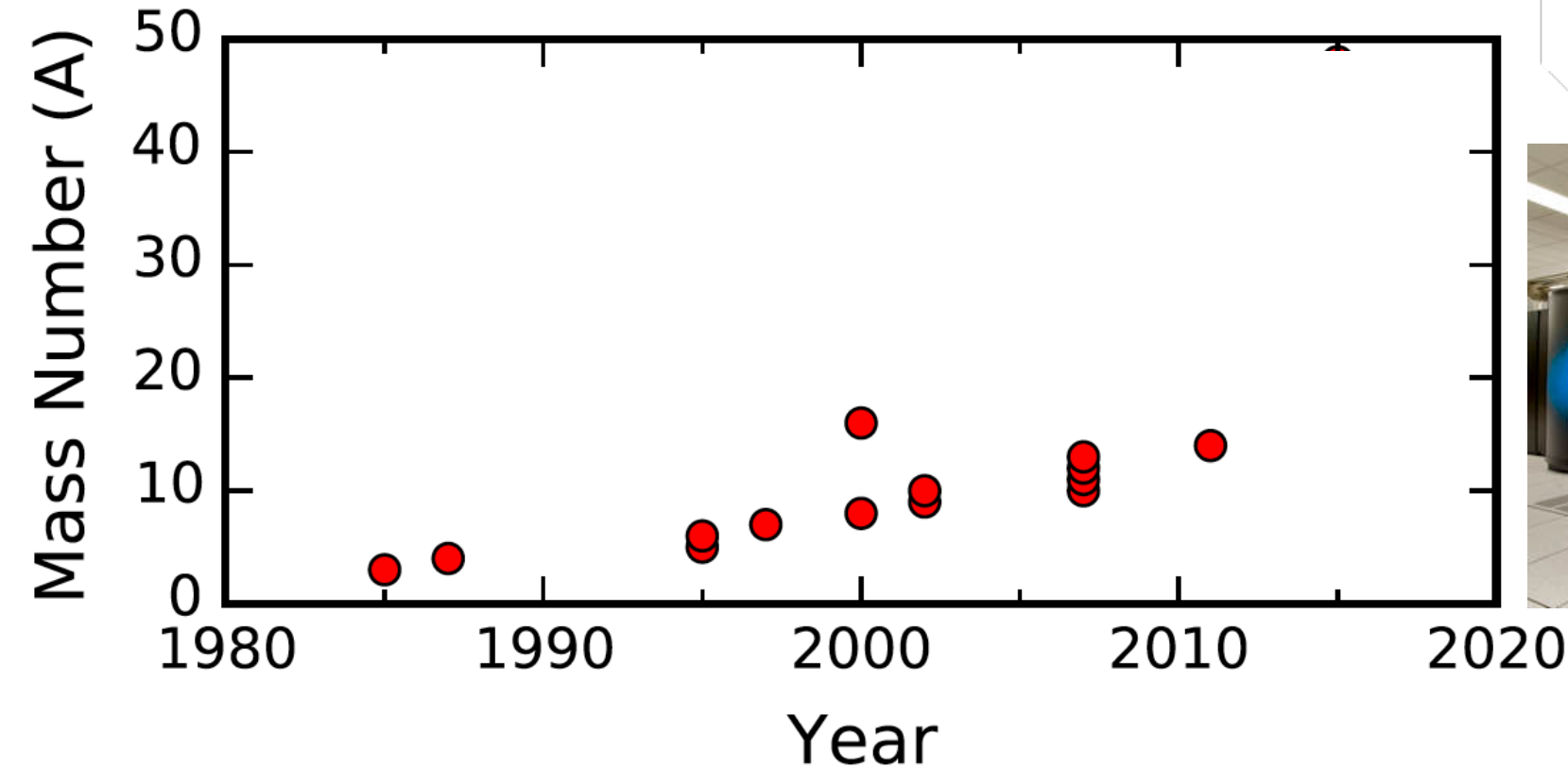
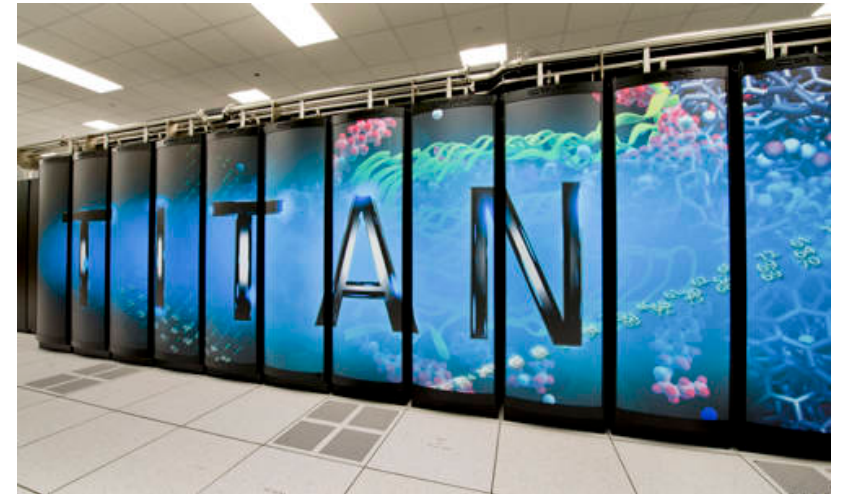
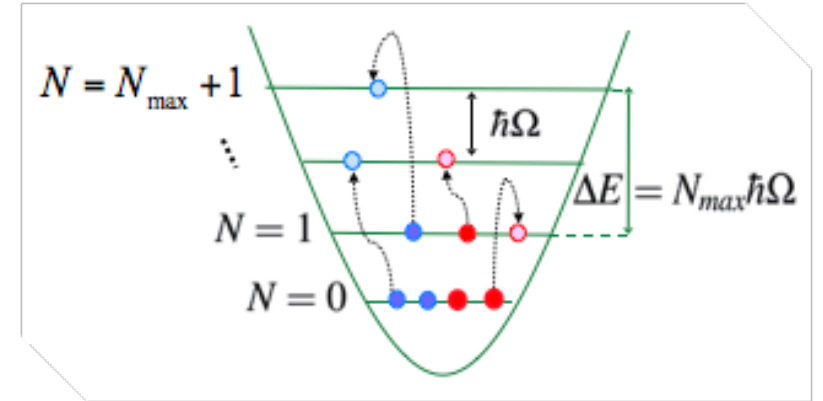
$$H\psi_n = E_n\psi_n$$

“If the forces are known, one should, in principle, be able to calculate deductively the properties of individual nuclei.”



Moore's law: exponential growth in computing power

Methods for light nuclei (QMC, NCSM) scale exponentially with mass

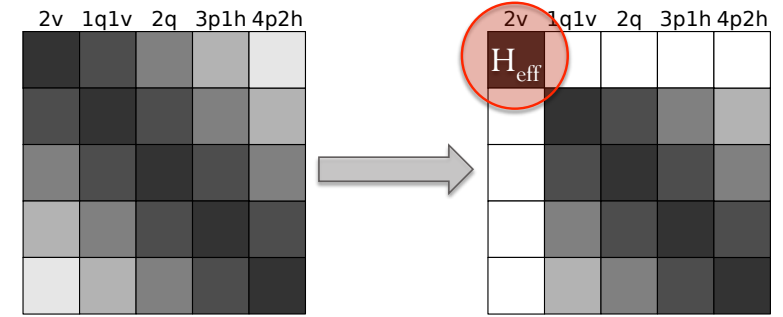



Moore's law: exponential growth in computing power

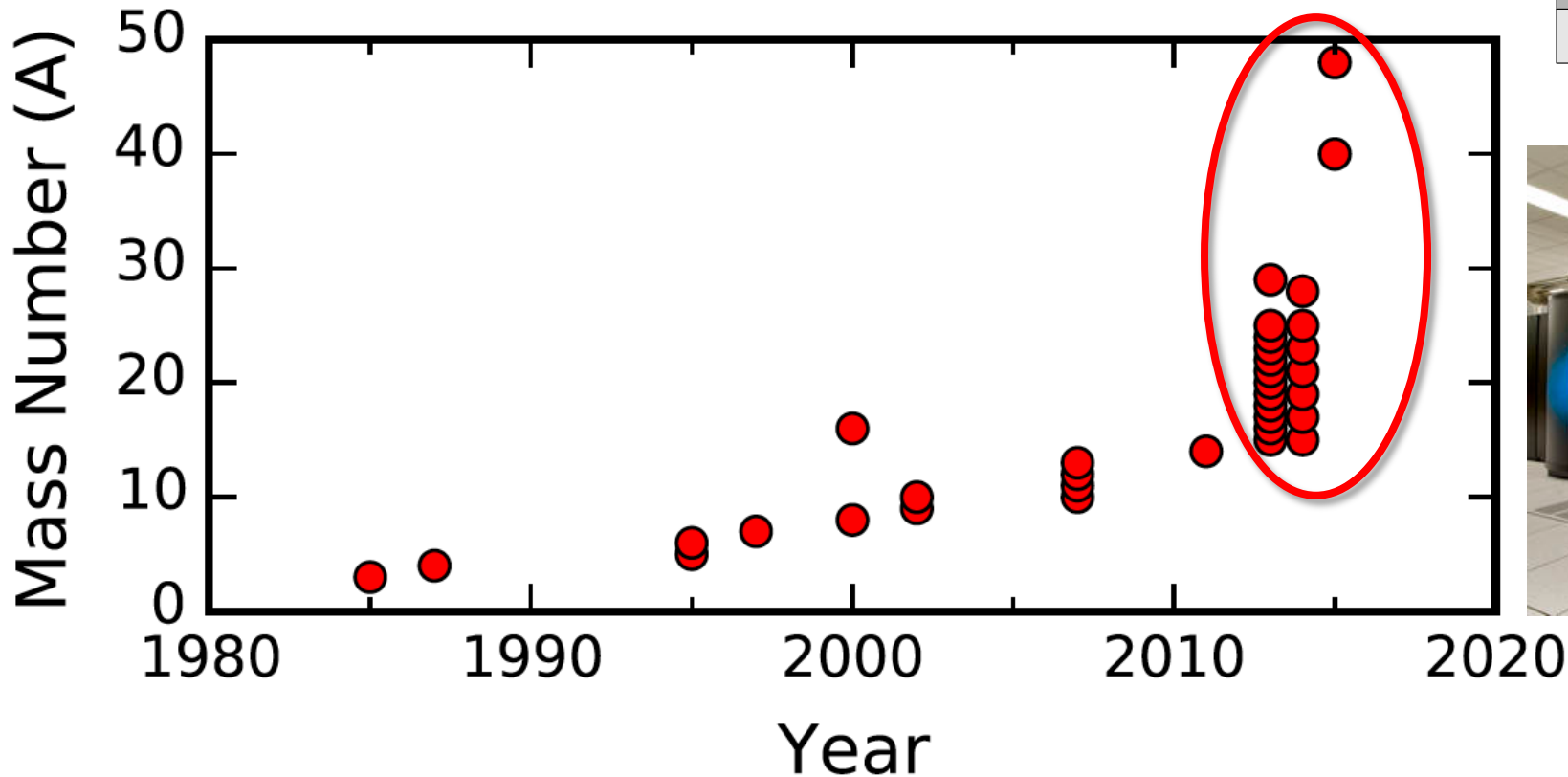
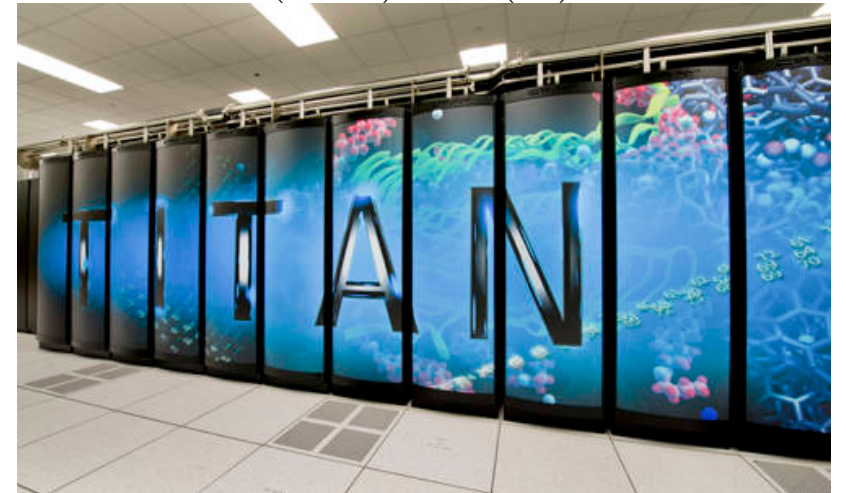
Methods for light nuclei (QMC, NCSM) scale exponentially with mass

Polynomial scaling methods developed (CC, VS-IMSRG, SCGF)

Explosion in limits of ab initio theory 



$$H(s=0) \rightarrow H(\infty)$$



Moore's law: exponential growth in computing power

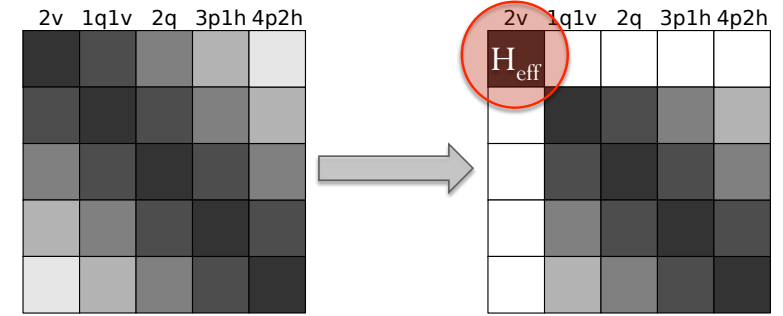
Methods for light nuclei (QMC, NCSM) scale exponentially with mass

Polynomial scaling methods developed (CC, VS-IMSRG,...)

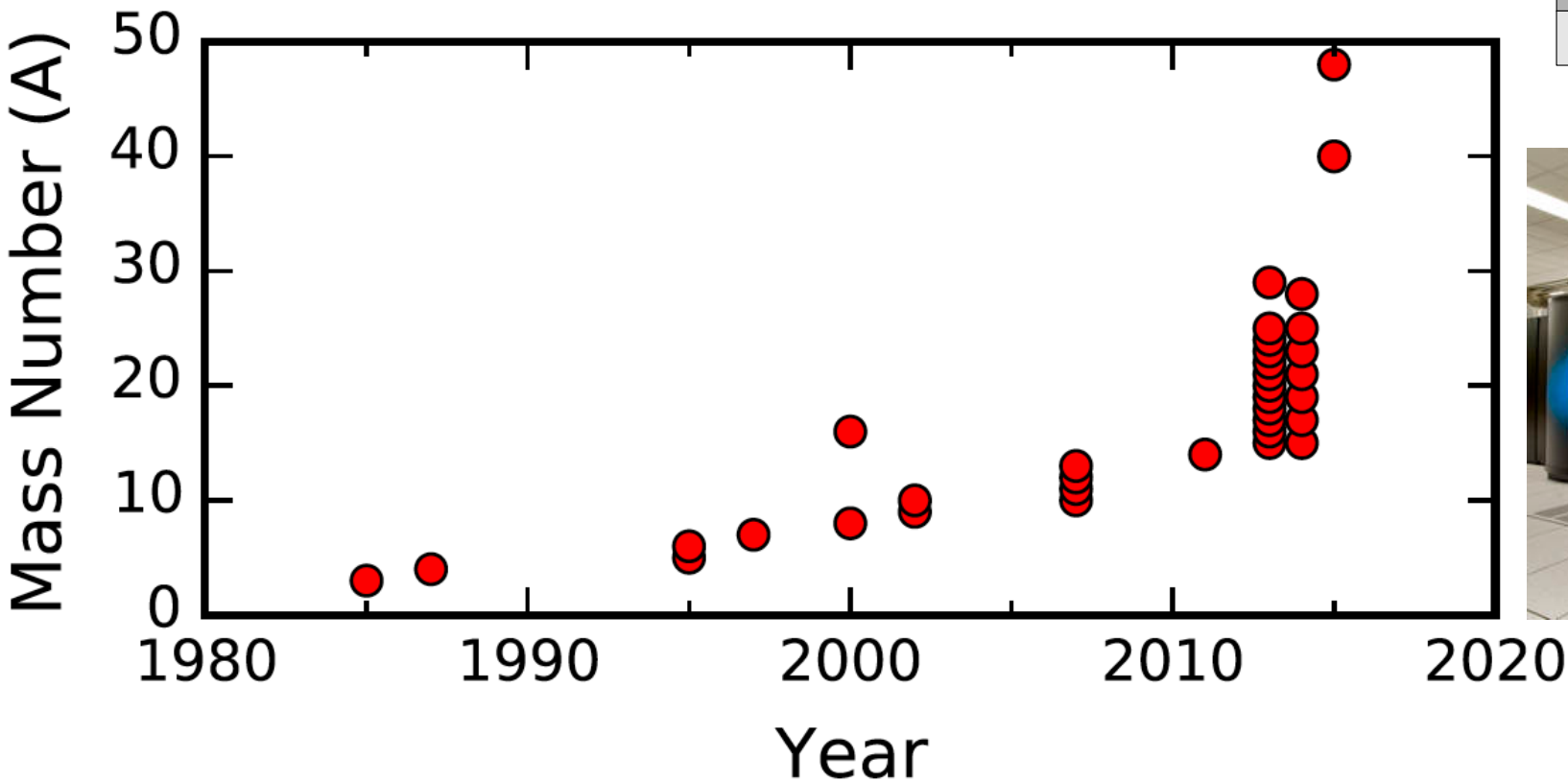
Explosion in limits of ab initio theory



2020: A > 100?



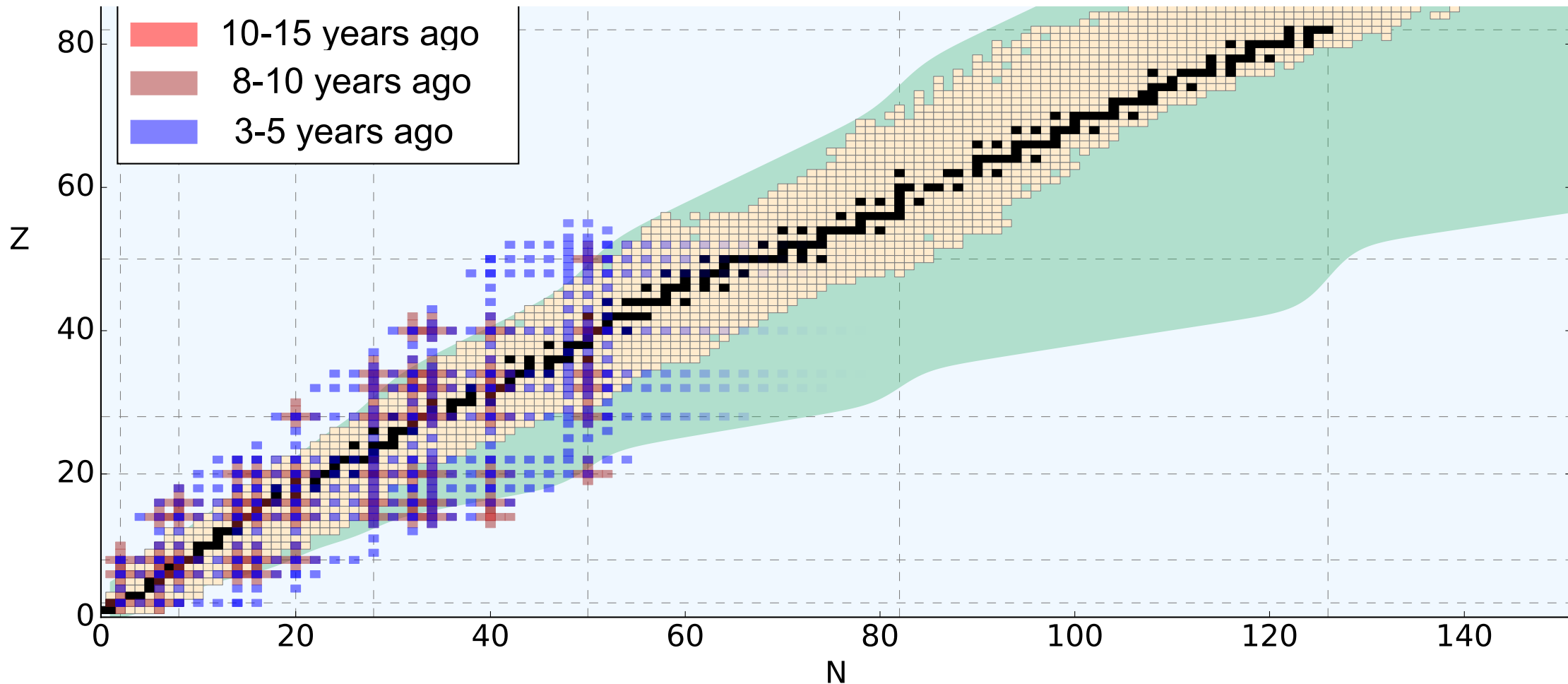
$$H(s=0) \rightarrow H(\infty)$$



Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

- Nuclear forces, electroweak physics
- Nuclear many-body problem

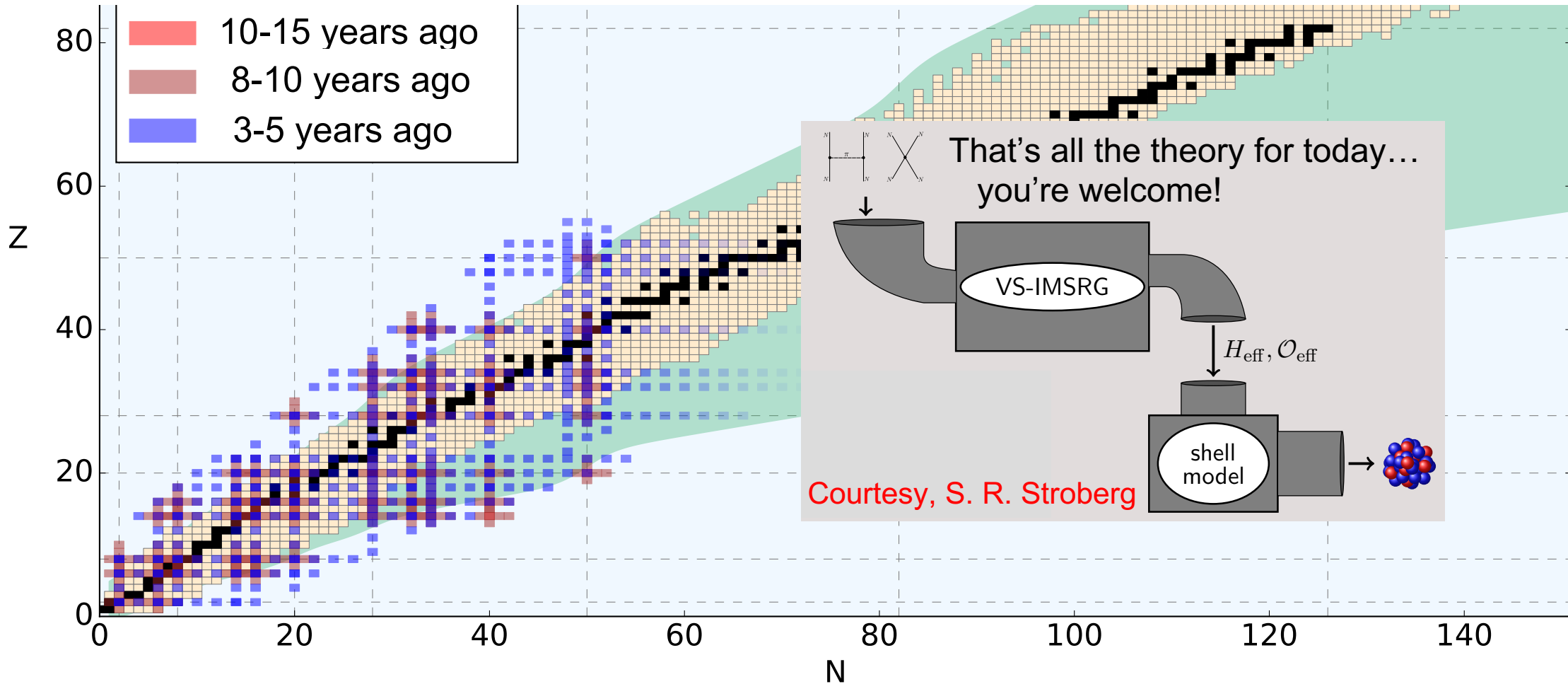
$$H\psi_n = E_n\psi_n$$



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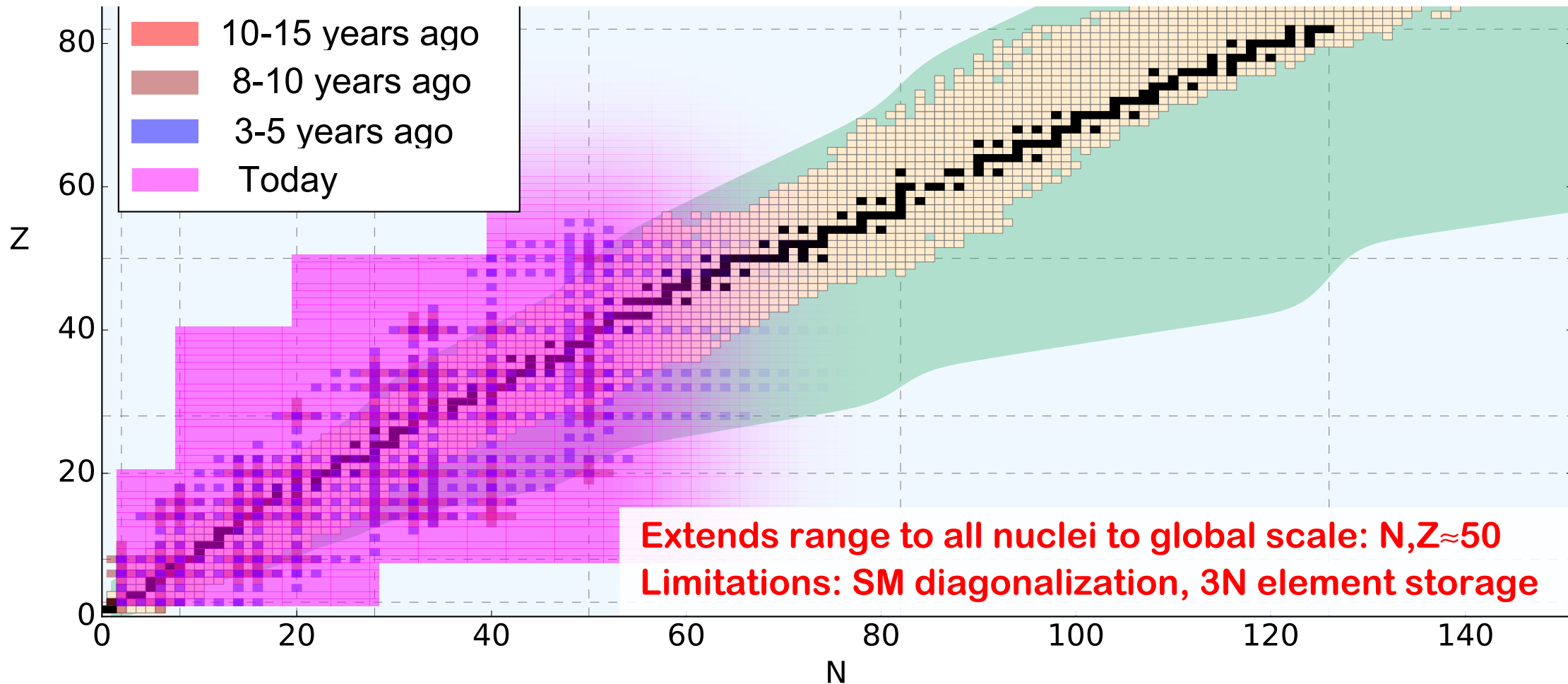
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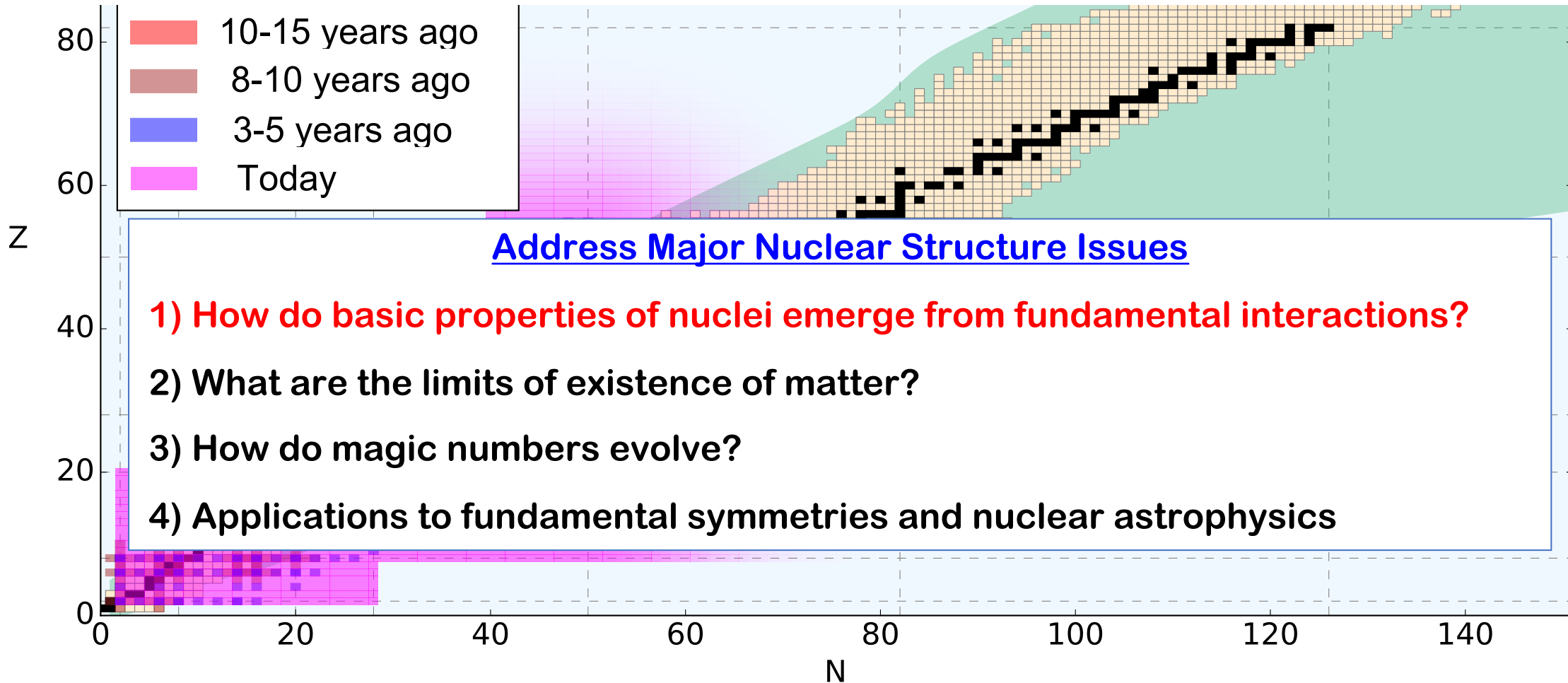
$$H\psi_n = E_n\psi_n$$



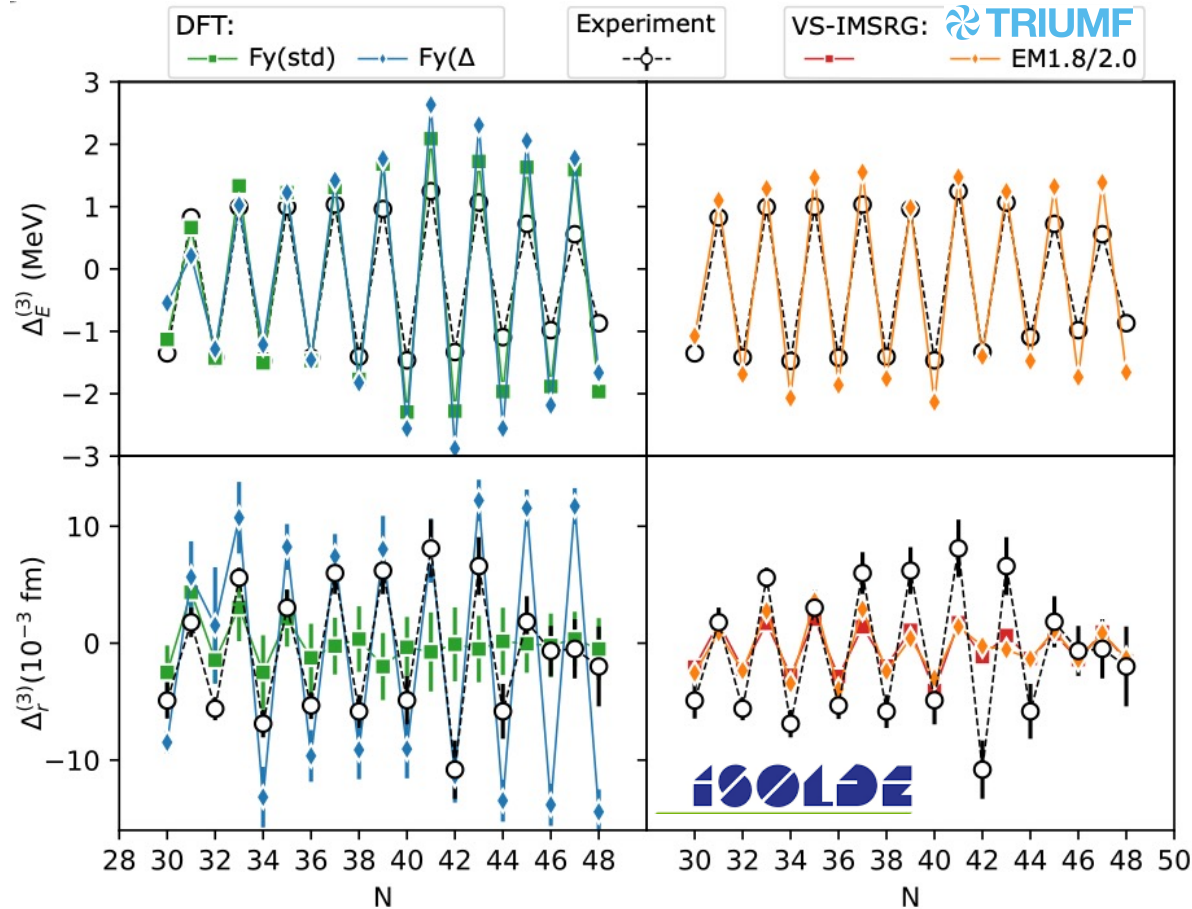
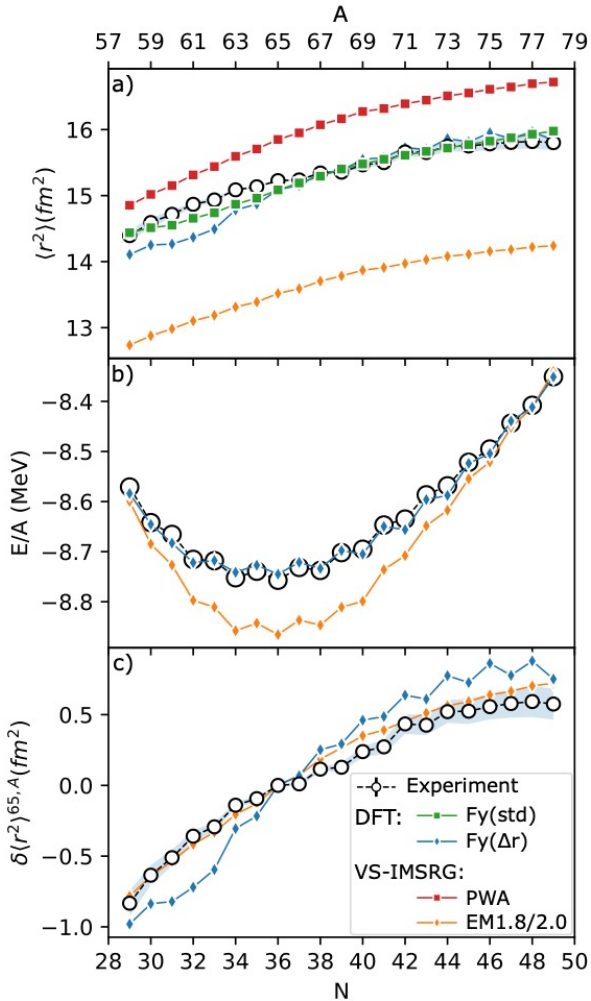
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$$H\psi_n = E_n\psi_n$$



Study odd-even staggering of charge radii across isotopic chains



$$\langle R^2 \rangle = \langle \Phi_0 | \tilde{R}^2 | \Phi_0 \rangle + \langle \Phi_{SM} | \tilde{R}^2 | \Phi_{SM} \rangle$$

de Groote et al., Nature Phys. (2019)

Cu isotopes, odd-even staggering well reproduced

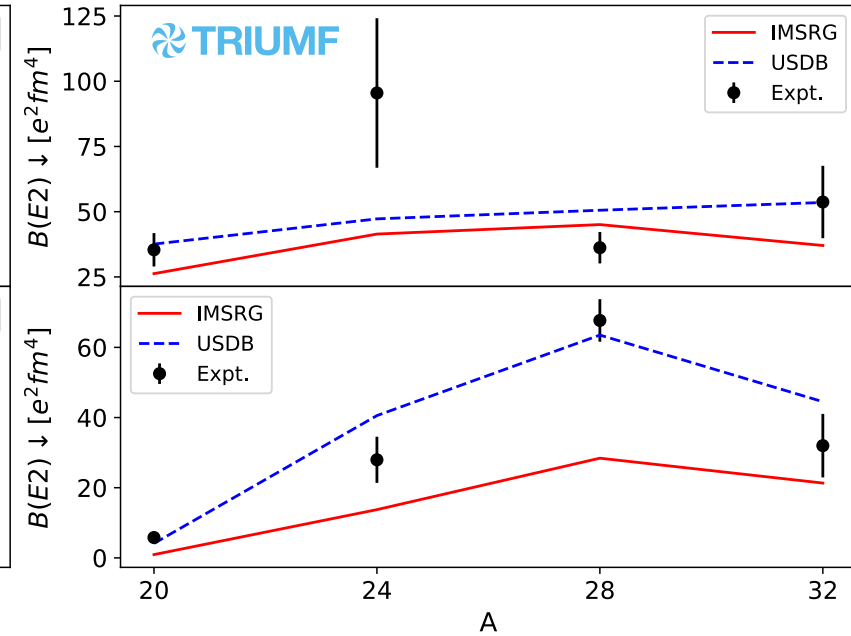
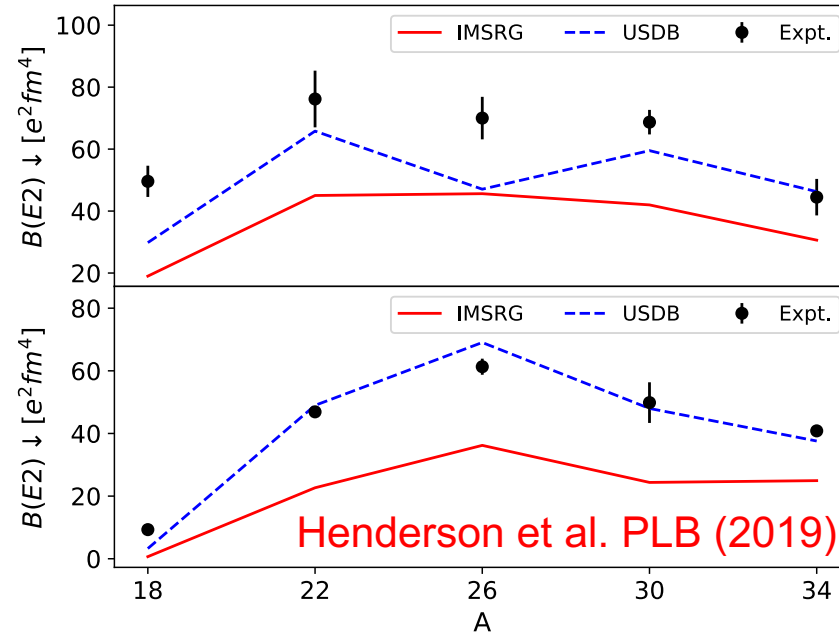
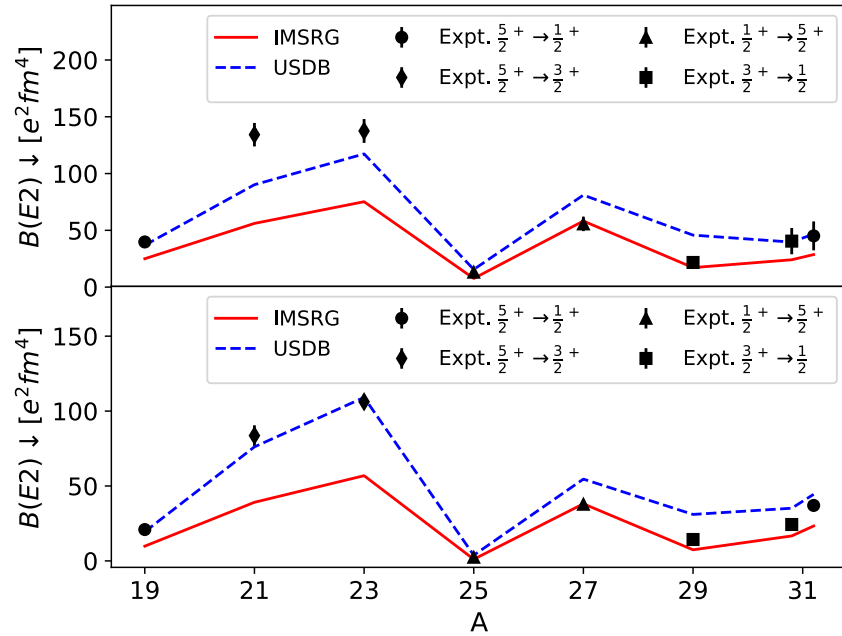
Ab initio competitive with DFT (fit to reproduce odd-even staggering)

Study charge E2 transitions across sd-shell

$$T_z = \pm \frac{1}{2}$$

$$T_z = \pm 1$$

$$T_z = \pm \frac{3}{2}$$

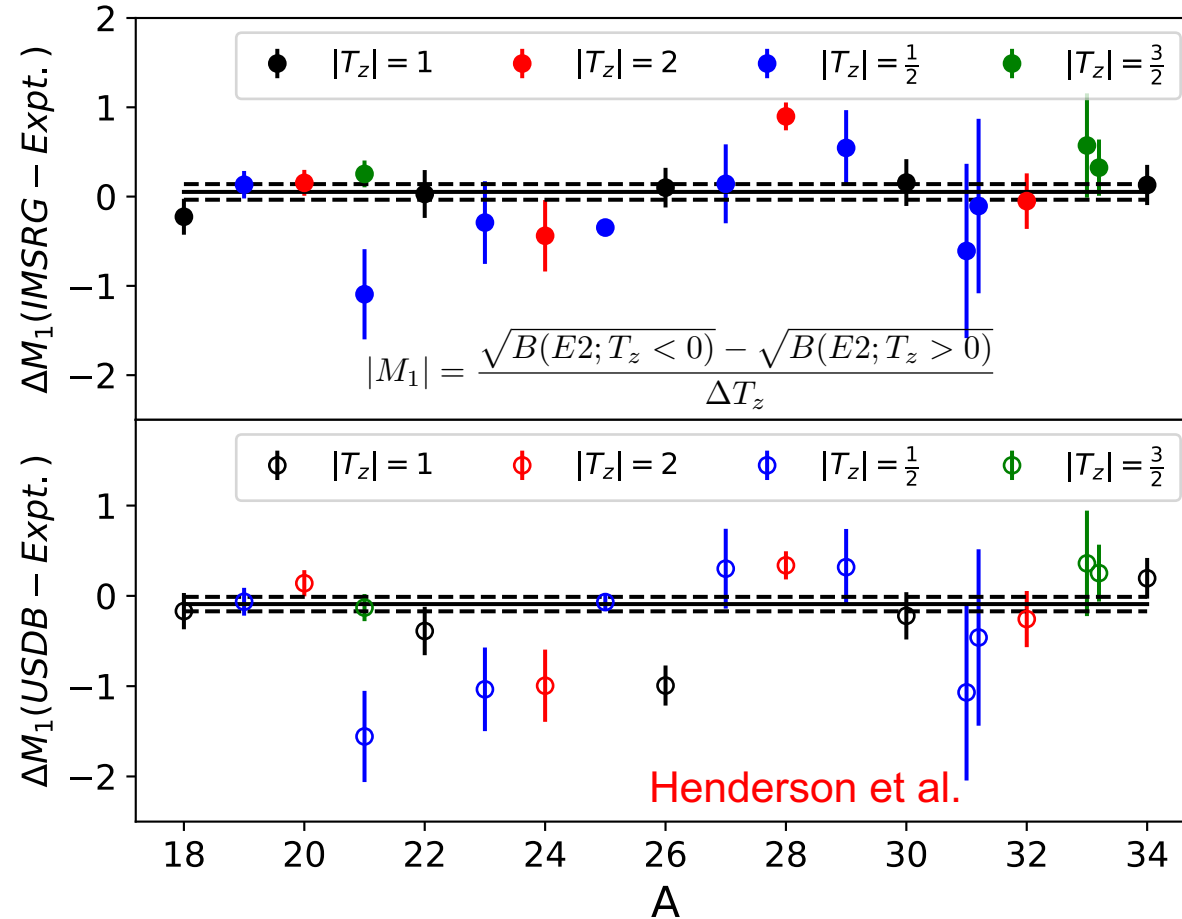
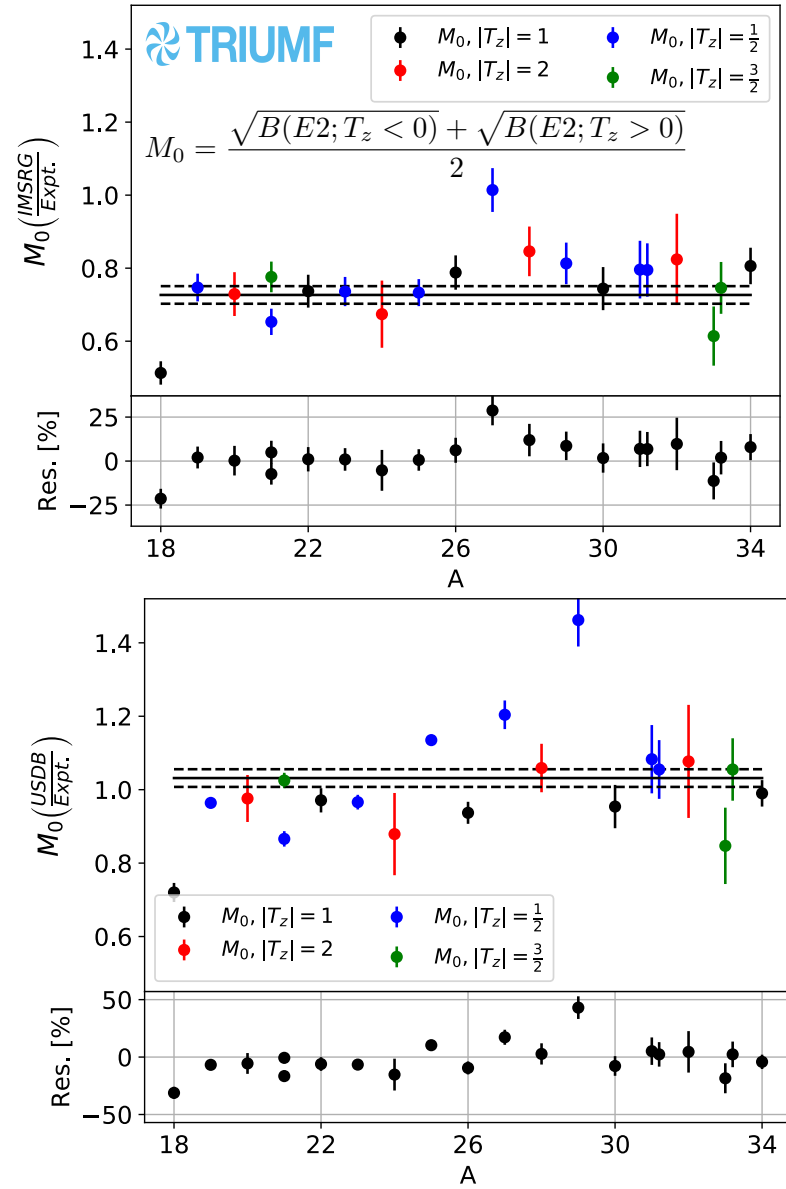


USDB with effective charges typically reproduces absolute values well

VS-IMSRG (**no effective charges**) typically underpredicts experiment

Trends well reproduced in both...

Study charge E2 transitions across sd-shell: IS (M_0) and IV (M_1)



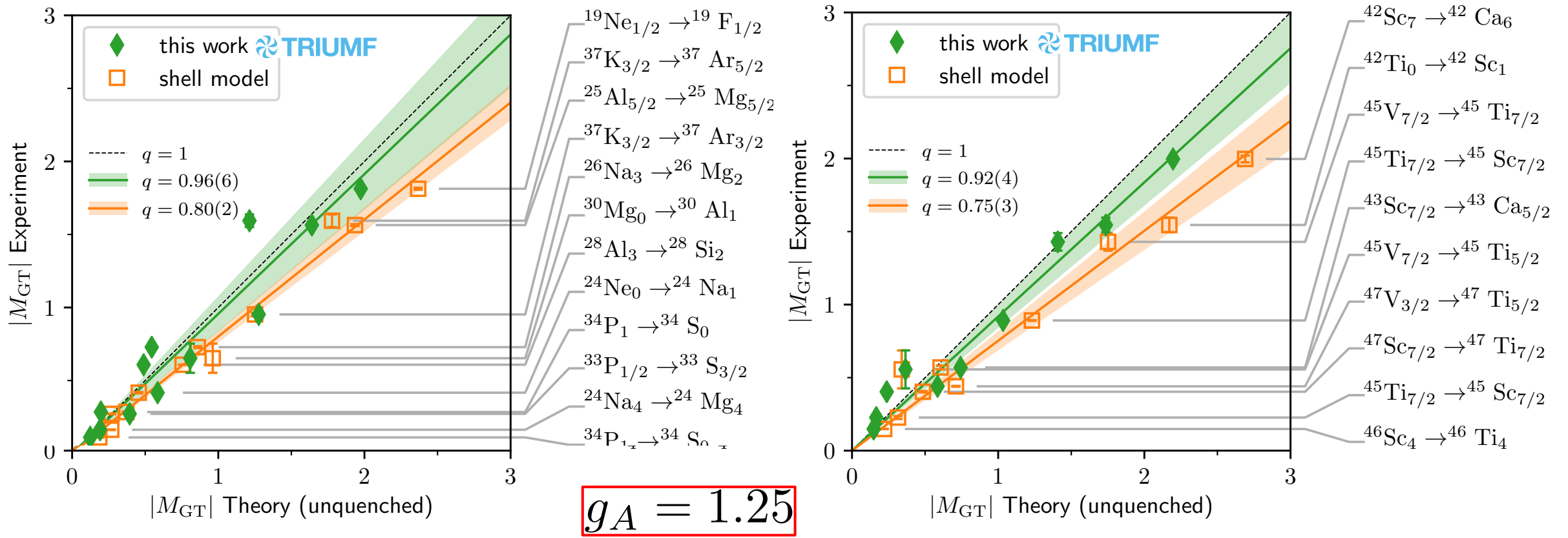
IS: USDB good agreement, VS-IMSrg systematically small

IV: Both agree well

Deficiencies in IS only

Comparison to standard phenomenological shell model

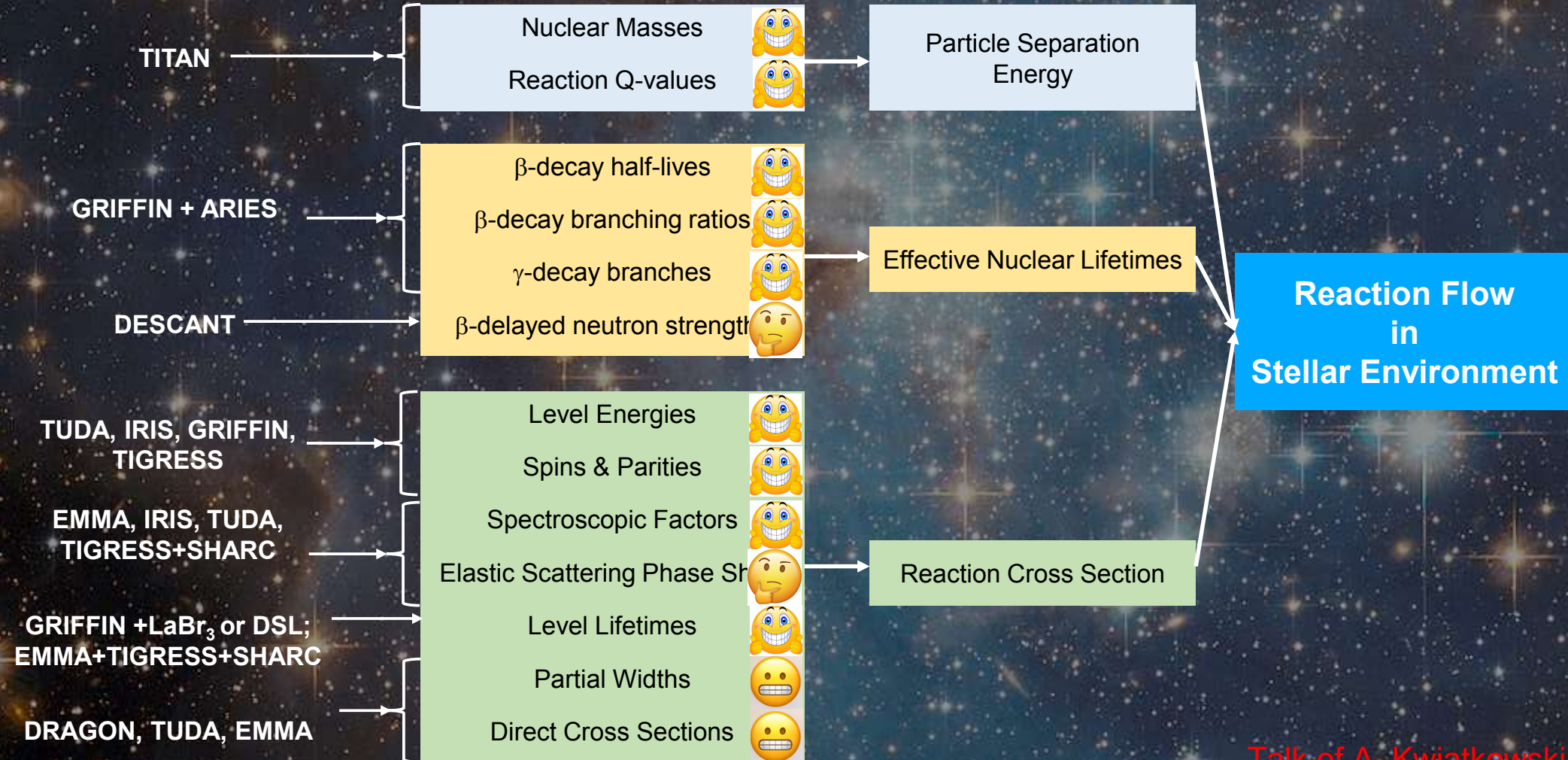
Ab initio calculations across the chart explain data with free-space g_A



Gysbers et al., Nature Phys. (2019)

Refine results with improvements in forces and many-body methods

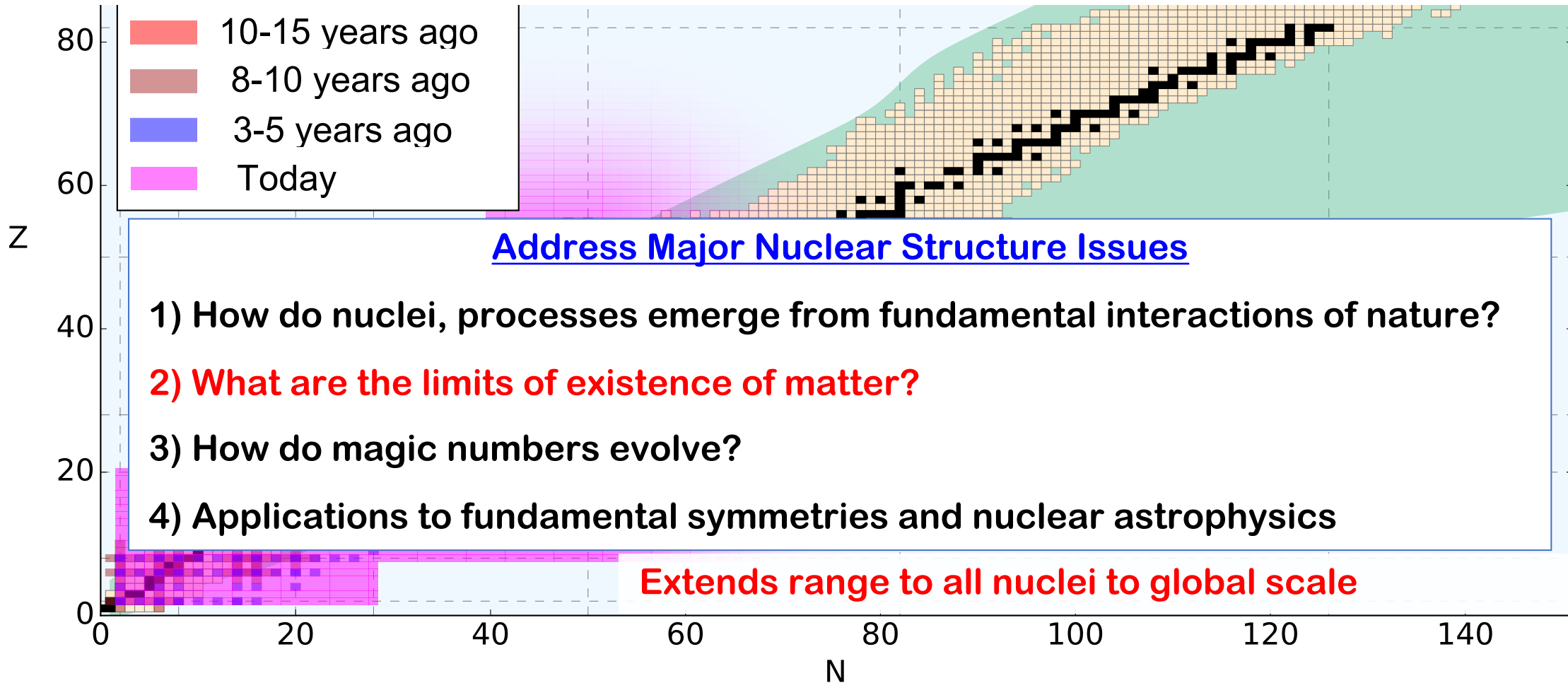
TRIUMF's nuclear astrophysics program in the era of multi-messenger astronomy



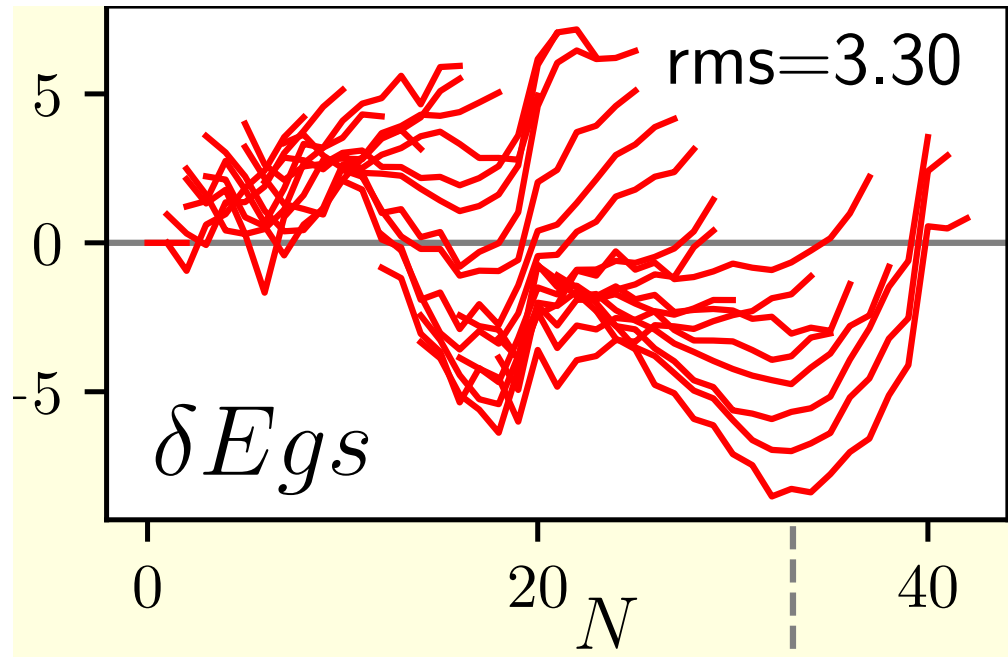
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$$H\psi_n = E_n\psi_n$$



Ab initio calculations of nearly 700 nuclei... how to analyze uncertainties?



$$\delta \mathcal{O} \equiv \mathcal{O}^{(th)} - \mathcal{O}^{(exp)}$$

B-W Mass formula: 3.1MeV Z<28

3.5MeV Z<20

DFT: 0.6-2.0 MeV

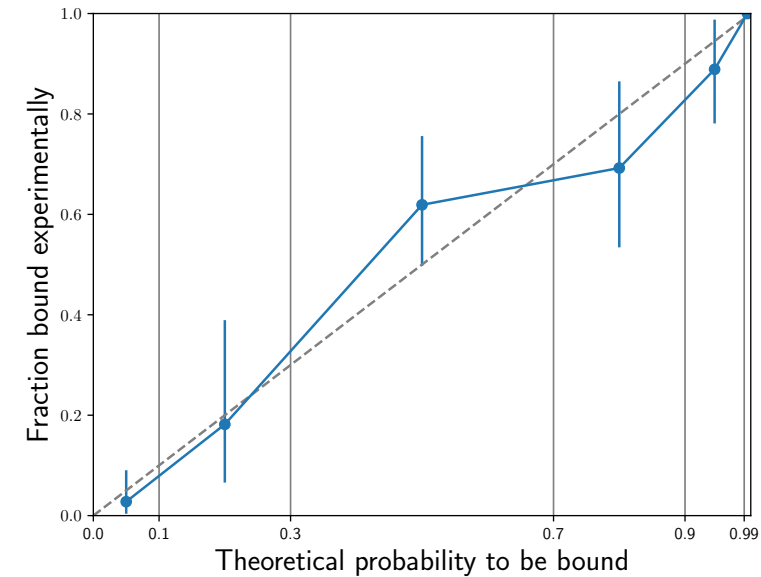
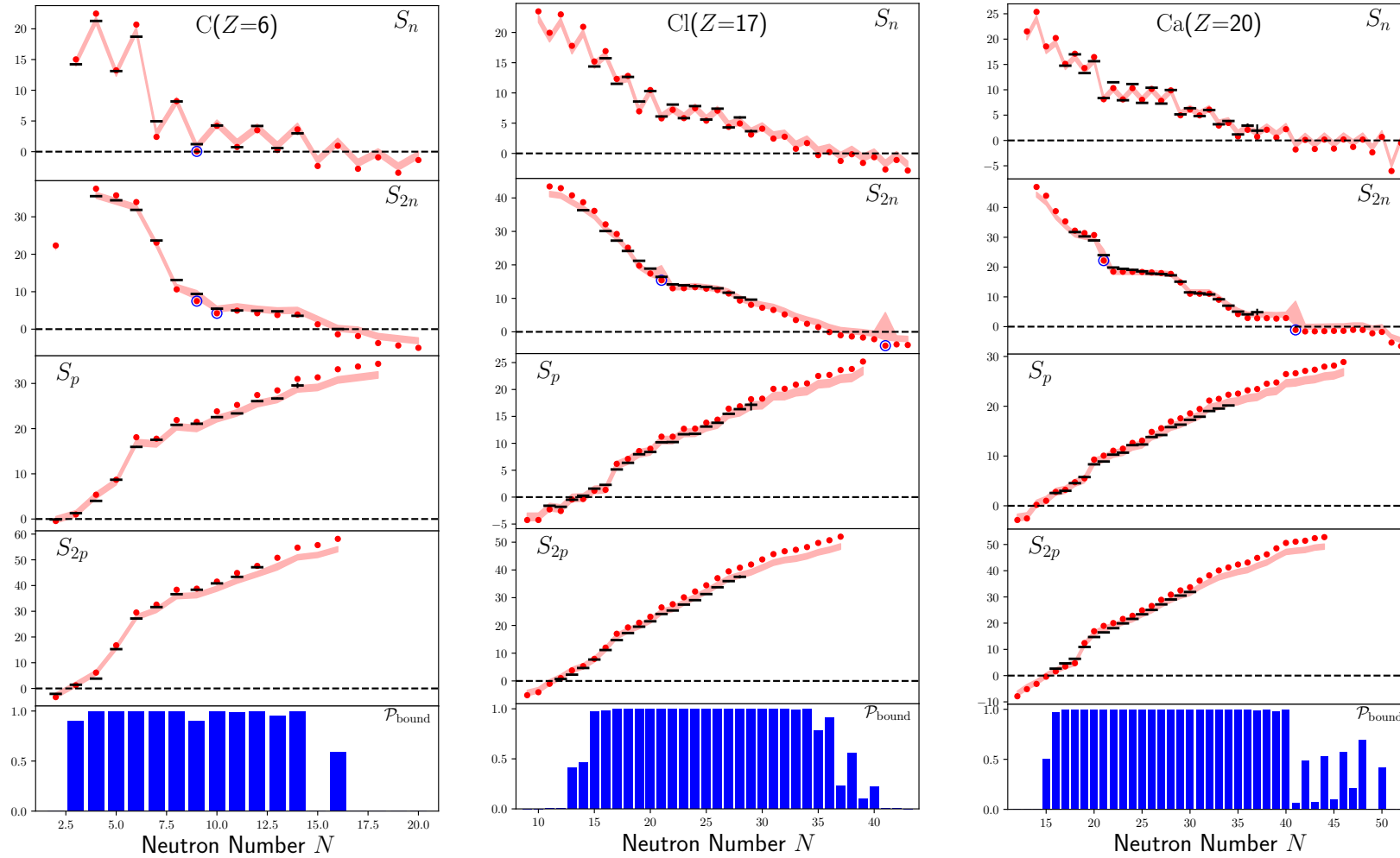
Stroberg et al arXiv:1905.10475

rms deviation at level of BW Mass formula, approaching EDF models

Input Hamiltonians fit to A=2,3,4 – not biased towards known data

What is deviation for separation energies? **Apply to nuclear driplines**

Determine rms deviation from experiment – extrapolate this uncertainty beyond data

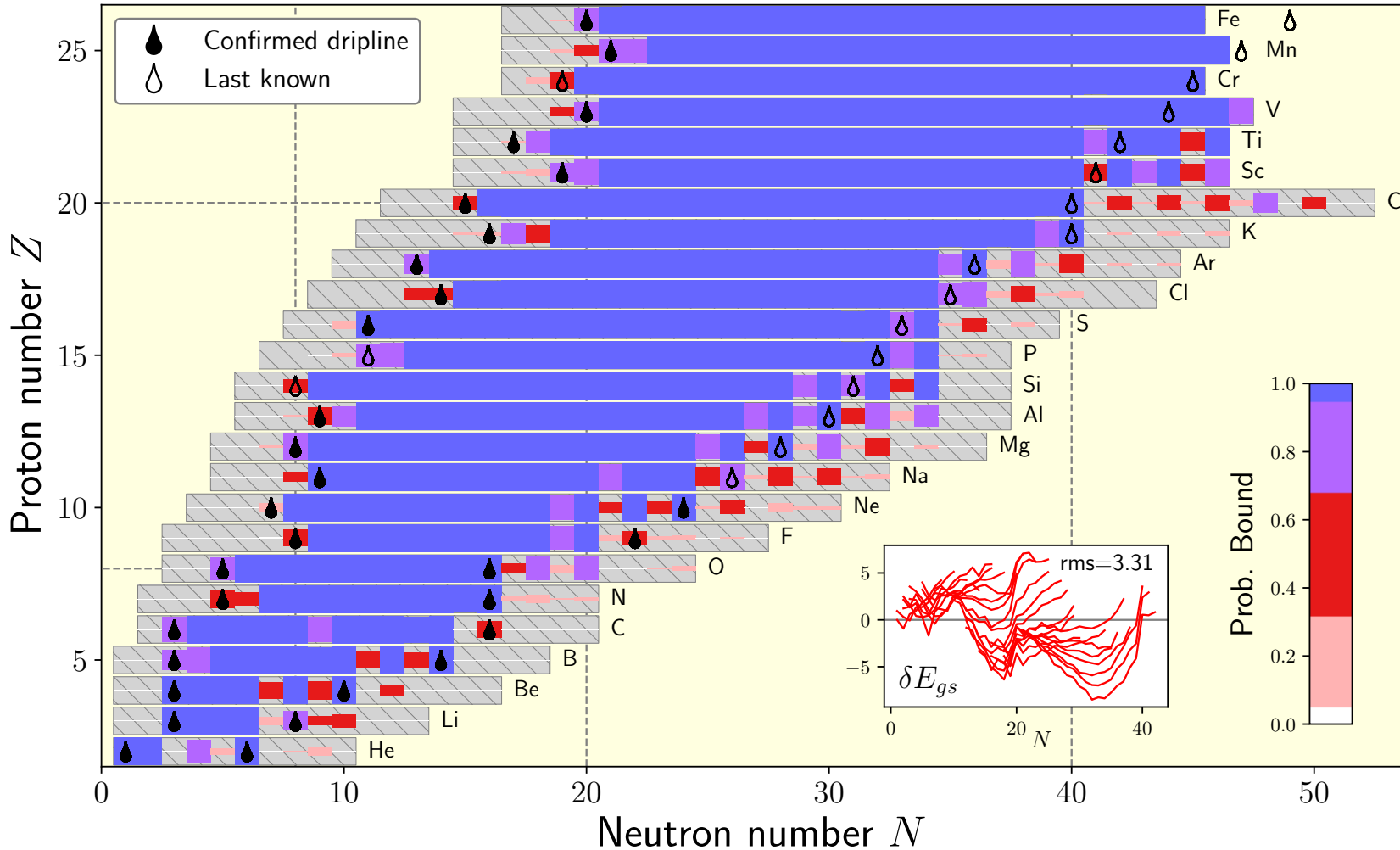


Determine range of likely separation energies reaching 0

Stroberg et al arXiv:1905.10475

Assign probability that a particular nucleus is bound

First predictions of proton and neutron driplines from first principles



$$\mathcal{P}_{1n} = \frac{1}{\sqrt{2\pi}\sigma_{1n}} \int_0^\infty \exp\left(-\frac{(x - S_n^{th.corr})^2}{2\sigma_{1n}^2}\right) dx$$

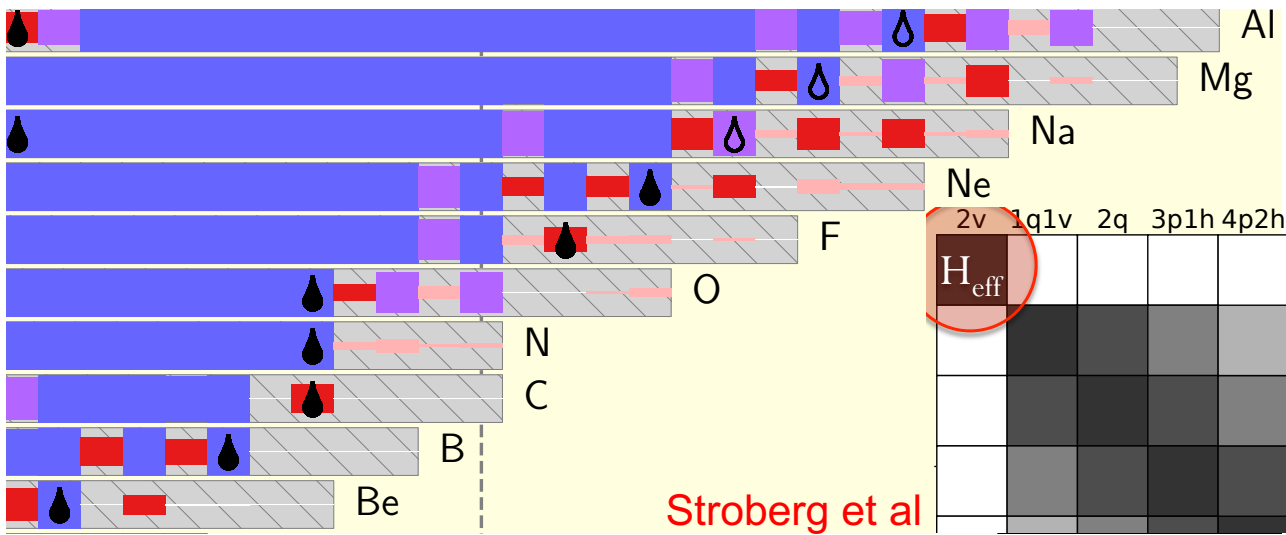
$$\mathcal{P}_{bound} = (\mathcal{P}_{1n}\mathcal{P}_{2n} + \xi_{1n,2n})(\mathcal{P}_{1p}\mathcal{P}_{2p} + \xi_{1p,2p})$$

Stroberg et al arXiv:1905.10475

Known drip lines largely predicted within uncertainties (issues remain at shell closures)

Provide *ab initio* predictions for neutron-rich region

New measurements determine dripline in F and Ne isotopes, extend known Na isotopes



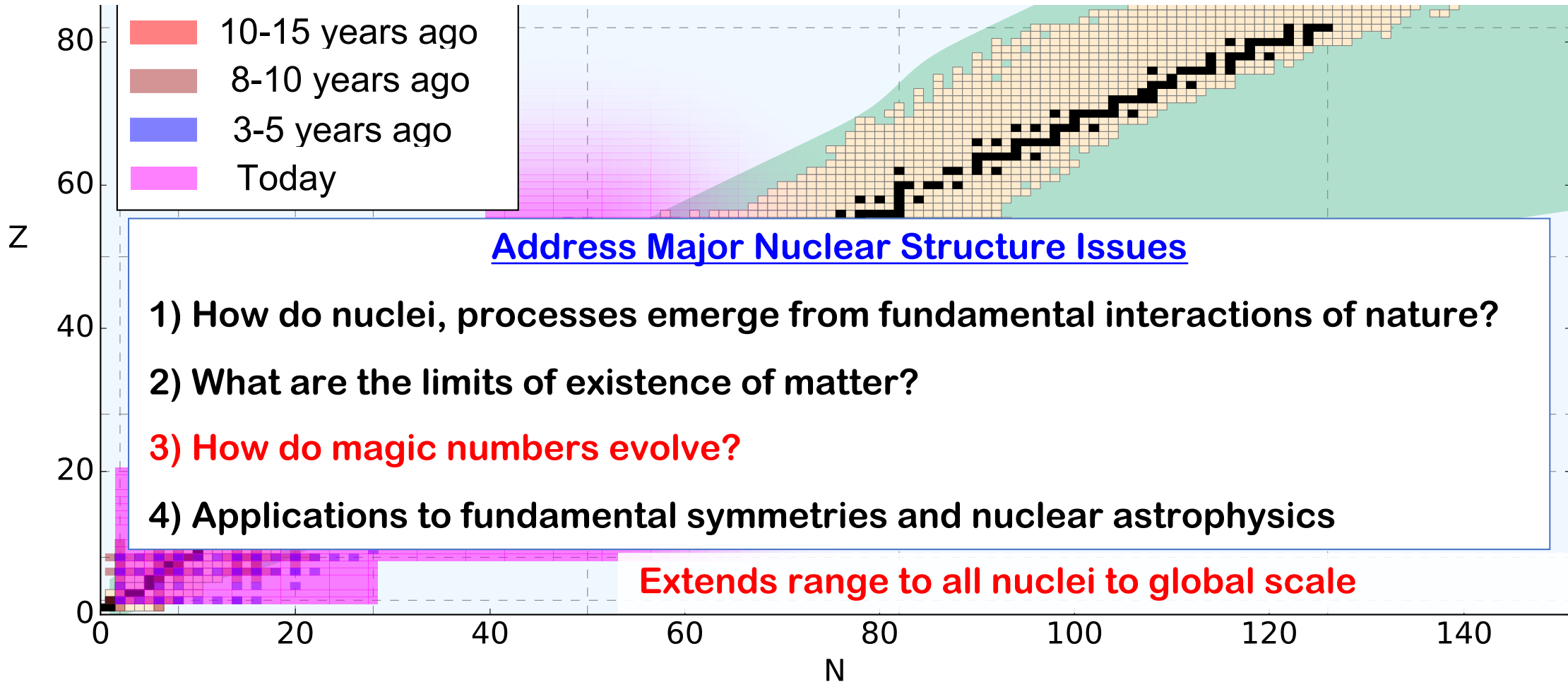
All new measurements agrees well with ab initio predictions

Next-generation RIB aim to extend driplines to Ca!

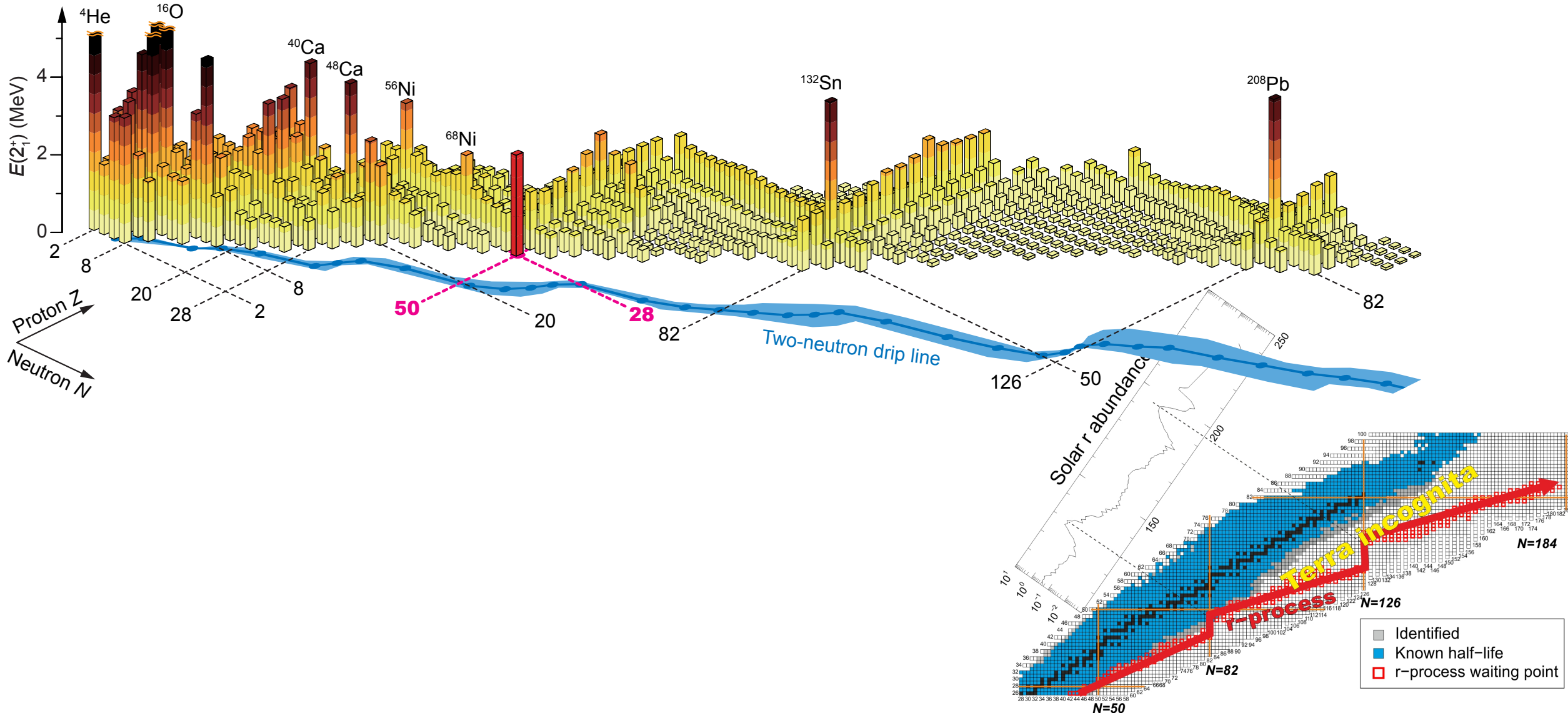
Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

- Nuclear forces, electroweak physics
- Nuclear many-body problem

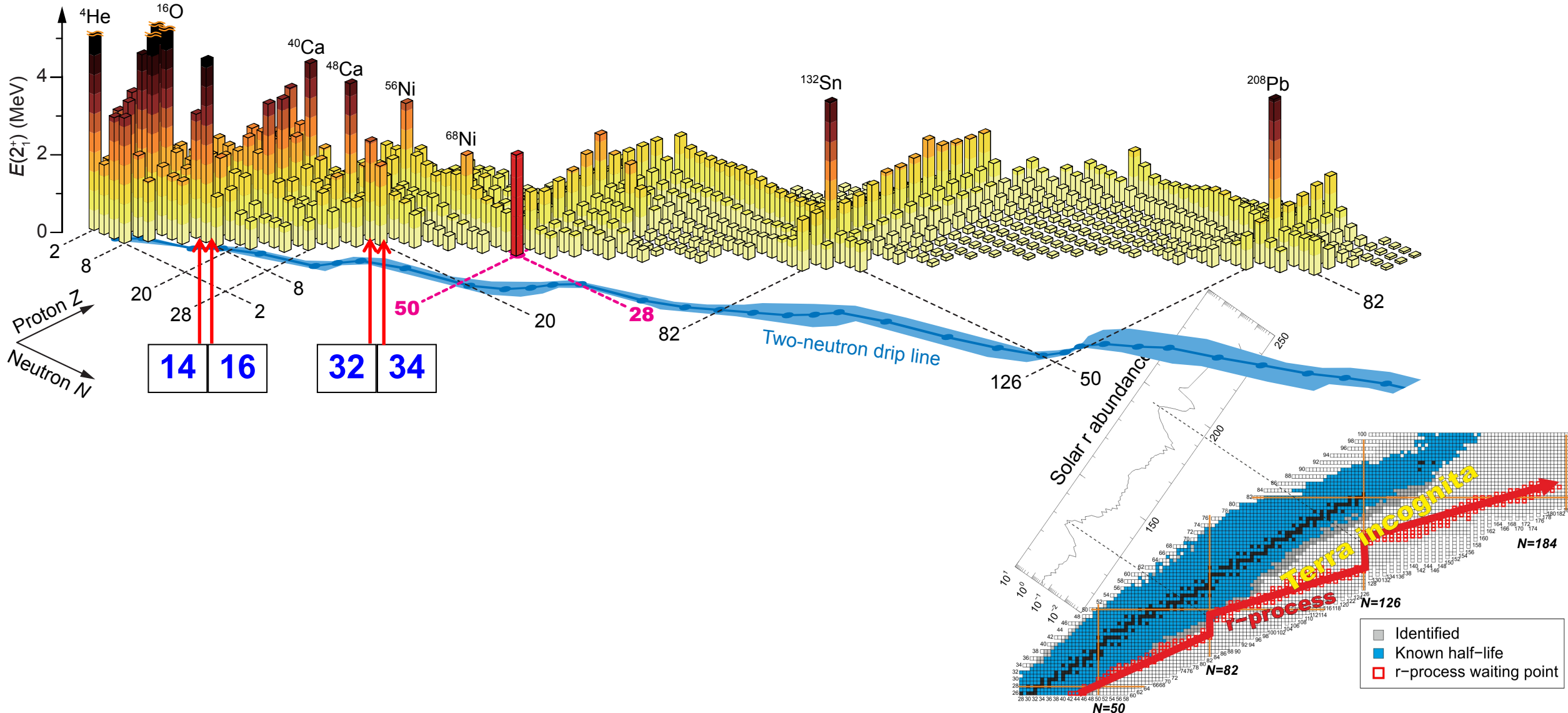
$$H\psi_n = E_n\psi_n$$



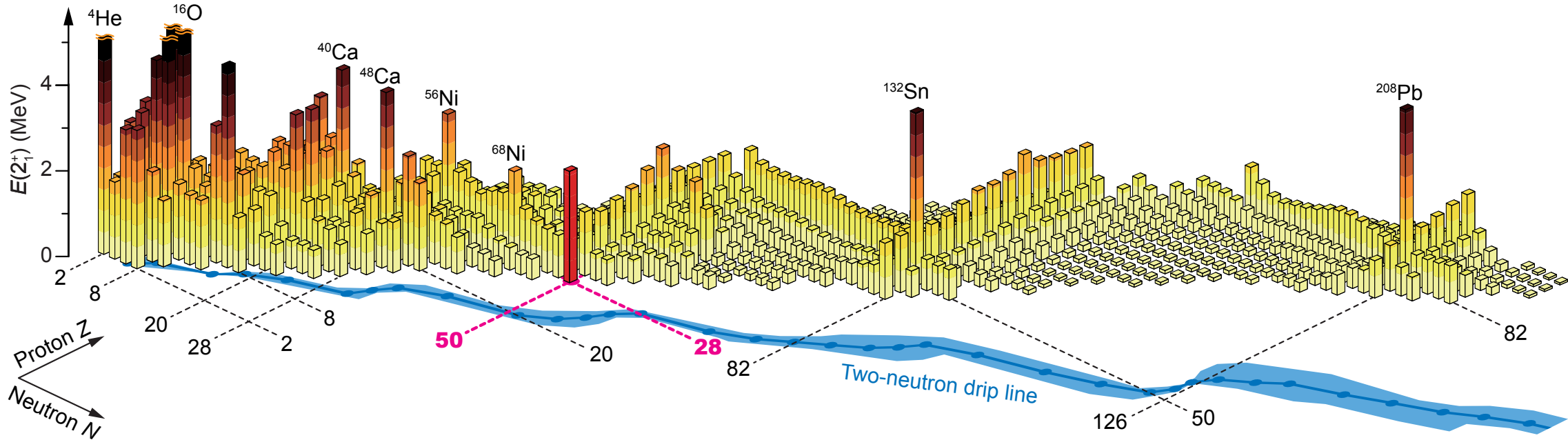
Magic numbers: pillars of nuclear structure, vital for r-process nucleosynthesis



Magic numbers: pillars of nuclear structure, **novel evolution in exotic nuclei**



Magic numbers: pillars of nuclear structure, novel evolution in exotic nuclei

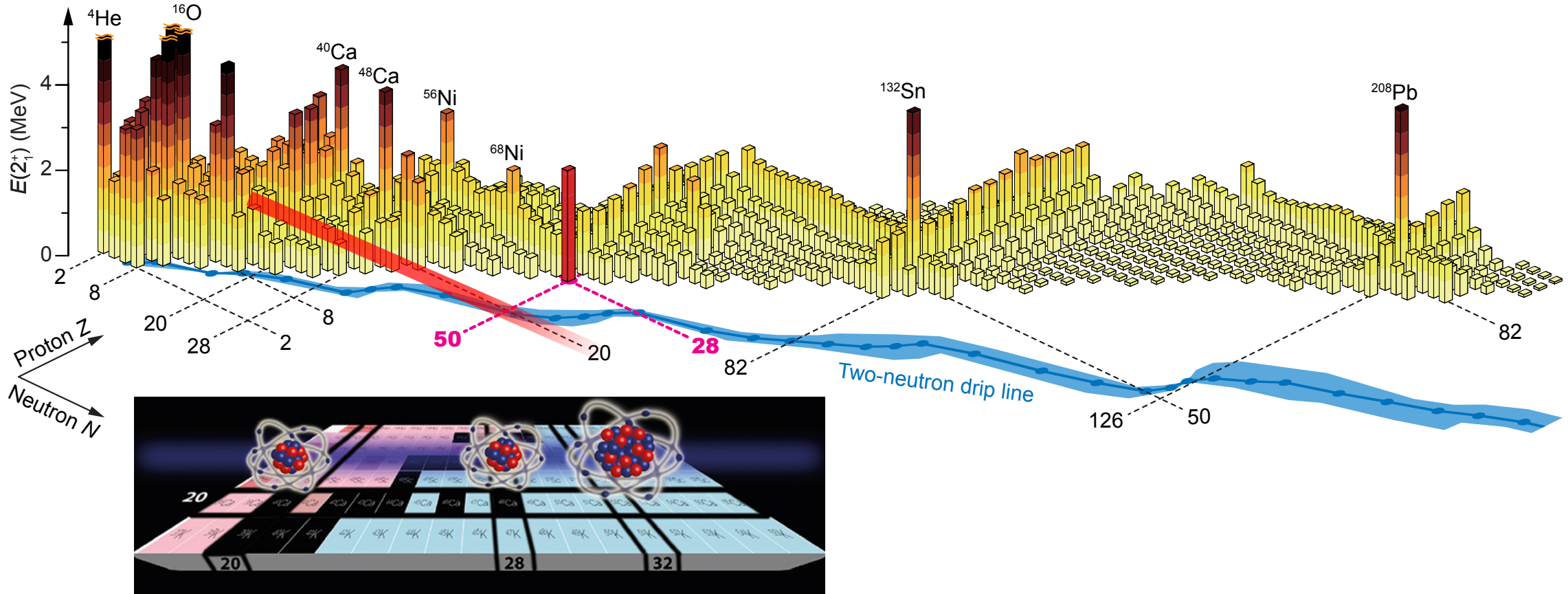


Signatures of Magic Numbers

- Sharp decrease in separation energy (masses)
- Elevated first excited 2_+ energy (spectroscopy)
- Tightly bound (decreased radii)

Must observe all signatures – many experiments (and calculations) needed!

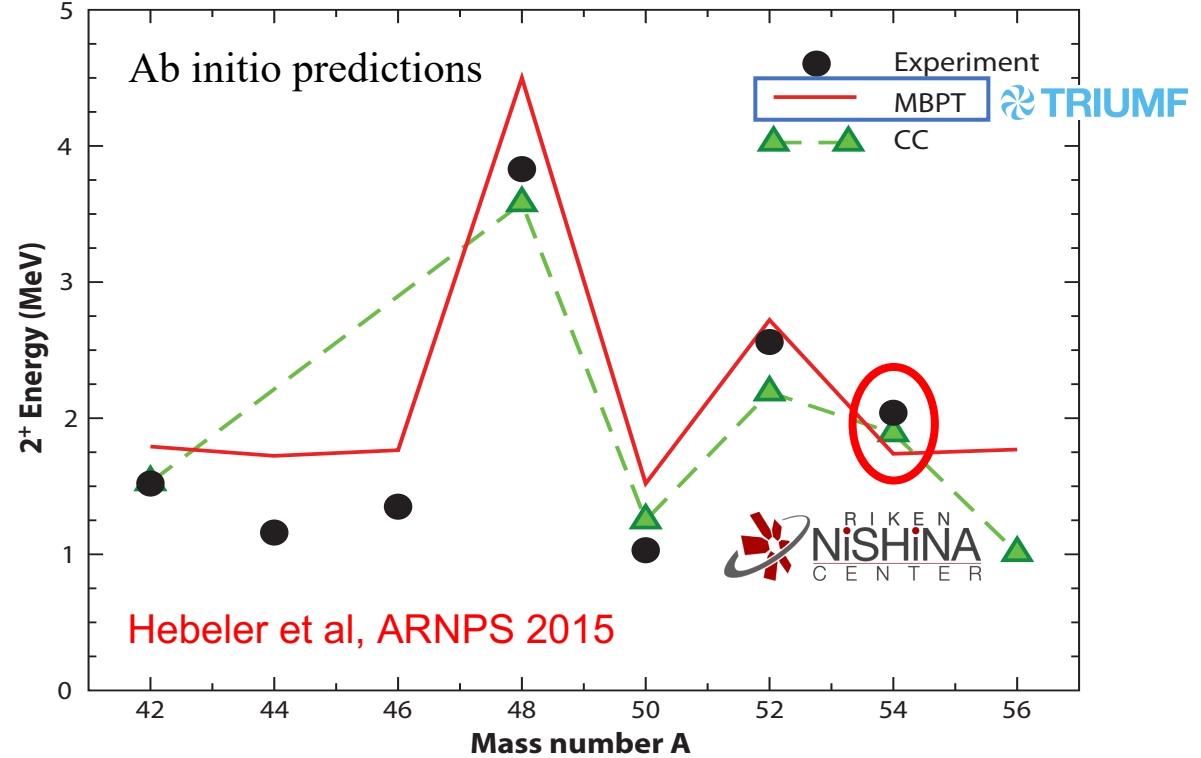
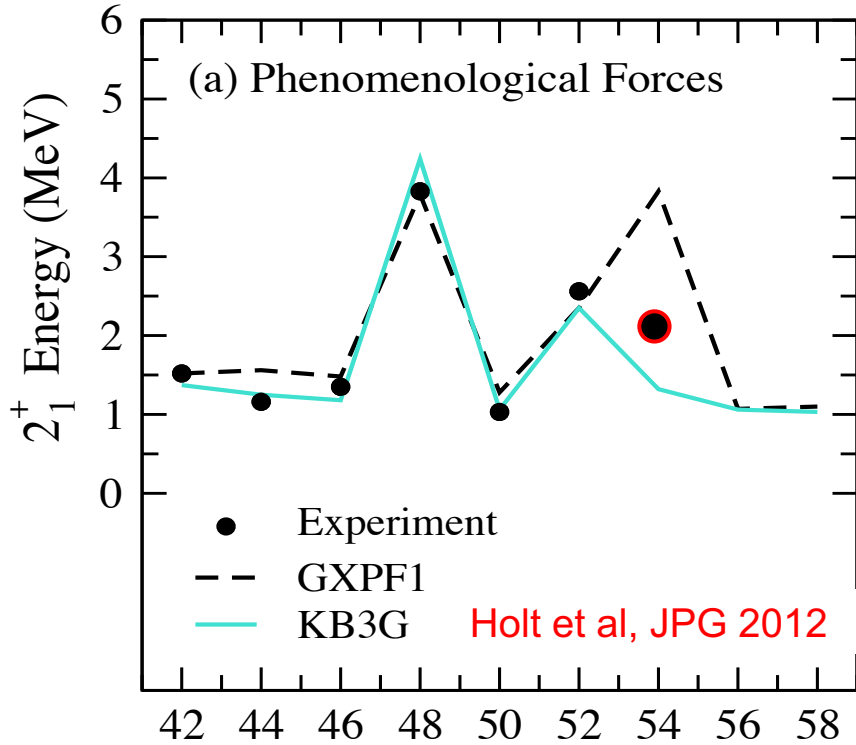
Magic numbers: pillars of nuclear structure, novel evolution in exotic nuclei



Highlight of TRIUMF theory and experiment:

Discovery and evolution of new N=32,34 magic numbers in calcium region

2013 potentially new magic numbers from 2^+ energies: N=32,34 – **New ^{54}Ca measurement at RIKEN**



Phenomenological Models

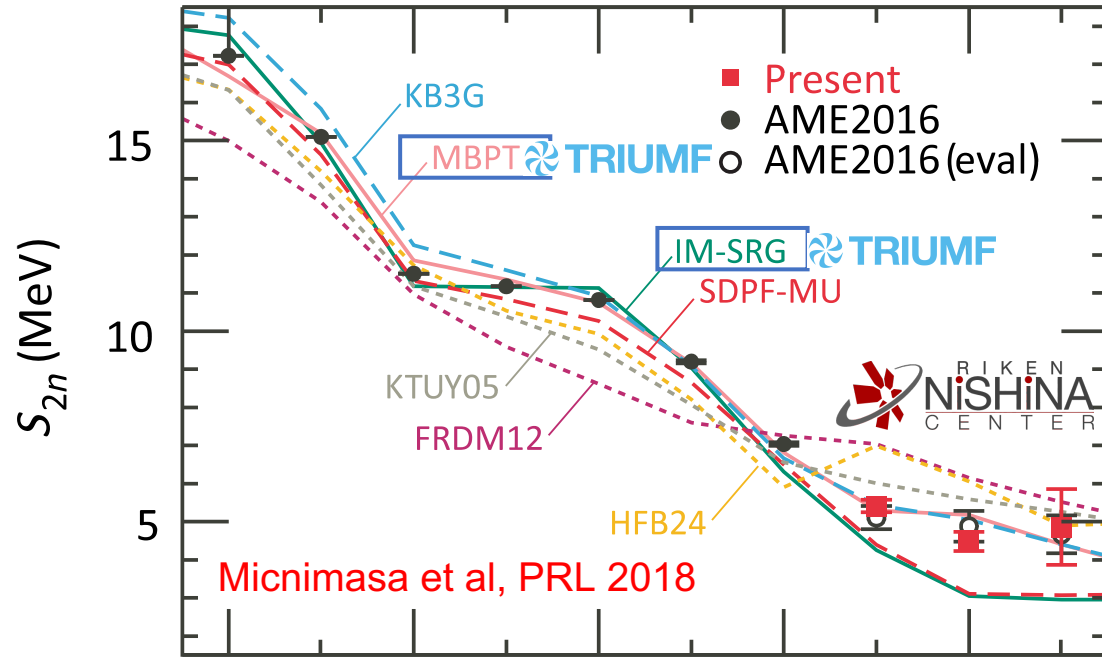
Readjusted to fit new data

Ab initio theories

Correctly predicted excitation energy of N=34!

2013-2018 impressive series of experiments; ideal example of theory/exp overlap

Story continues at RIKEN



TITAN @ TRIUMF Measurement

Flat trend from $^{50-52}\text{Ca}$

^{52}Ca 1.74 MeV deviation from AME!

ISOLTRAP @ CERN Measurement

Sharp decrease from $^{52-54}\text{Ca}$

Confirms N=32 magic number

RIBF @ RIKEN Measurement

Modest decrease past ^{54}Ca

Confirms N=34 magic number

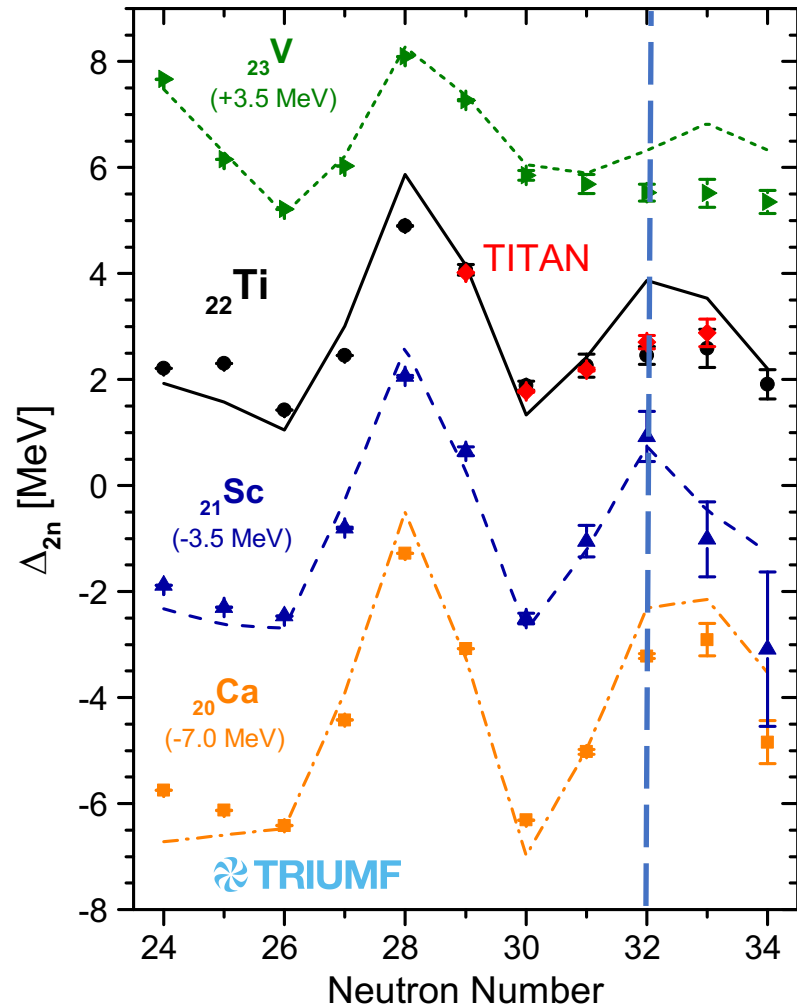
Ab Initio

Excellent agreement with RIBF data

Predicts doubly magic $^{48,52,54}\text{Ca}$

Further questions: how do magic numbers evolve with proton number?

Current frontier of measurements and theory



New TITAN Measurements of Ti masses

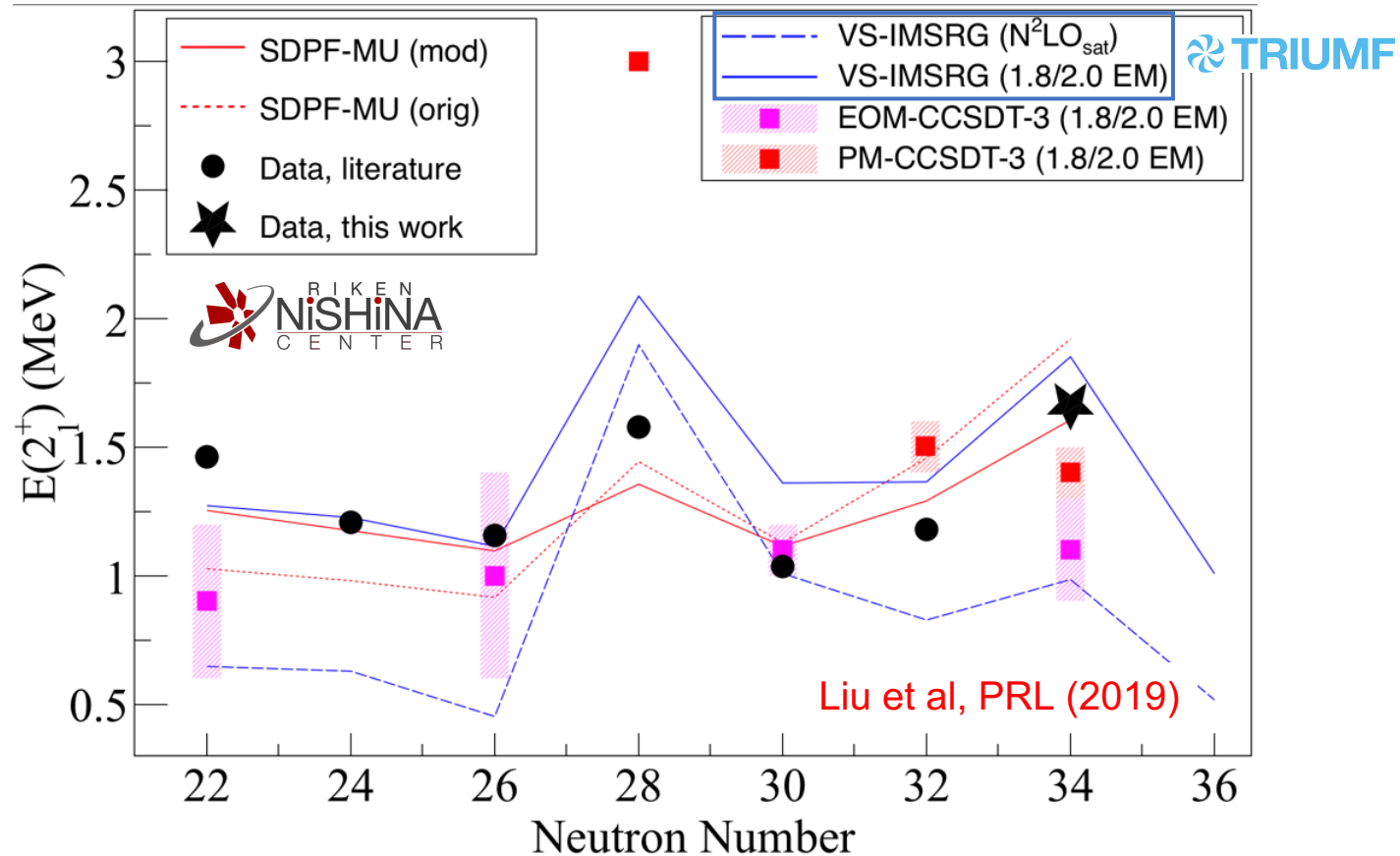
Probe “dawning” of N=32 magic number

Ab Initio from NN+3N

Generally good agreement, but predicts appearance too early

Future: Evolution to be measured in Ar, Cl

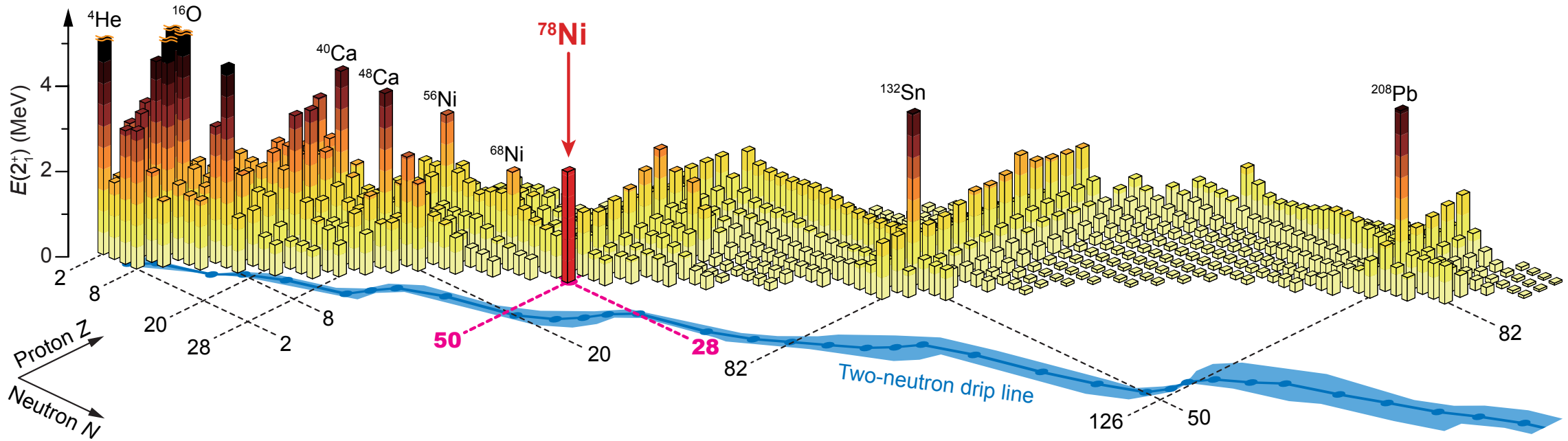
New measurement at RIKEN: 2^+ energy in ^{52}Ar – clear peak at N=34



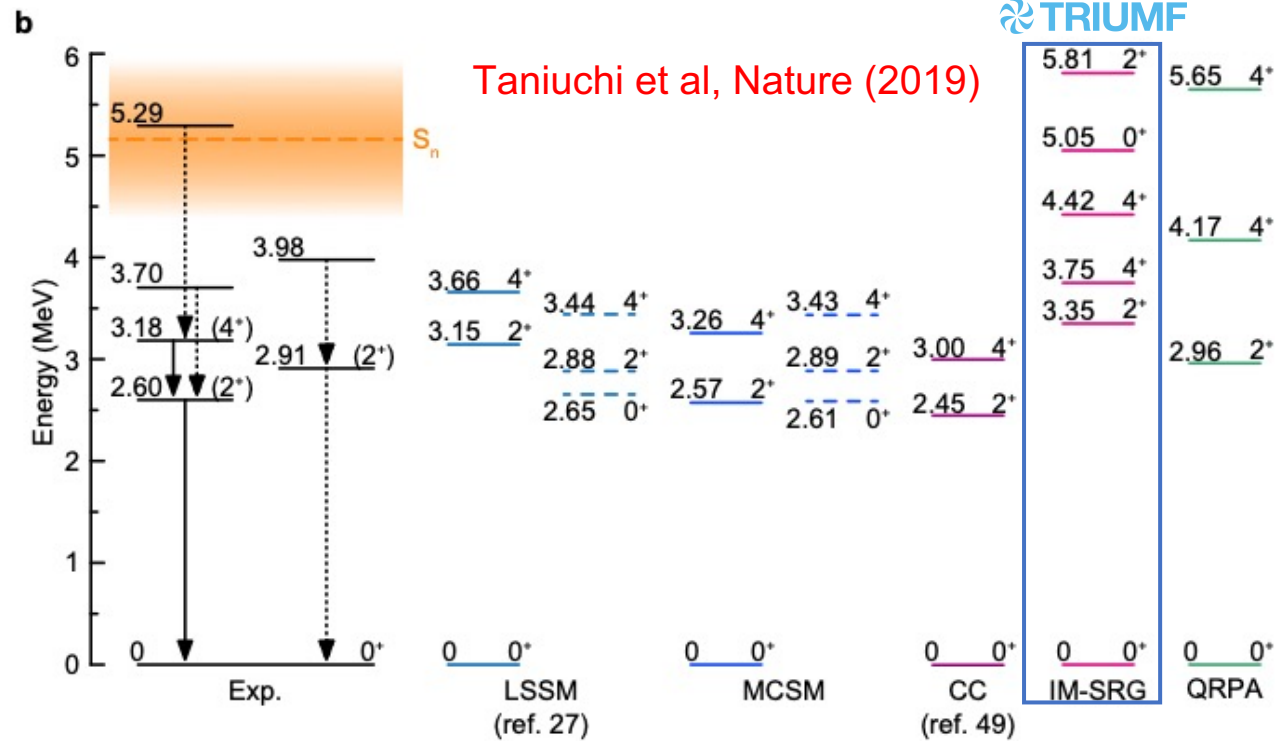
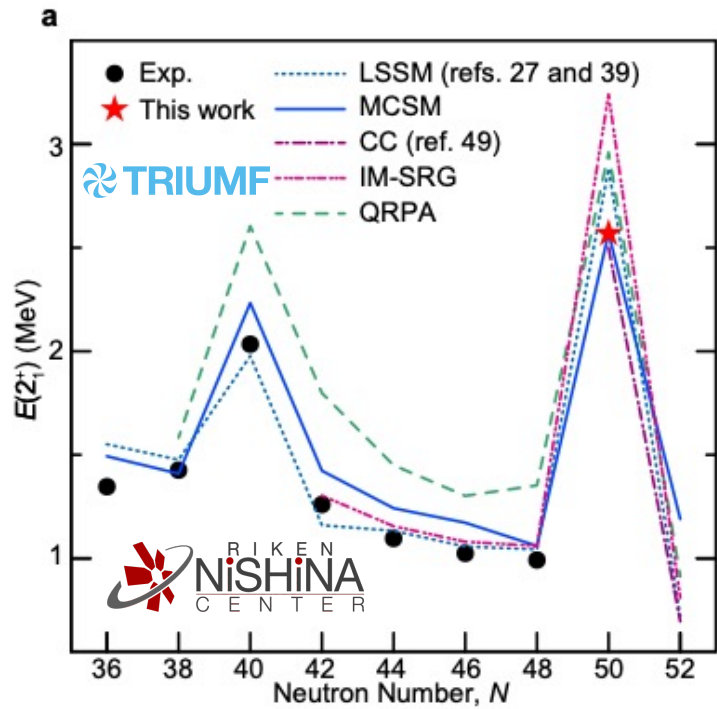
Agreement with IMSRG and other ab initio predictions (coupled cluster theory)

First evidence for persistence of N=34 magic number away from calcium!

Magic numbers: pillars of nuclear structure, novel evolution in exotic nuclei



New measurement at RIKEN 2^+ energy in ^{78}Ni – clear peak compared to ^{76}Ni

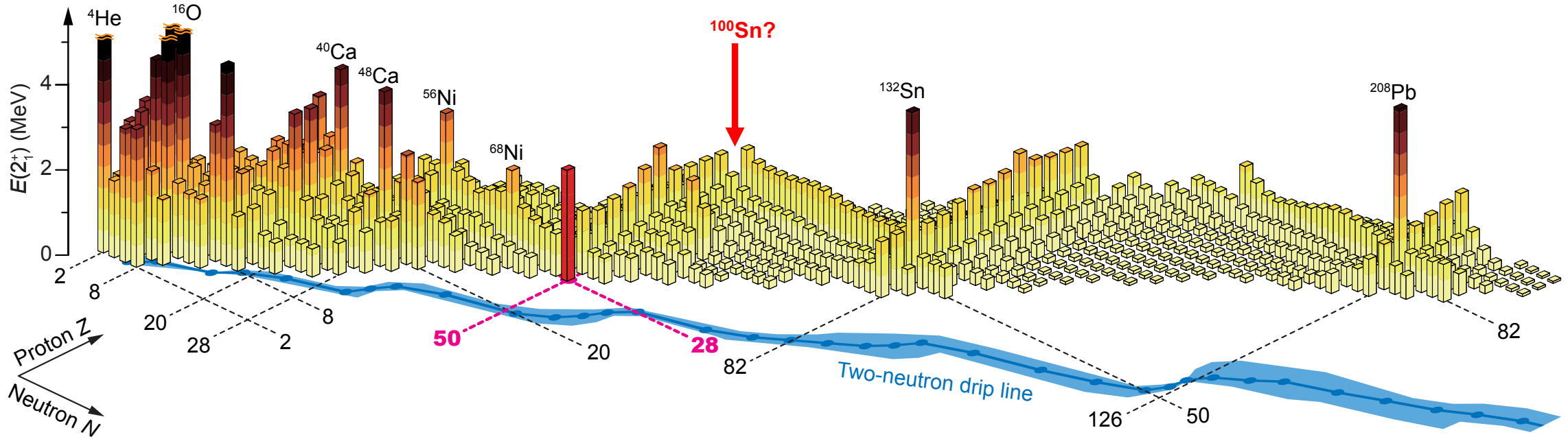


Peak wrt neighboring systems well predicted by IMSRG (also phenomenology)

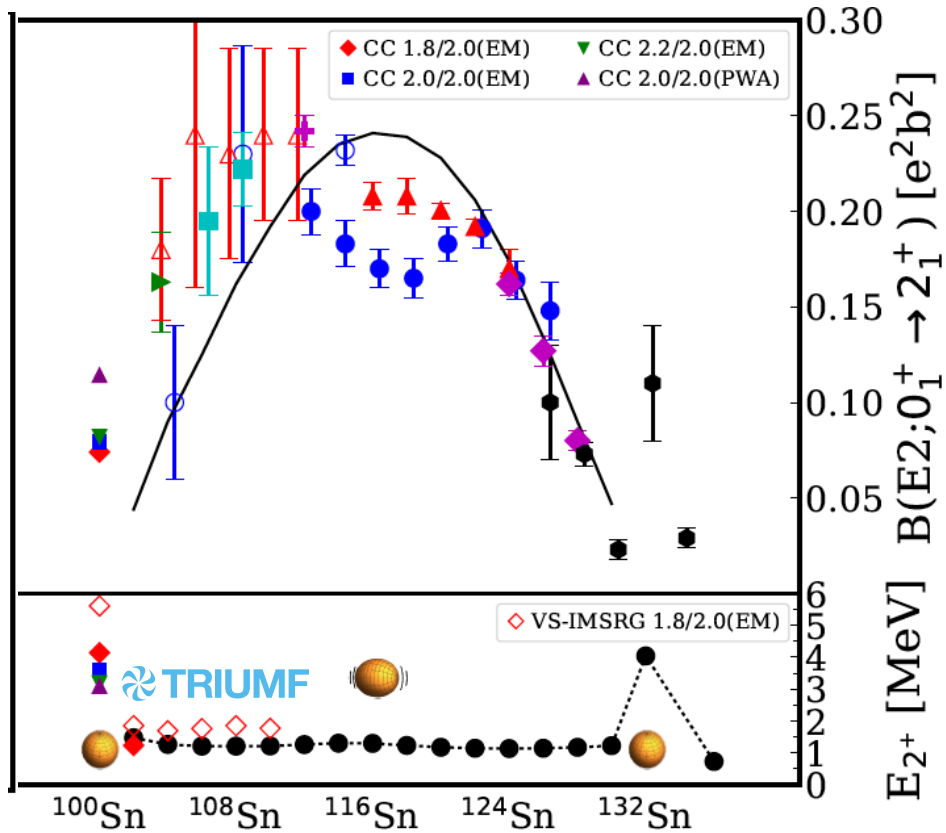
First evidence for the (double) magicity of ^{78}Ni

Next: determine evolution below $Z=28$

Magic numbers: pillars of nuclear structure, novel evolution in exotic nuclei

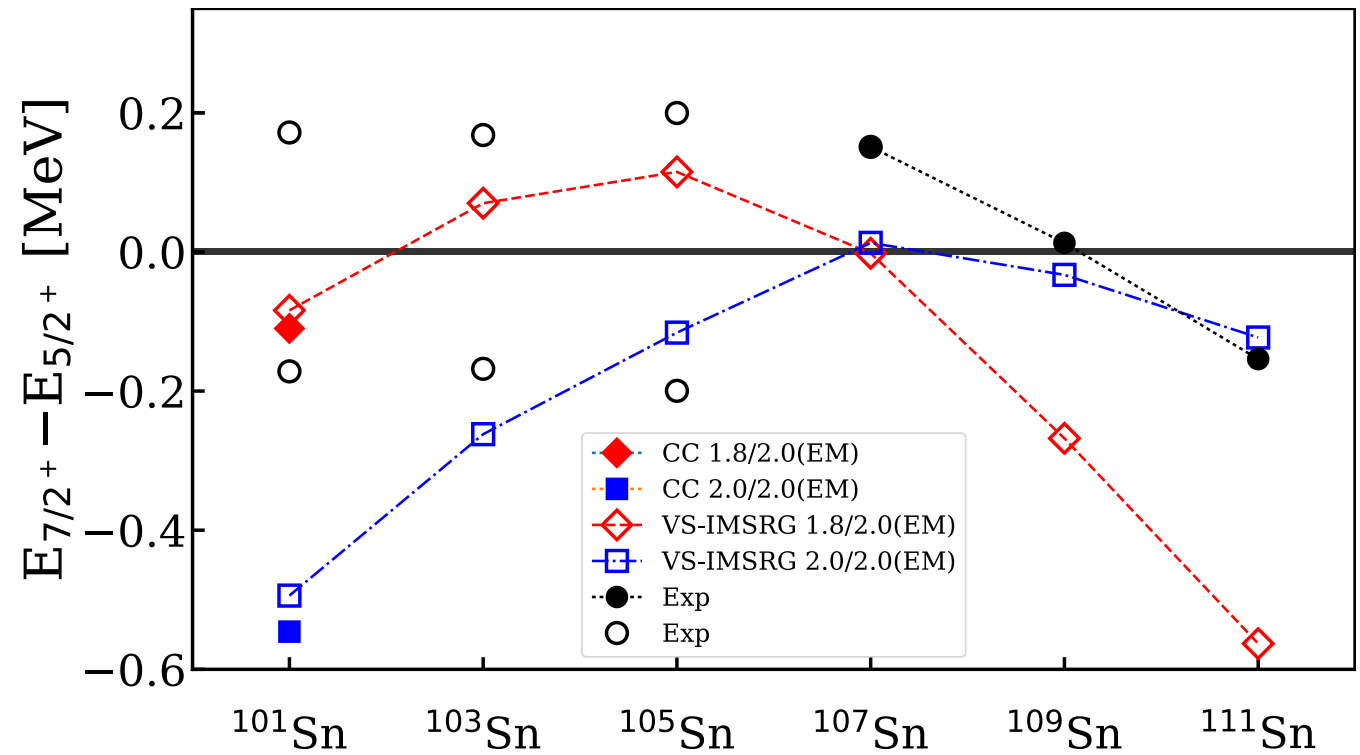


Extend ab initio to heavy-mass region: magicity of ^{100}Sn , controversial level ordering in ^{101}Sn



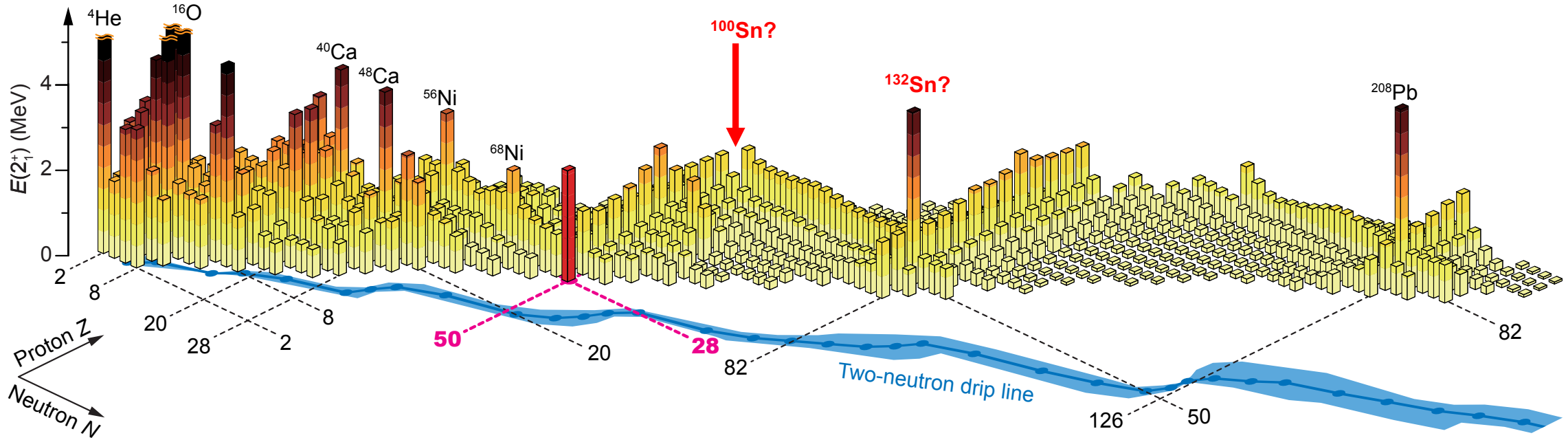
Predicts doubly magic nature from 2^+ energies and $B(E2)$ systematics
Limits of ab initio theory...

Morris et al., PRL (2018)

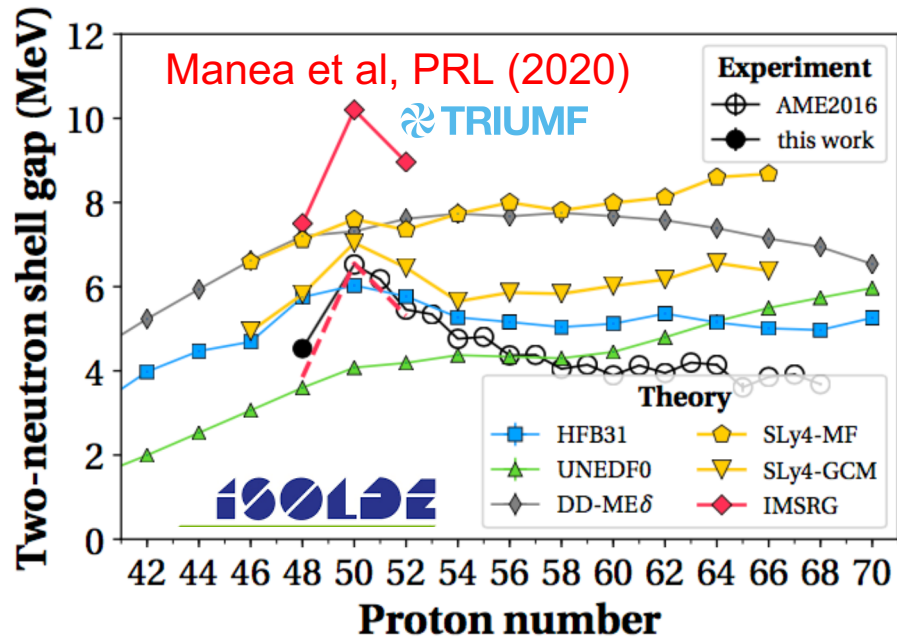
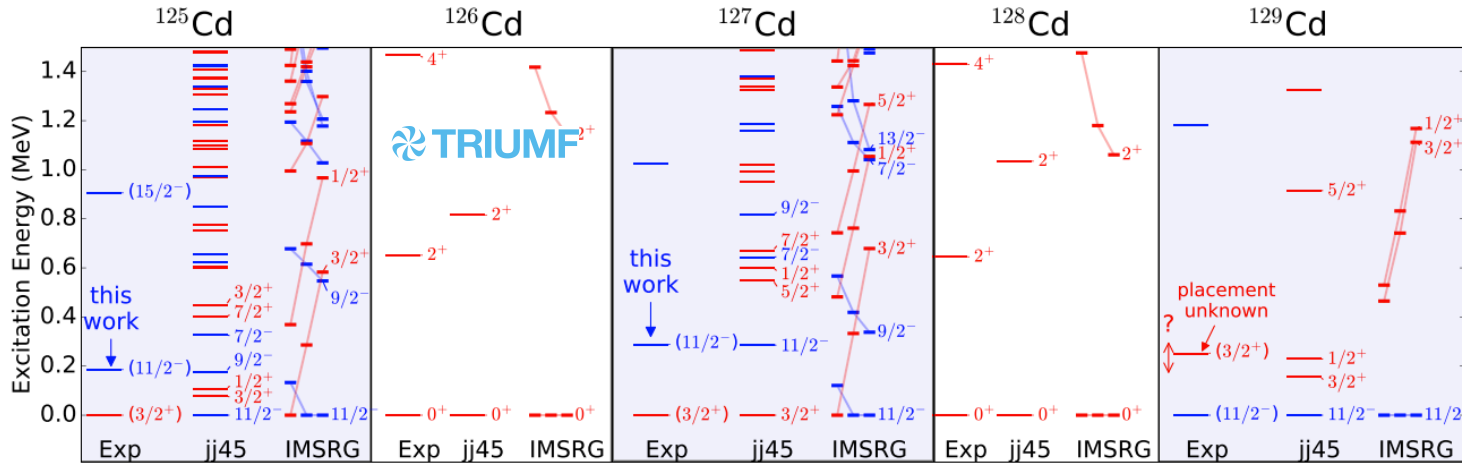


Both calculations predict $5/2^+$ ground state

Magic numbers: pillars of nuclear structure, novel evolution in exotic nuclei



Several studies show N=70 gap clearly not converged wrt $E_{3\max}$ – for neutron-rich Sn, In, Cd...



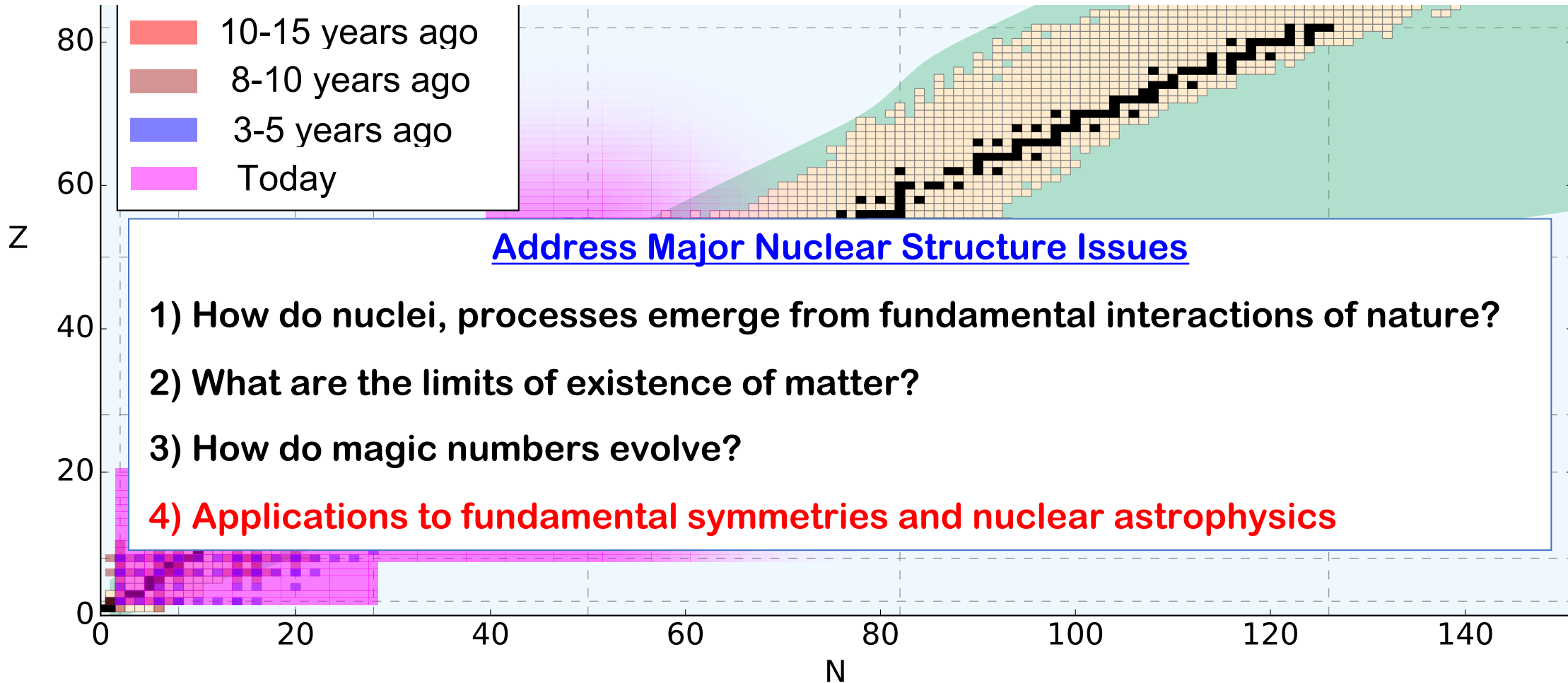
Lascar et al PRC (2017)

Resorted to unreliable extrapolations...

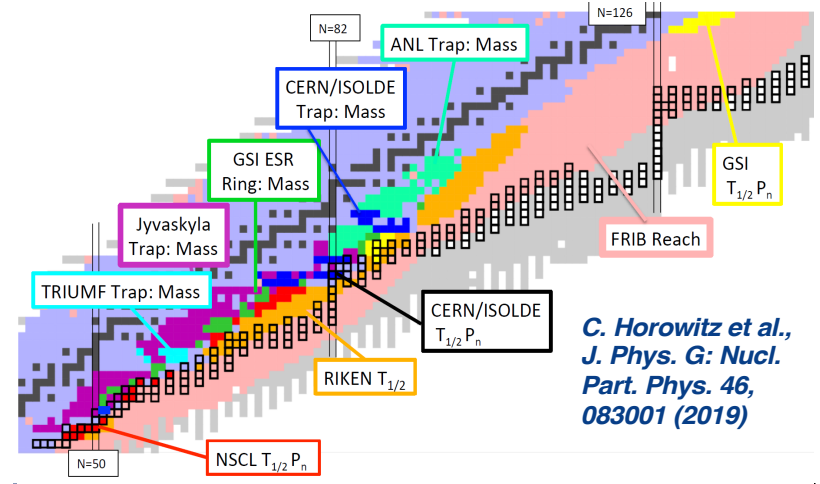
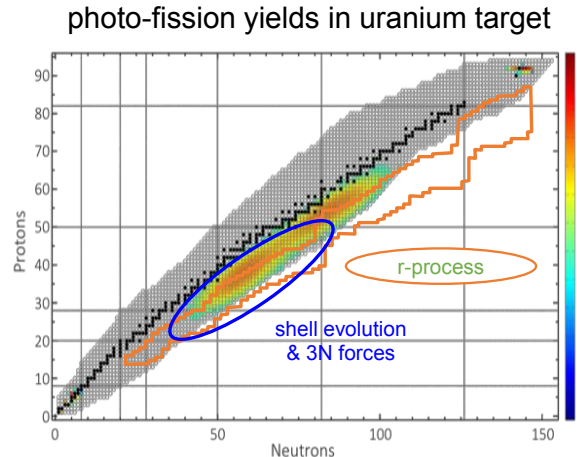
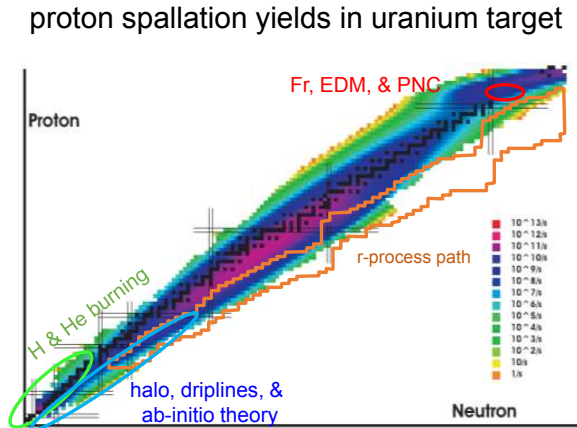
Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

- Nuclear forces, electroweak physics
- Nuclear many-body problem

$$H\psi_n = E_n\psi_n$$

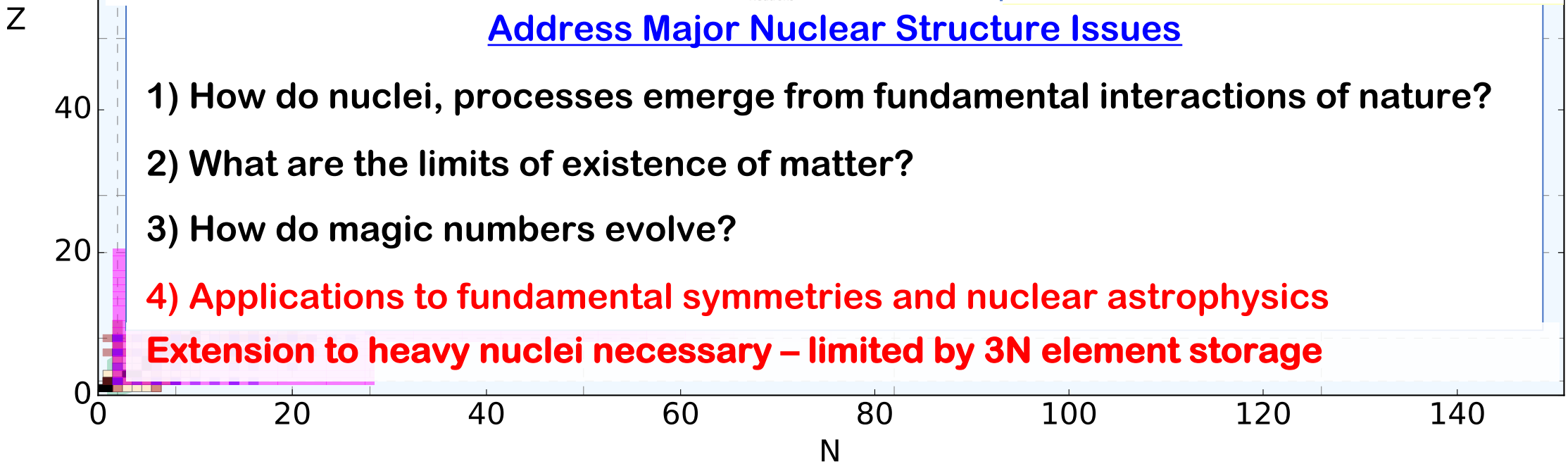


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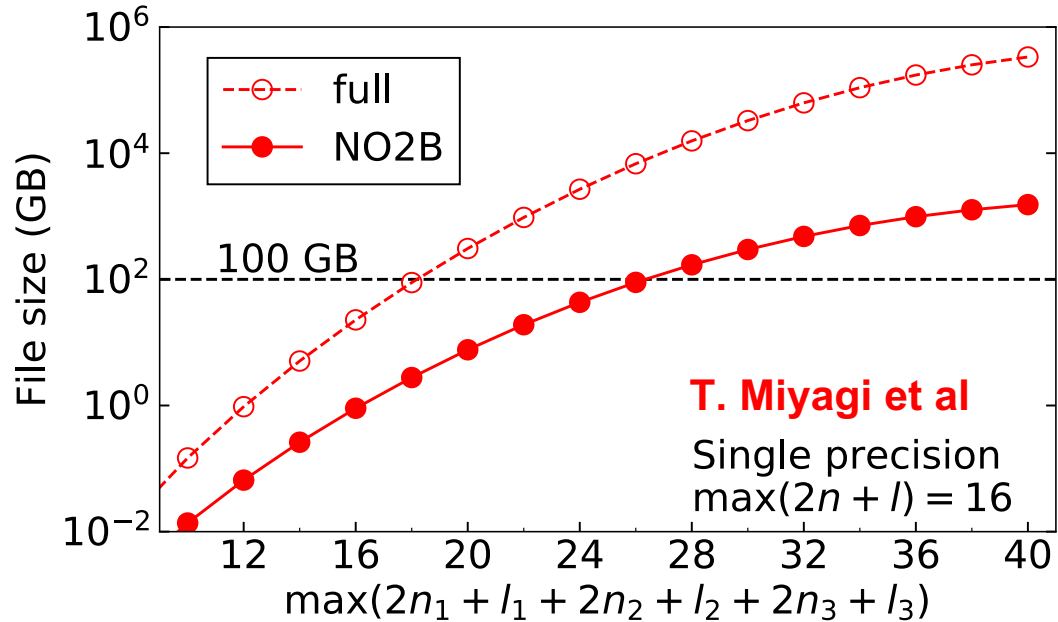


*C. Horowitz et al.,
J. Phys. G: Nucl.
Part. Phys. 46,
083001 (2019)*

Address Major Nuclear Structure Issues



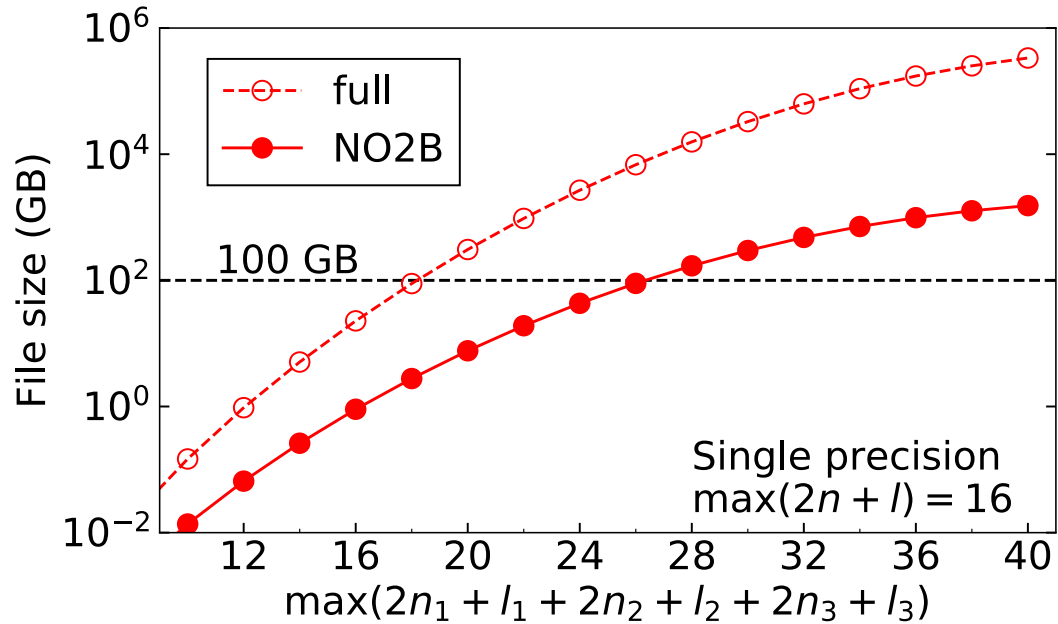
Improvements in storage of 3N matrix elements greatly expands reach of ab initio theory!



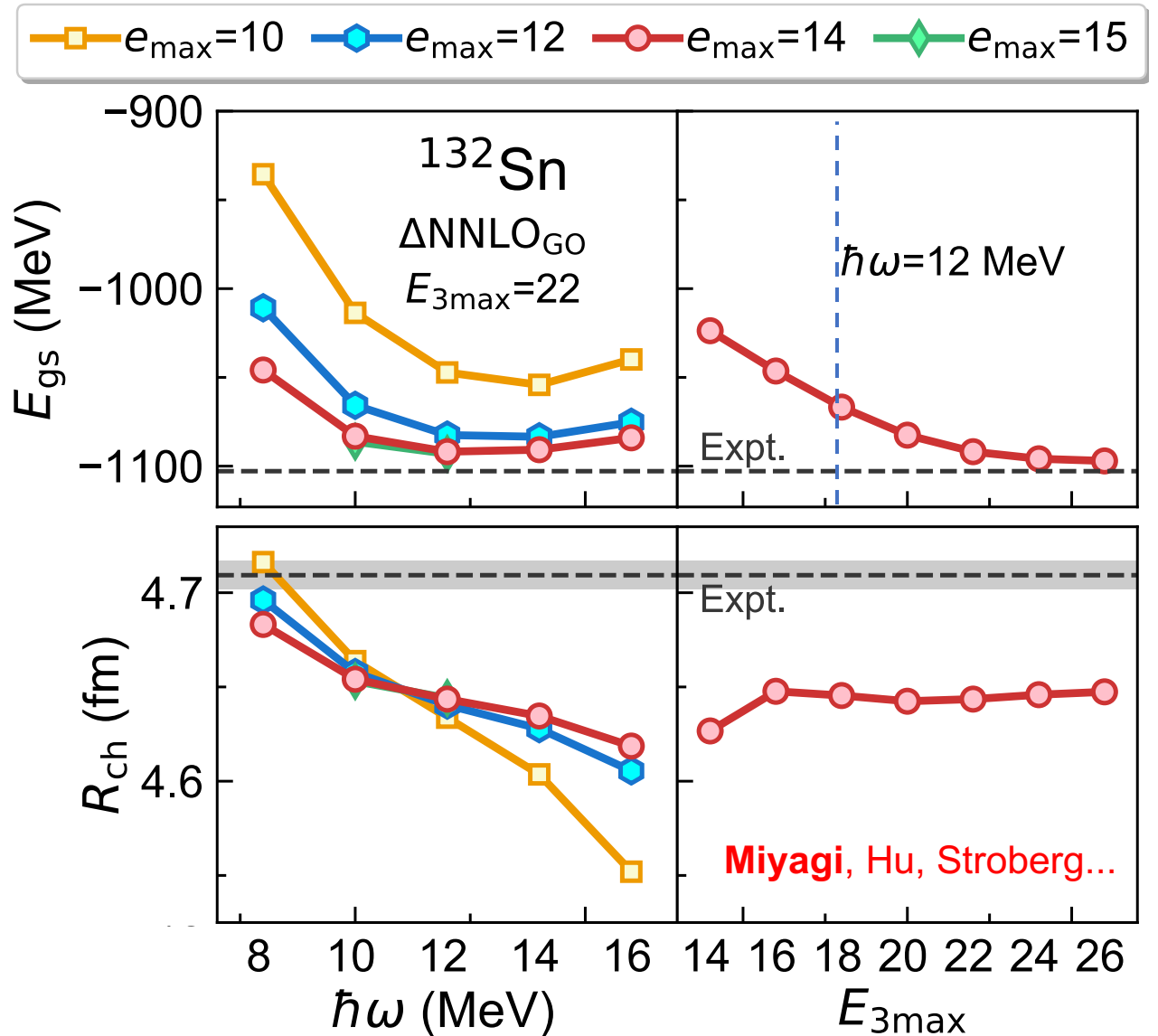
First converged calculations of ^{132}Sn !

Opens new region of chart to ab initio theory

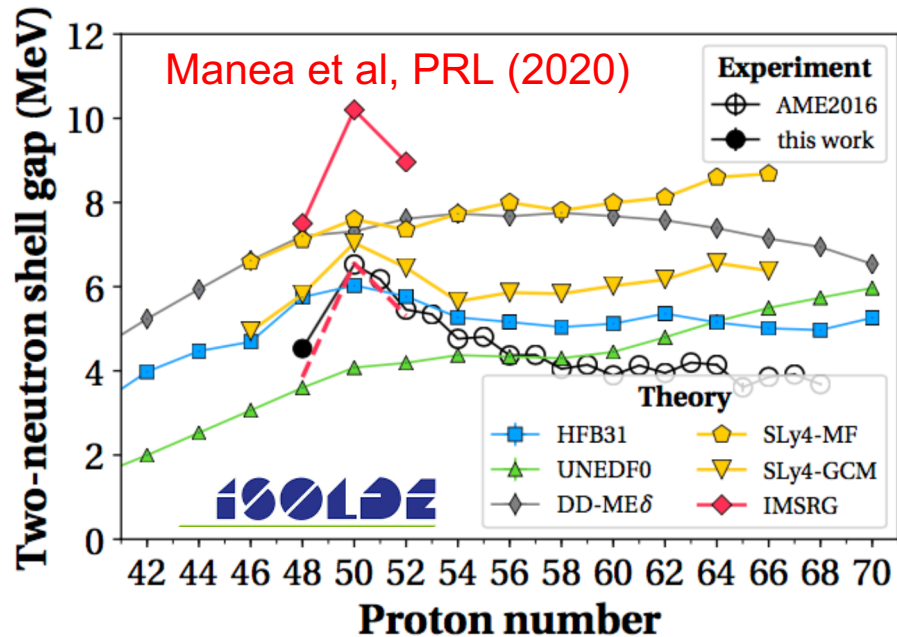
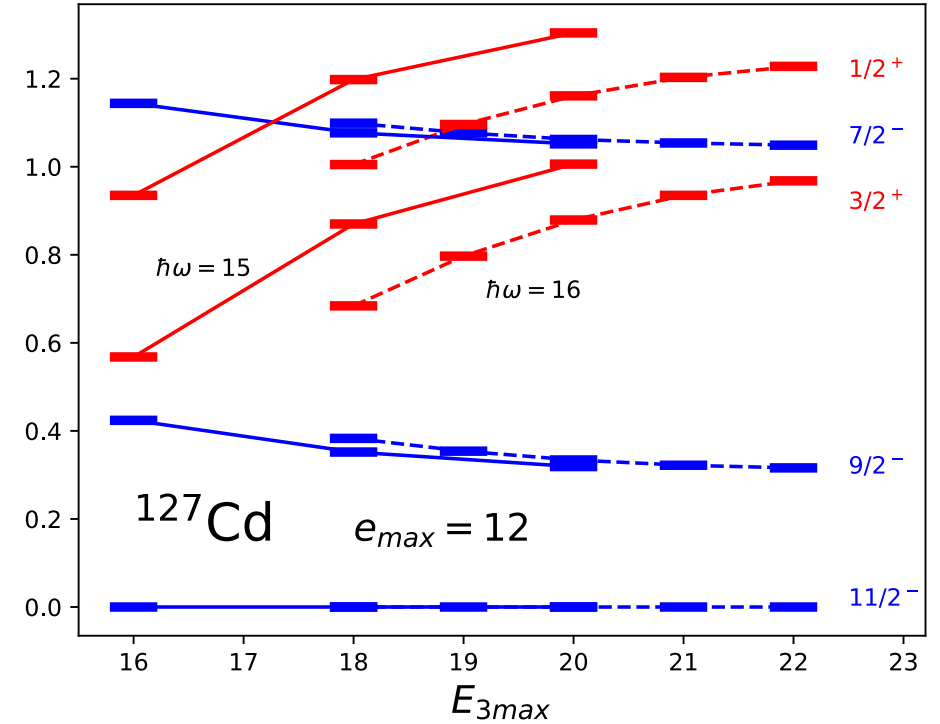
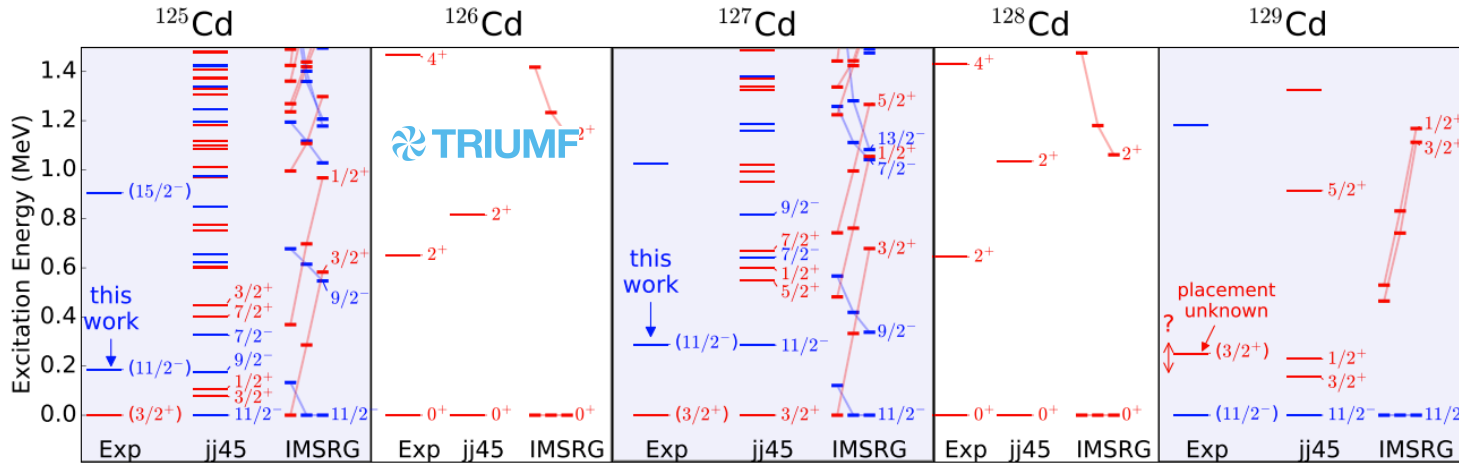
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First converged calculations of ^{132}Sn !
 Opens new region of chart to ab initio theory



Size of N=70 gap clearly not converged wrt E3max – for neutron-rich Sn, In, Cd...



Lascar et al PRC (2017)

Resorted to unreliable extrapolations...

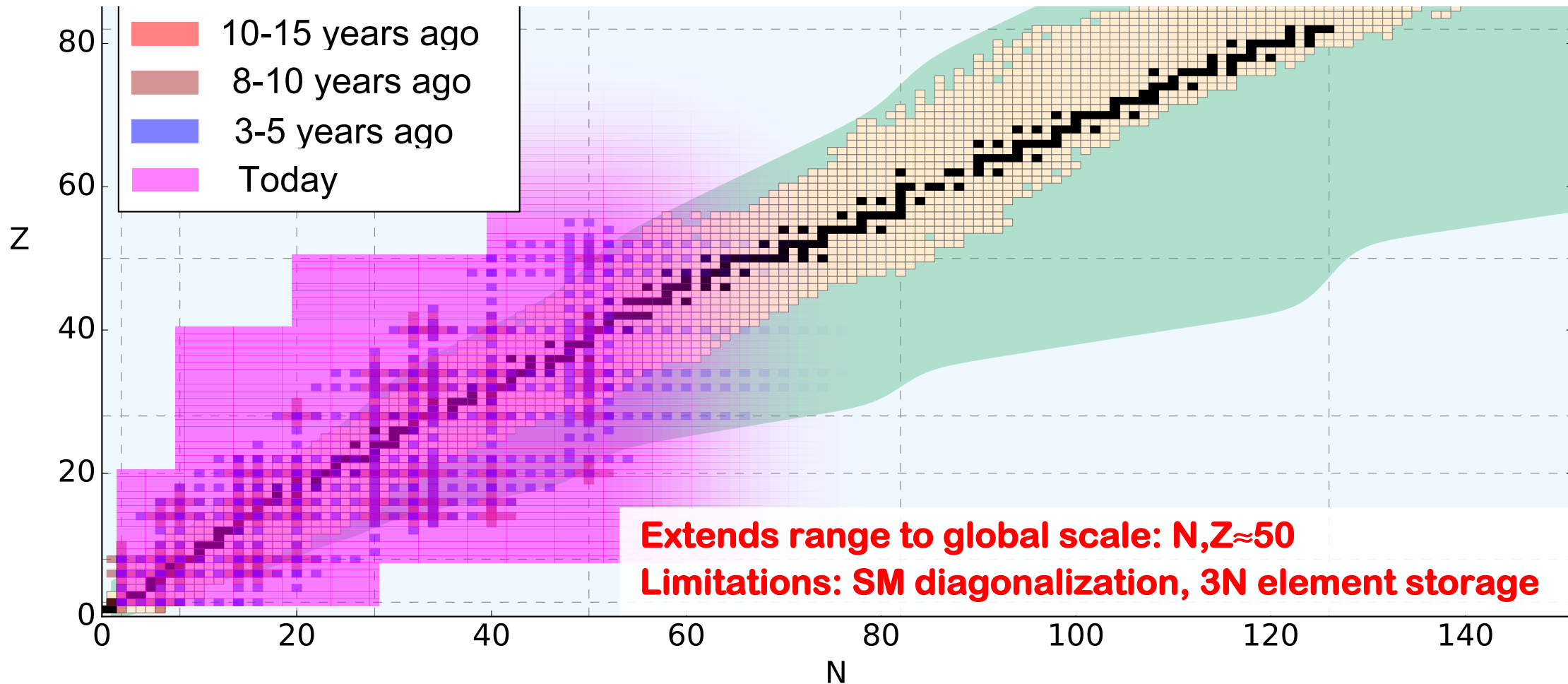
New capabilities: converged spectra in N=82 region!

Explore new physics near ^{132}Sn !

Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

- Nuclear forces, electroweak physics
- Nuclear many-body problem

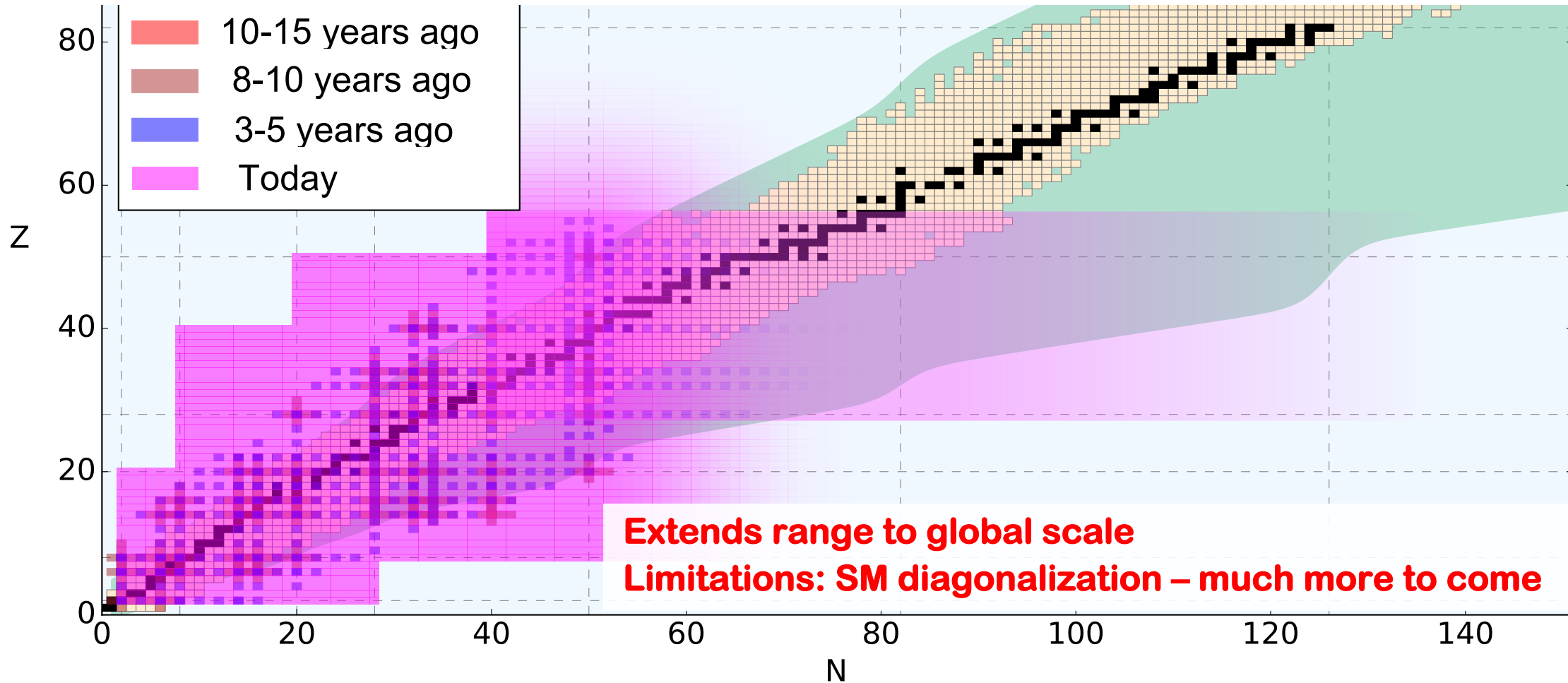
$$H\psi_n = E_n\psi_n$$



Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

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- Nuclear many-body problem

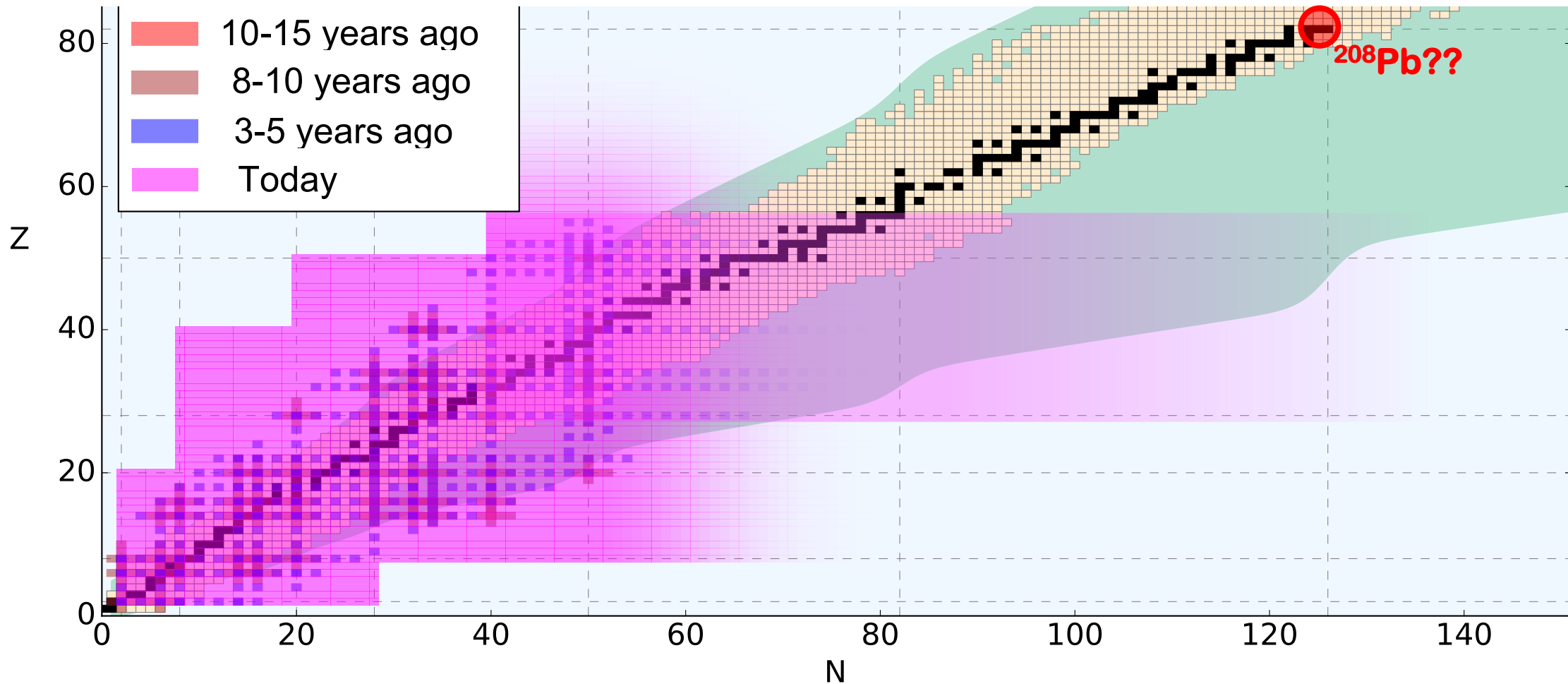
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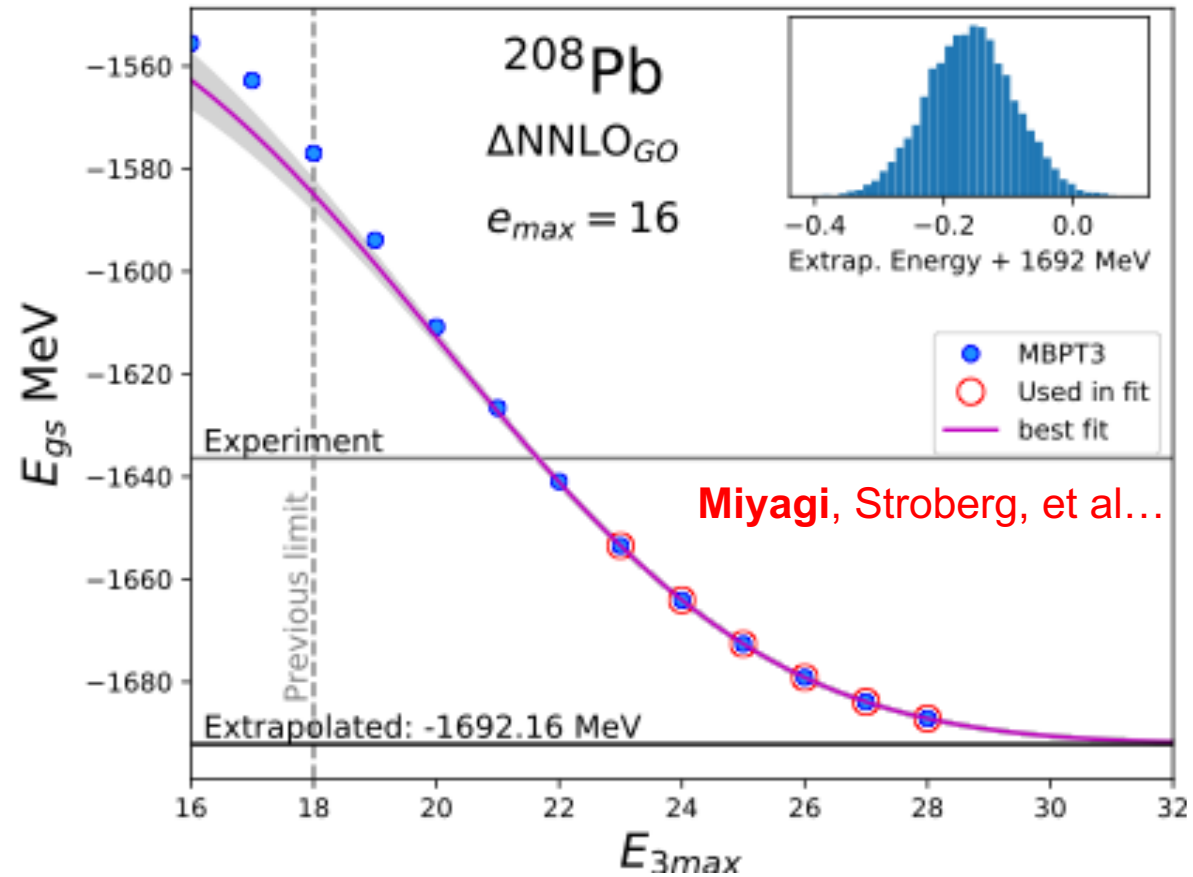
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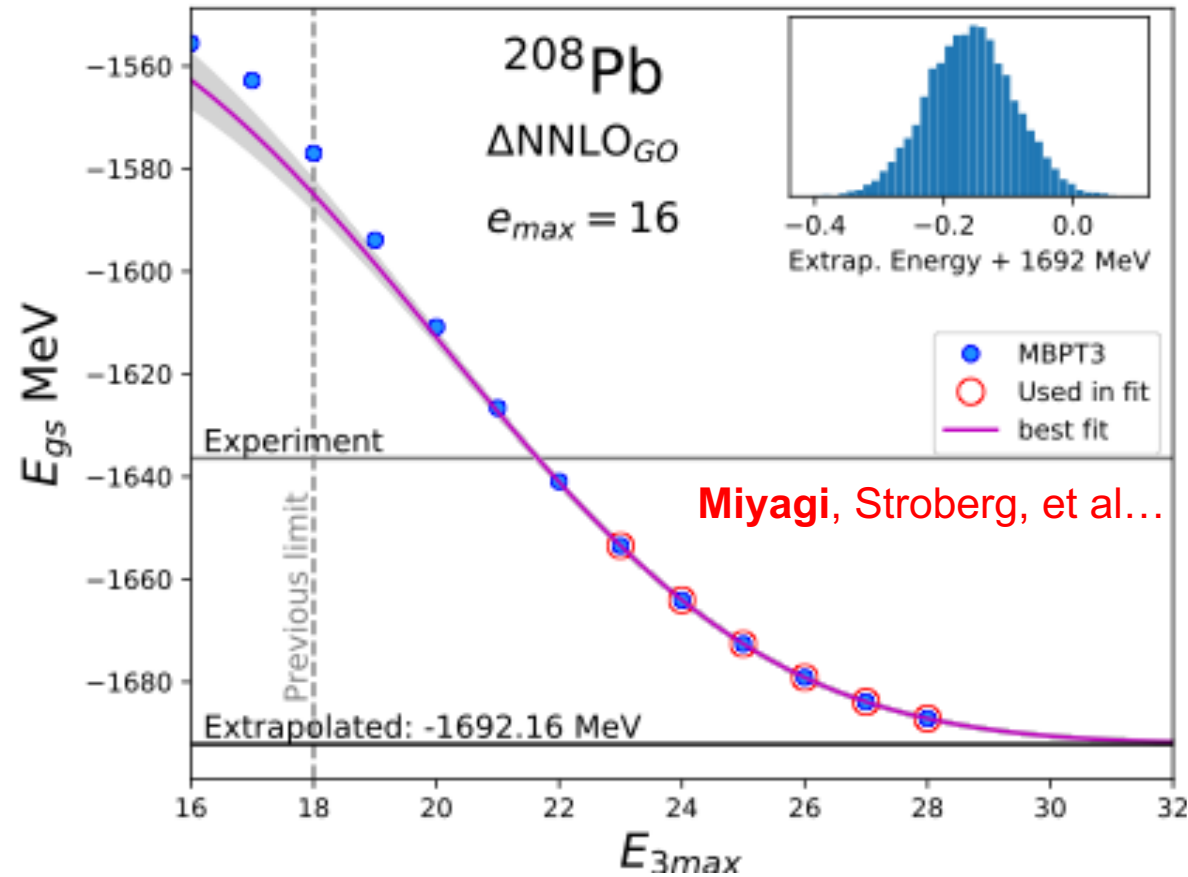
Improvements in storage of 3N matrix elements greatly expands reach of ab initio theory!

Increased $E_{3\text{max}}$ range allows first reliable convergence of ^{208}Pb

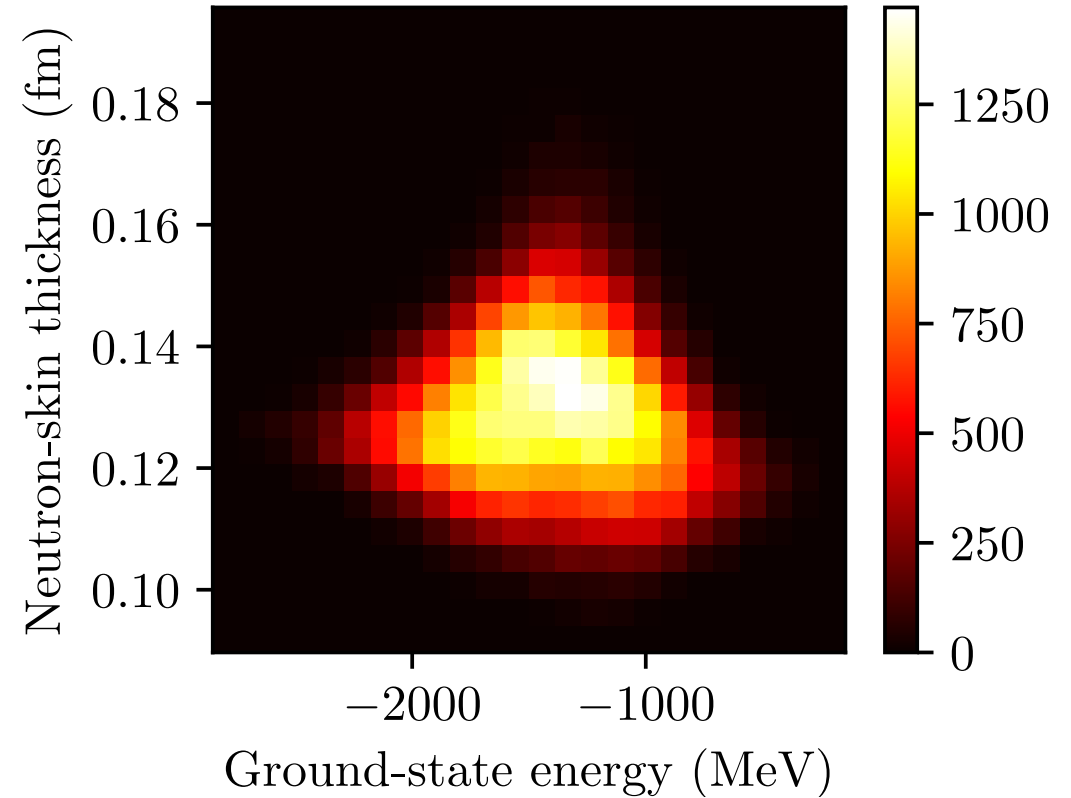


Improvements in storage of 3N matrix elements greatly expands reach of ab initio theory!

Increased $E_{3\text{max}}$ range allows first reliable convergence of ^{208}Pb



Miyagi, Stroberg, et al...



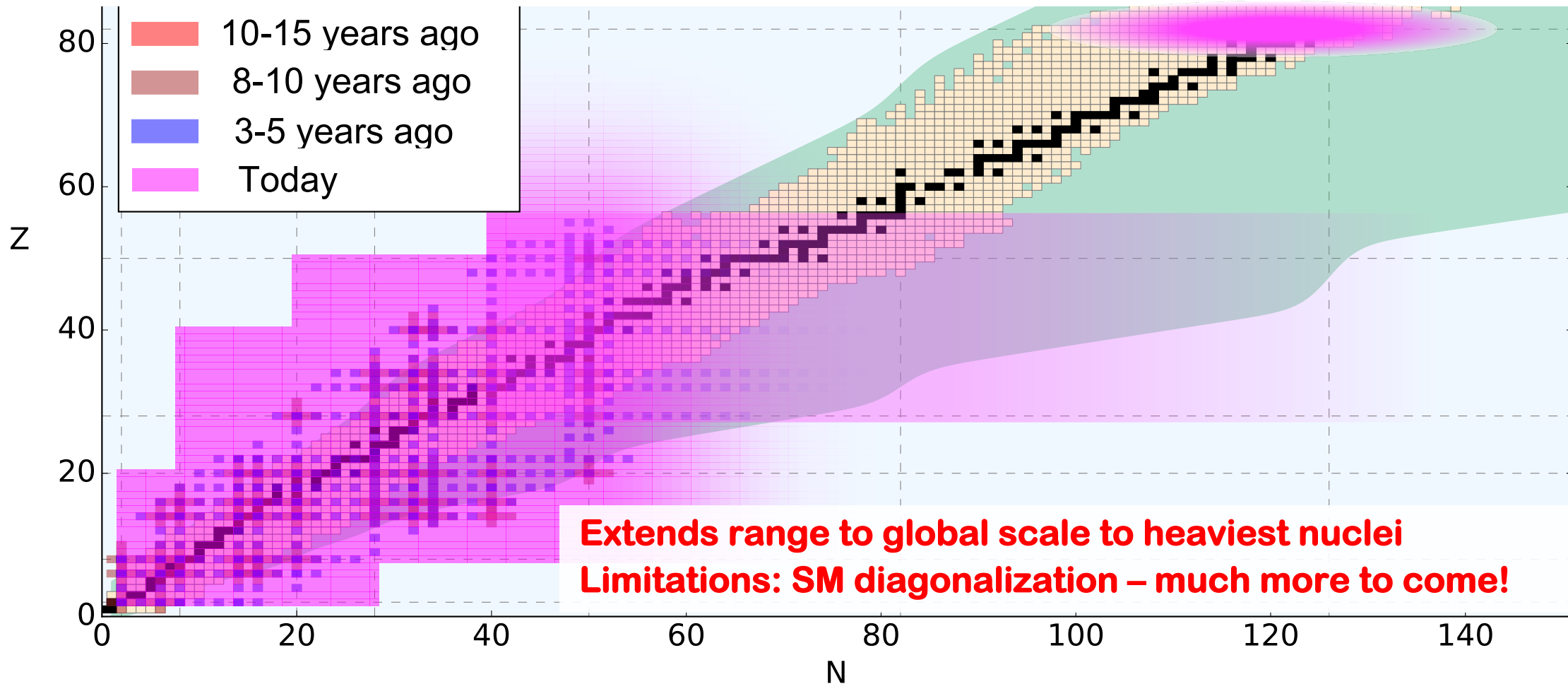
Machine learning algorithms sample “all” chiral interactions: 100 000 ^{208}Pb calculations - billions in progress

Heat map of neutron skin/ground state energy - constraints on equation of state and neutron stars!

Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

- Nuclear forces, electroweak physics
- Nuclear many-body problem

$$H\psi_n = E_n\psi_n$$



Aim of modern nuclear theory: Develop unified *first-principles* picture of structure and reactions

Nuclear Structure

- Development of forces and currents¹
- Dripline predictions for medium-mass
- Evolution of magic numbers from masses, radii, spectroscopy, EM transitions: ⁷⁸Ni
- Multi-shell theory:
 - Island of inversion²
 - Forbidden decays³

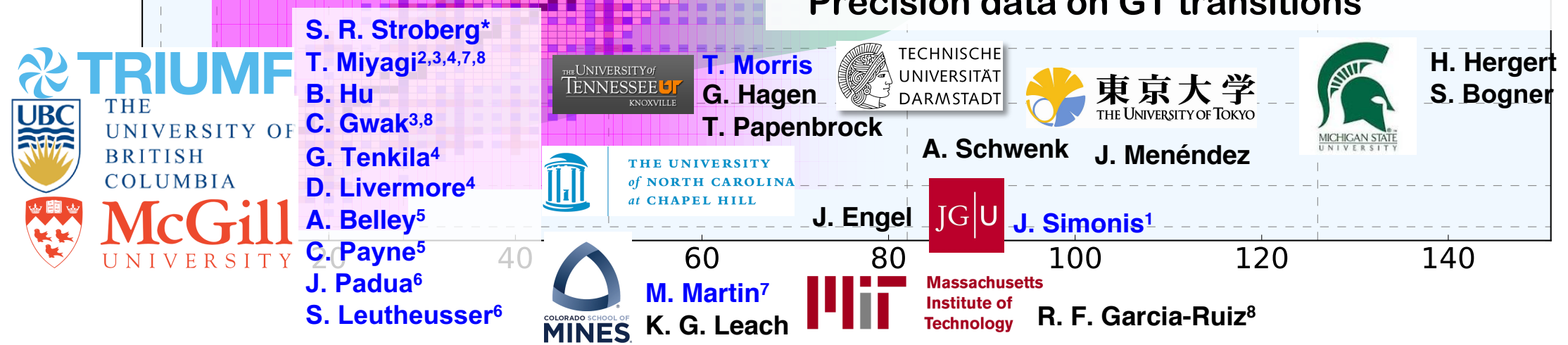
Atomic systems⁴

Fundamental Symmetries/BSM Physics

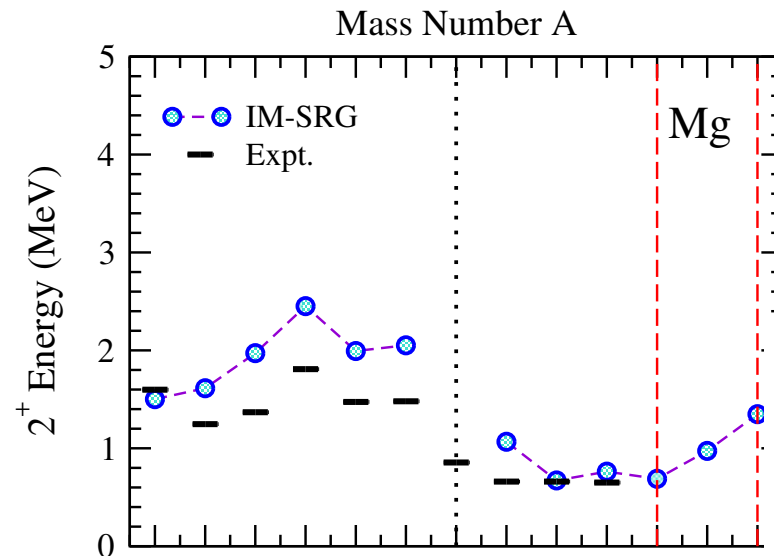
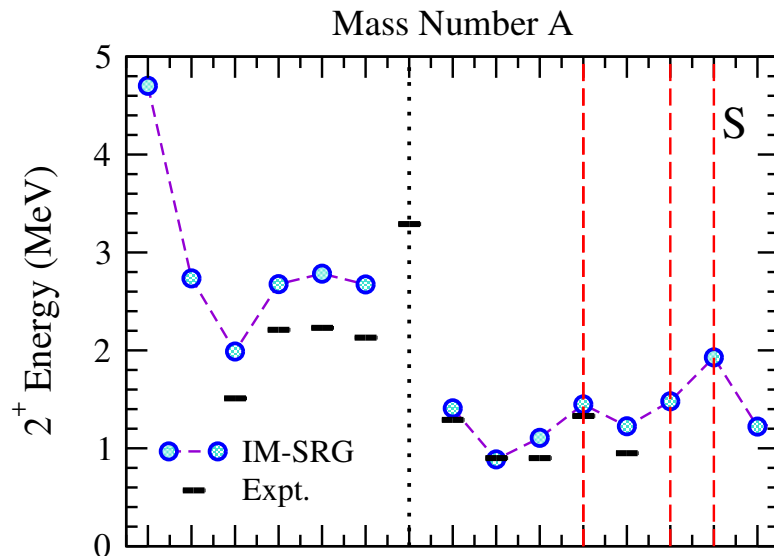
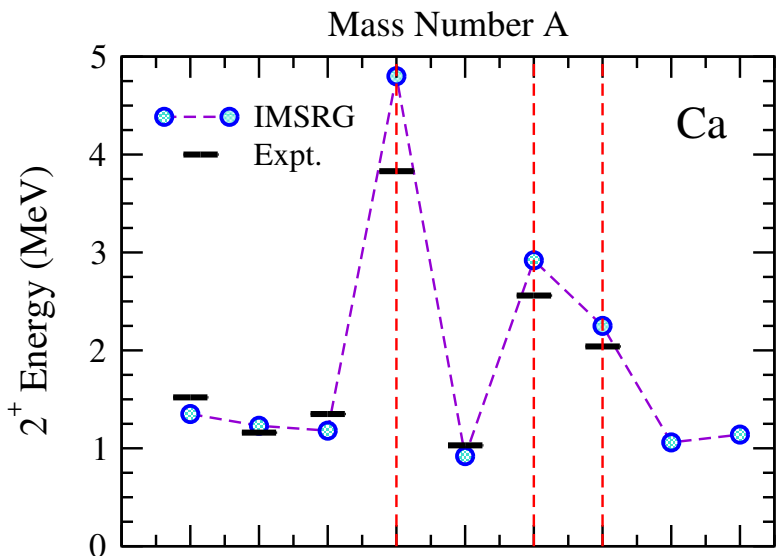
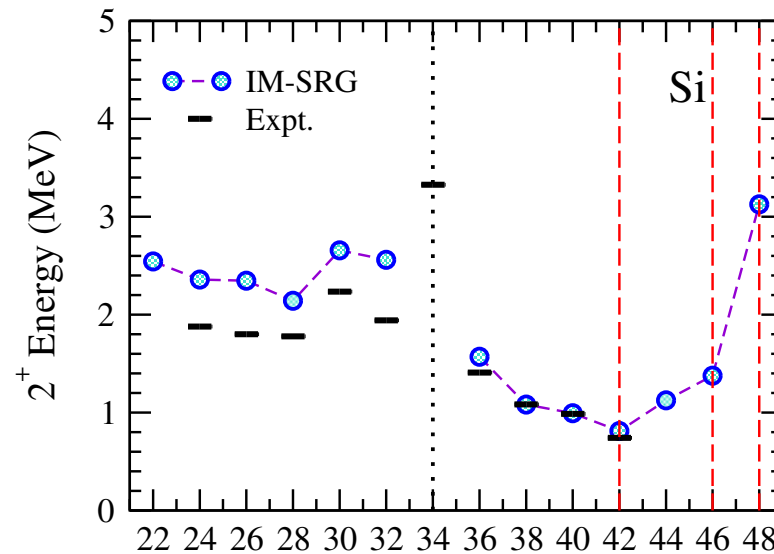
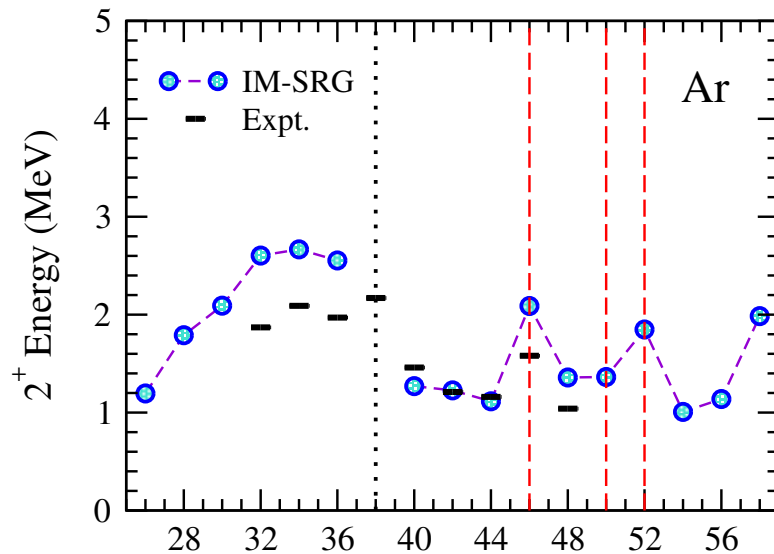
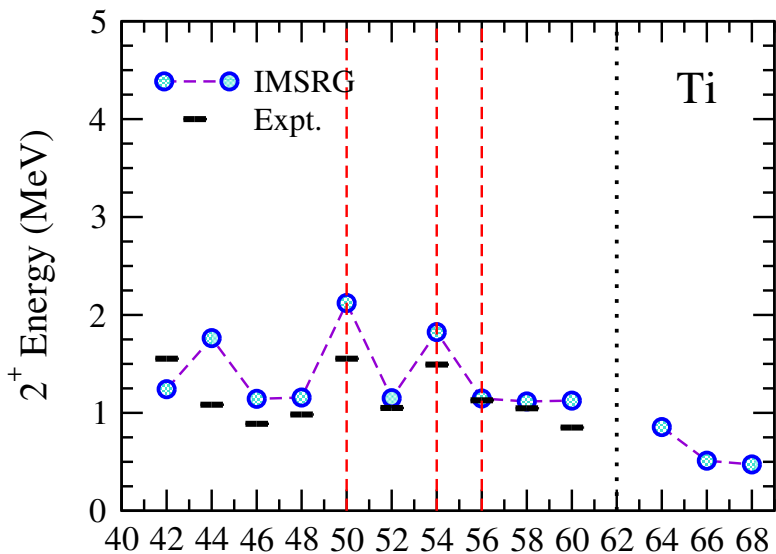
- Effective electroweak operators: GT quenching
- Effective $0\nu\beta\beta$ decay operator⁵
- WIMP-Nucleus scattering⁶
- Superallowed Fermi transitions⁷
- Symmetry-violating moments [molecules]⁸

Experimental overlap

- Best data for constraining nuclear forces
- New measurements of driplines
- Data on magic numbers in exotic nuclei
- Precision data on GT transitions



Ab initio predictions from above calcium towards oxygen – **persistence of N=34**



Mass Number A

Mass Number A

Mass Number A

Calculate **large GT matrix elements**

$$M_{GT} = g_A \langle f | \mathcal{O}_{GT} | i \rangle$$

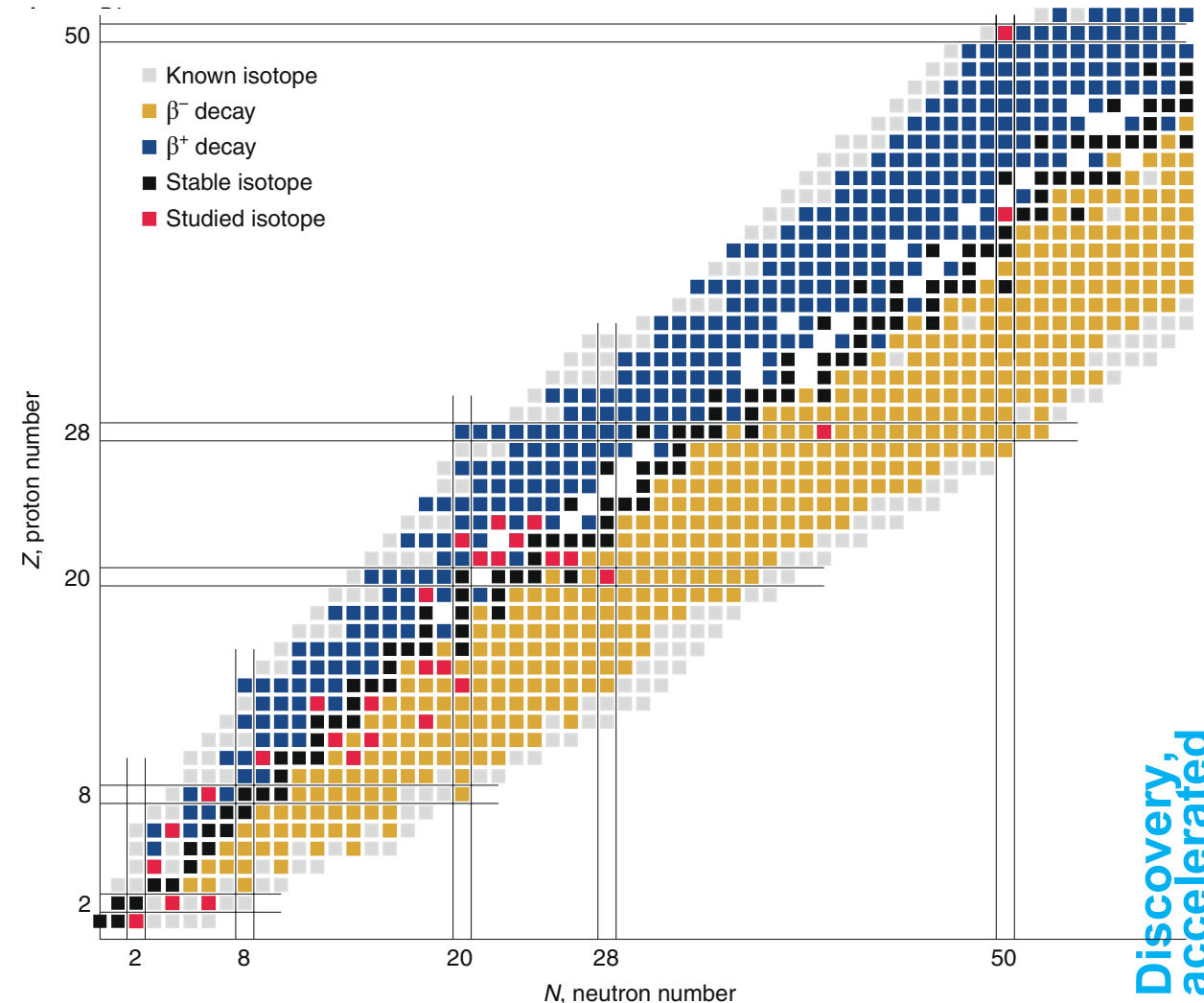
$$\mathcal{O}_{GT} = \mathcal{O}_{\sigma\tau}^{1b} + \mathcal{O}_{2BC}^{2b}$$

- Light, medium, and heavy regions
- Benchmark different ab initio methods
- Wide range of NN+3N forces
- Consistent inclusion of 2BC

NUCLEAR PHYSICS

Beta decay gets the ab initio treatment

One of the fundamental radioactive decay modes of nuclei is β decay. Now, nuclear theorists have used first-principles simulations to explain nuclear β decay properties across a range of light- to medium-mass isotopes, up to ^{100}Sn .



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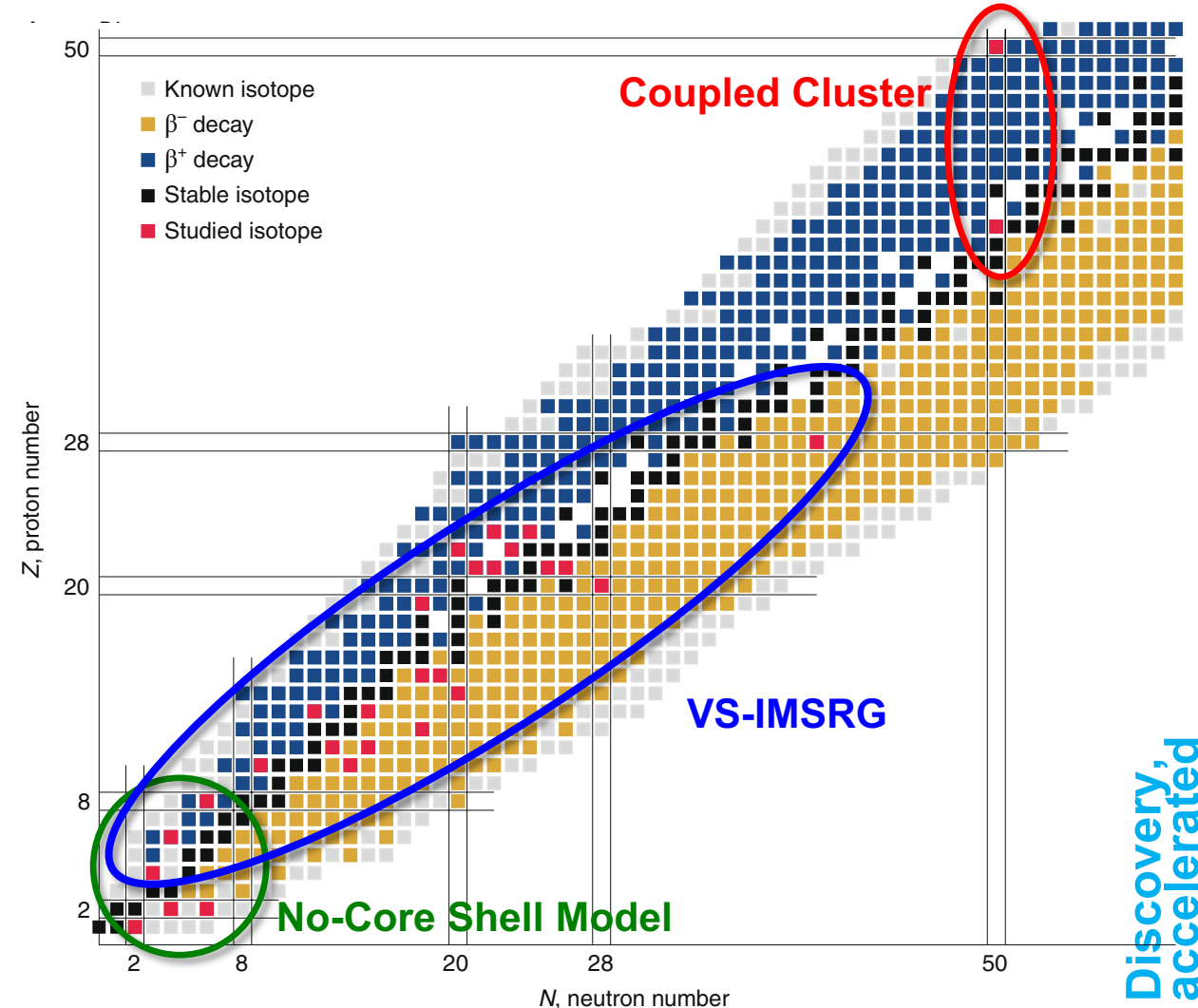
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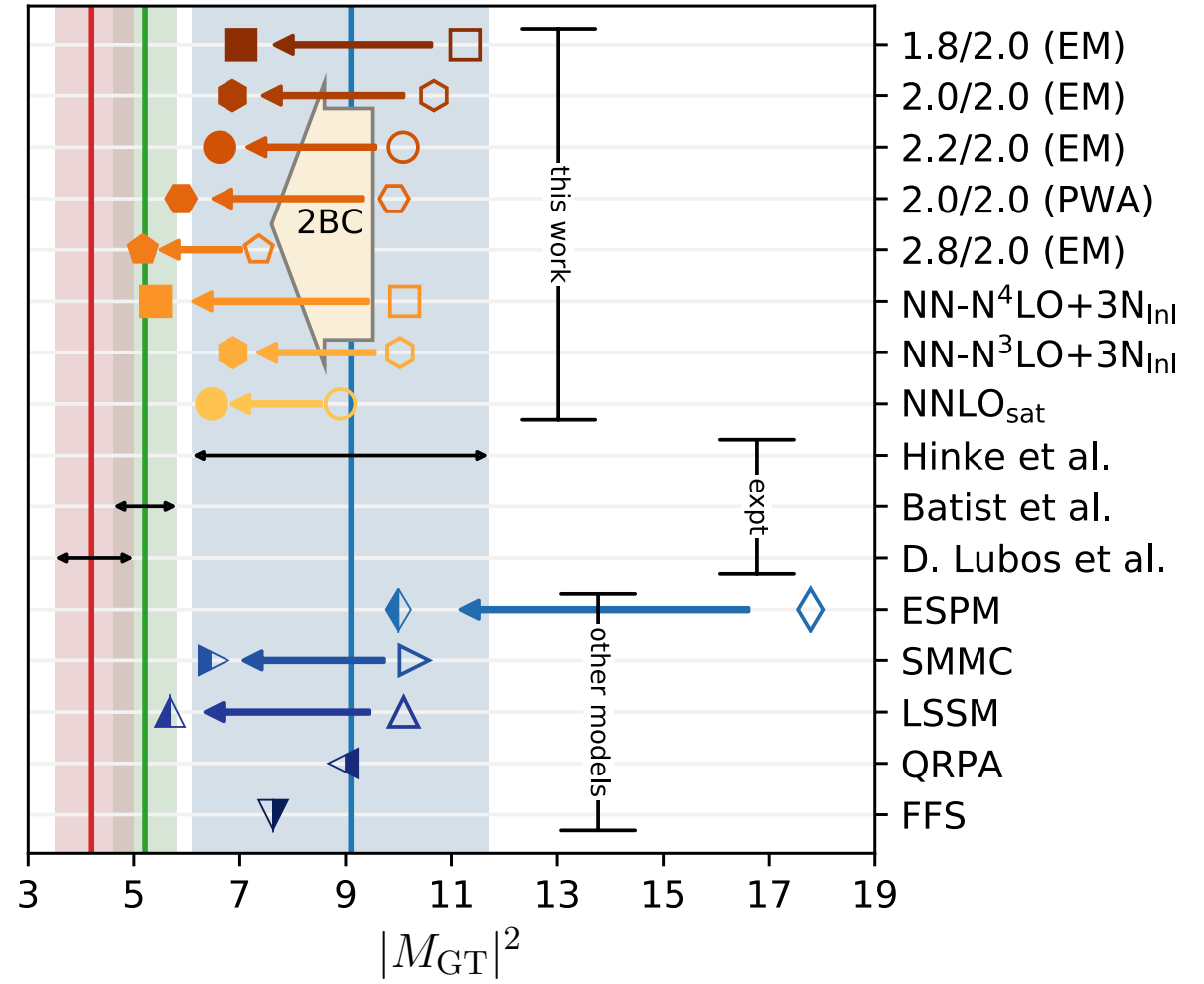
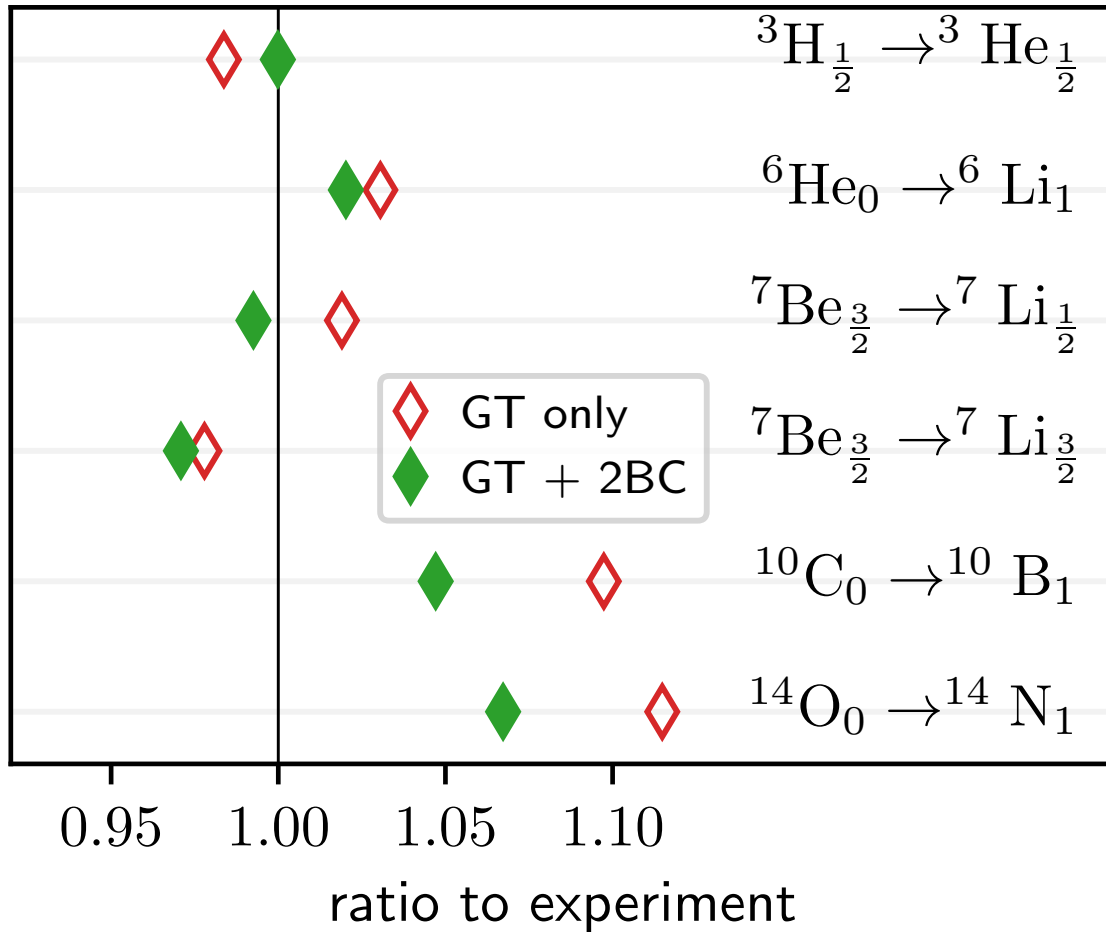
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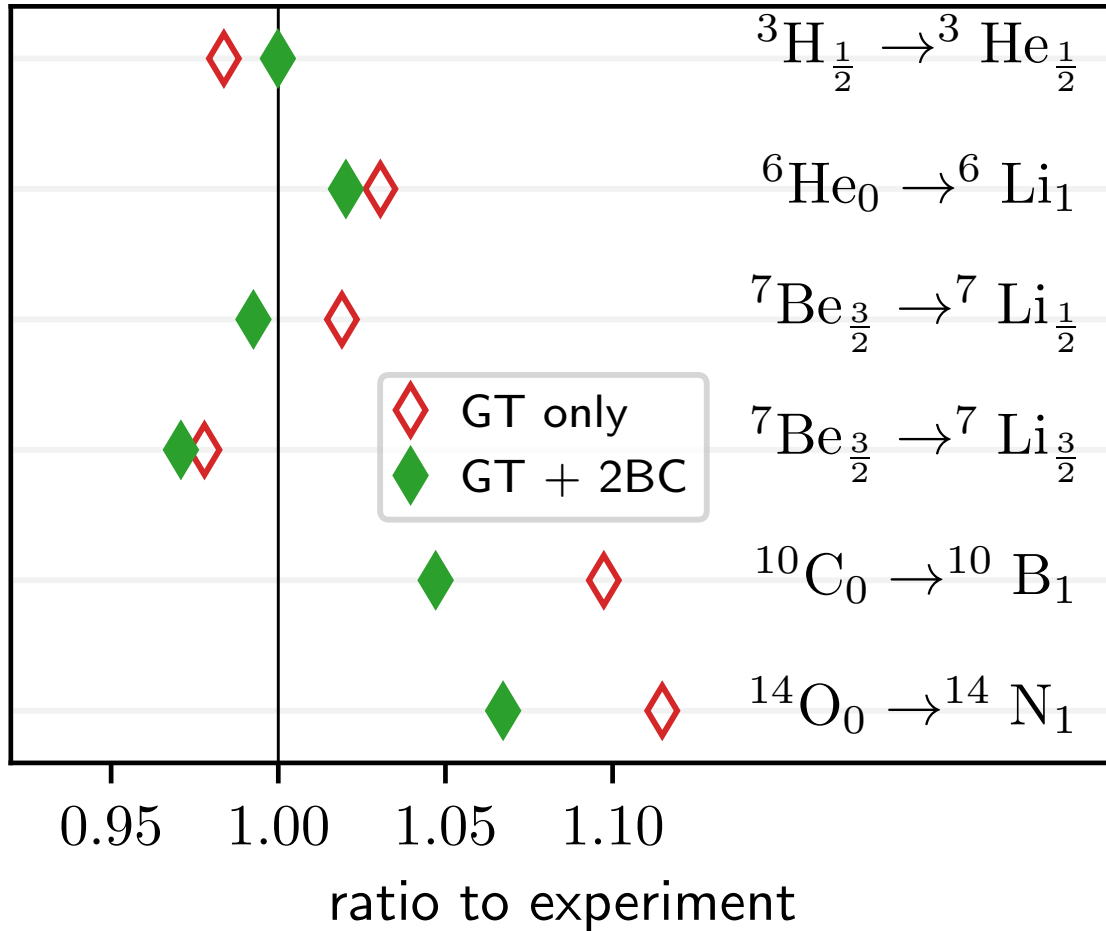
NCSM in light nuclei, CC calculations of GT transition in ^{100}Sn from different forces



Large quenching effect from correlations

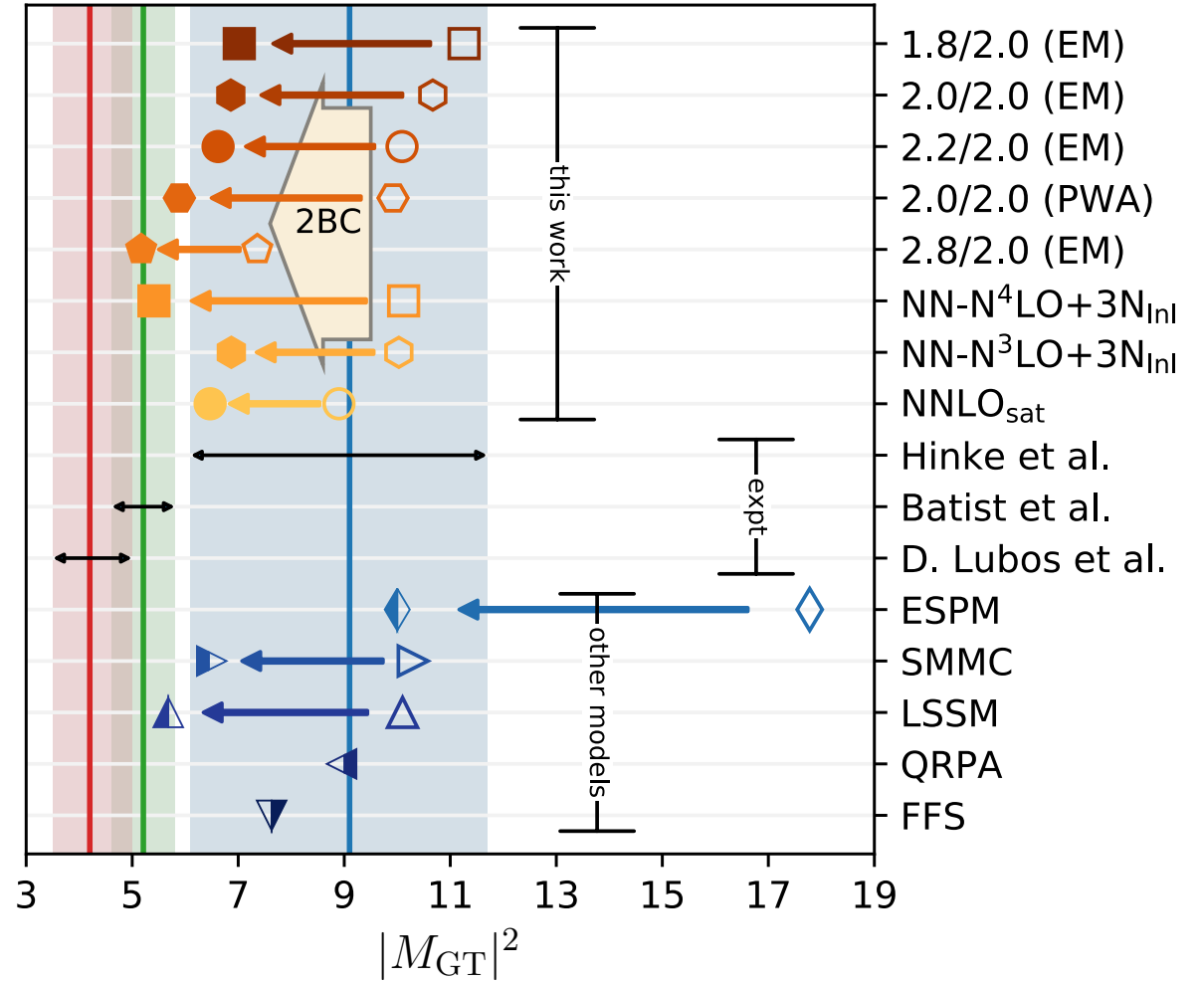
Gysbers et al., Nature Phys. (2019)

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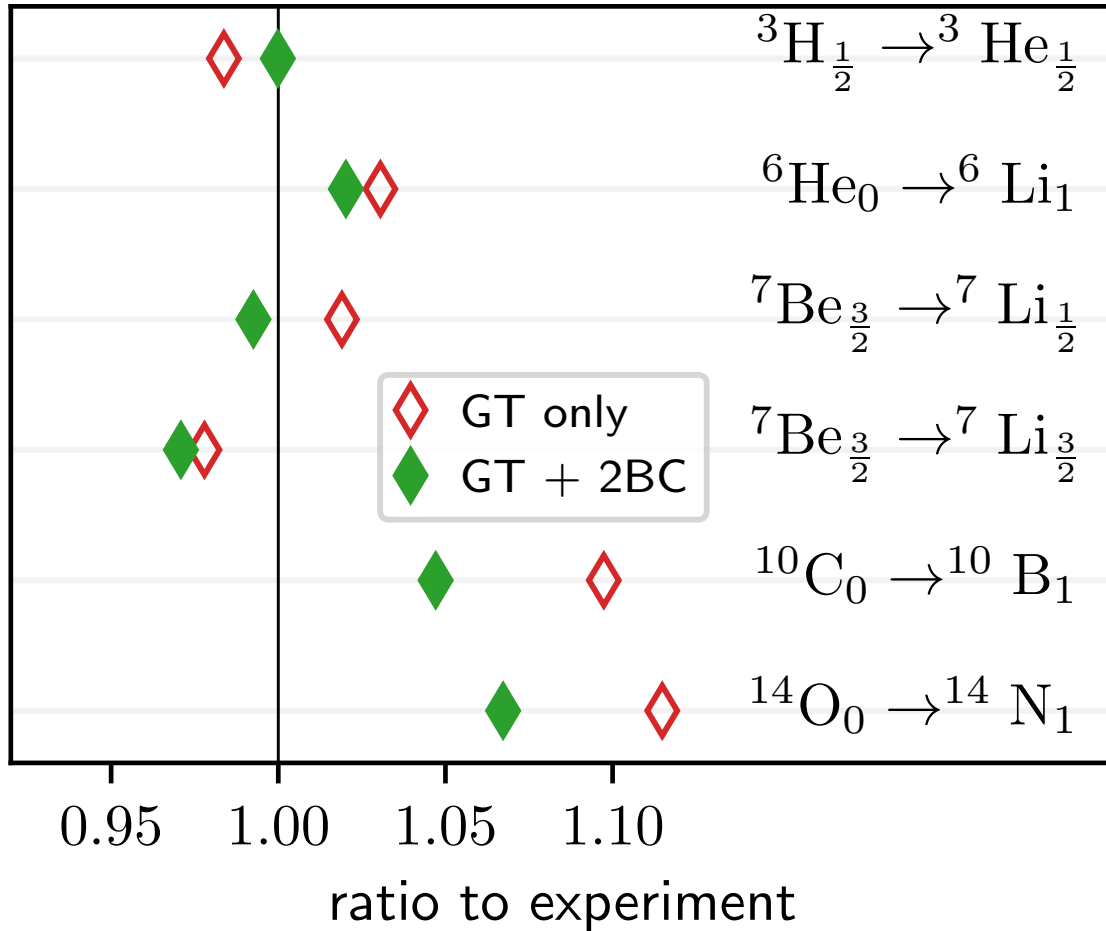
Large quenching effect from correlations

Addition of 2BC further quenches and reduces spread in results



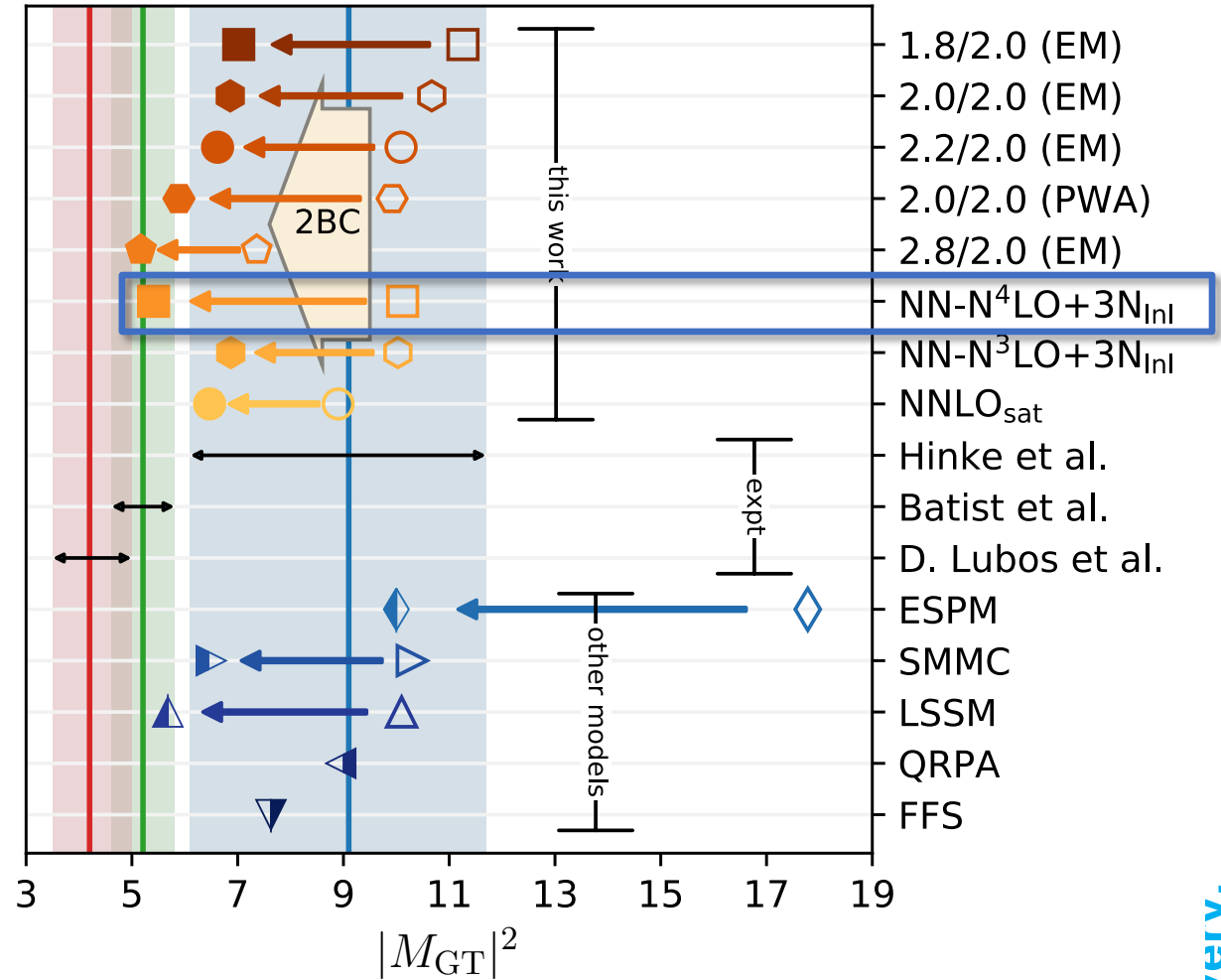
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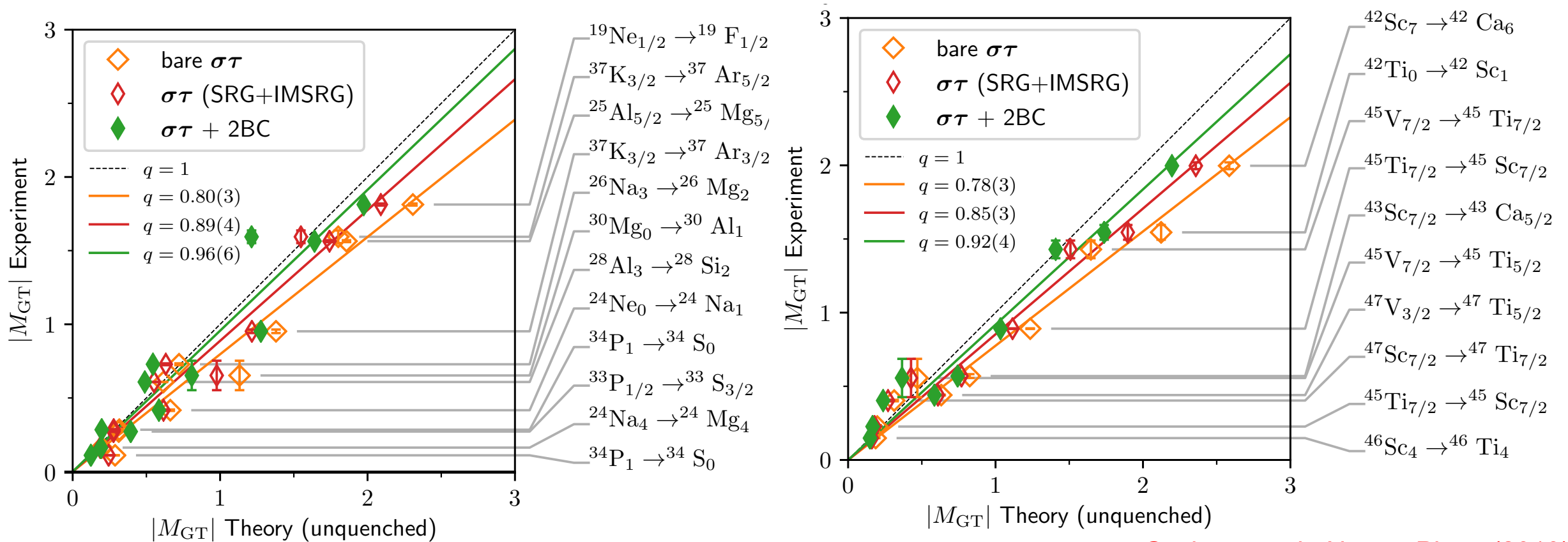


Gysbers et al., Nature Phys. (2019)

Ab initio calculations of **large** GT transitions in *sd*, *pf* shells

Bare operator similar to phenomenological shell model

Modest quenching from consistent ab initio wavefunctions and operators



Further modest quenching from 2BC

Gysbers et al., Nature Phys. (2019)

Explicitly construct unitary transformation from sequence of rotations

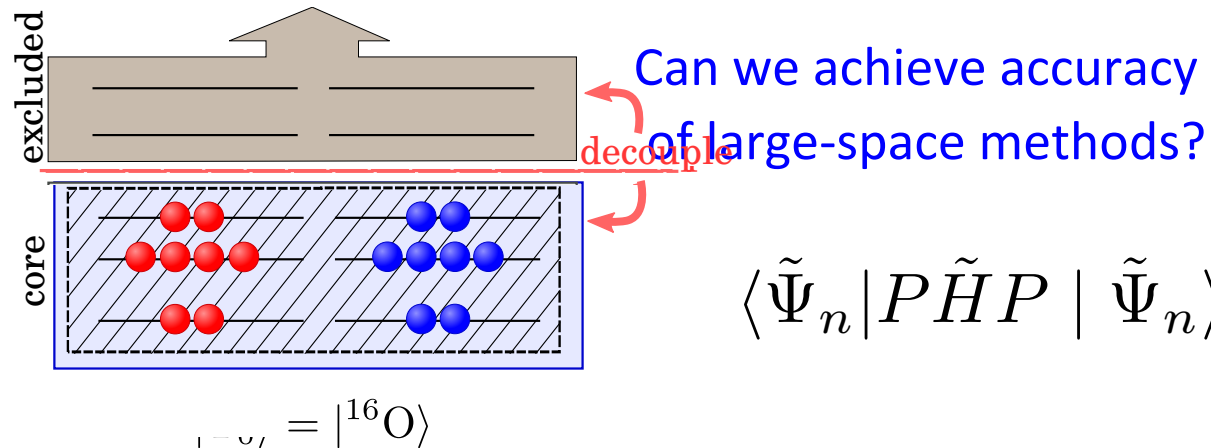
$$U = e^{\Omega} = e^{\eta_n} \dots e^{\eta_1} \quad \eta = \frac{1}{2} \arctan \left(\frac{2H_{\text{od}}}{\Delta} \right) - \text{h.c.}$$

$$\tilde{H} = e^{\Omega} H e^{-\Omega} = H + [\Omega, H] + \frac{1}{2} [\Omega, [\Omega, H]] + \dots$$

All operators truncated at two-body level IMSRG(2)
IMSRG(3) in progress

Tsukiyama, Bogner, Schwenk, PRC 2012
 Morris, Parzuchowski, Bogner, PRC 2015

Step 1: Decouple core



$$\langle \tilde{\Psi}_n | P \tilde{H} P | \tilde{\Psi}_n \rangle \approx \langle \Psi_i | H | \Psi_i \rangle$$

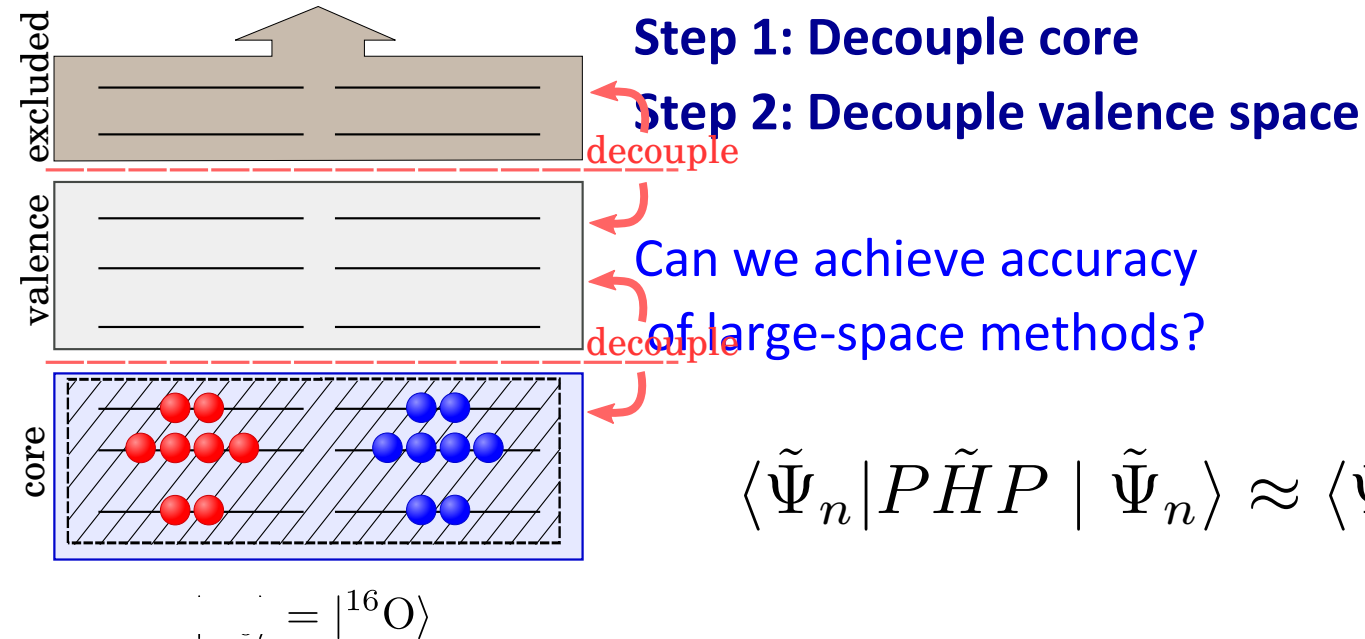
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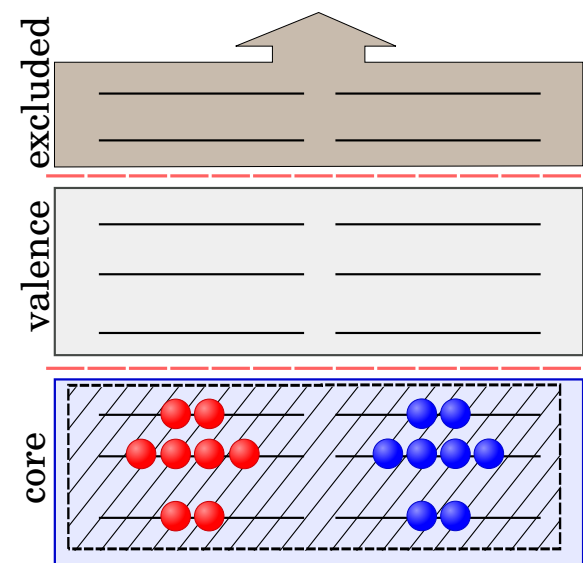
$\langle P H P \rangle$	$\langle P H Q \rangle \rightarrow 0$
$\langle Q H P \rangle \rightarrow 0$	$\langle Q H Q \rangle$

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$$\tilde{H} = e^\Omega H e^{-\Omega} = H + [\Omega, H] + \frac{1}{2} [\Omega, [\Omega, H]] + \dots$$

$$\tilde{\mathcal{O}} = e^\Omega \mathcal{O} e^{-\Omega} = \mathcal{O} + [\Omega, \mathcal{O}] + \frac{1}{2} [\Omega, [\Omega, \mathcal{O}]] + \dots$$



Step 1: Decouple core

Step 2: Decouple valence space

Step 3: Decouple additional operators

$$\langle \tilde{\Psi}_n | P \tilde{H} P | \tilde{\Psi}_n \rangle \approx \langle \Psi_i | H | \Psi_i \rangle$$

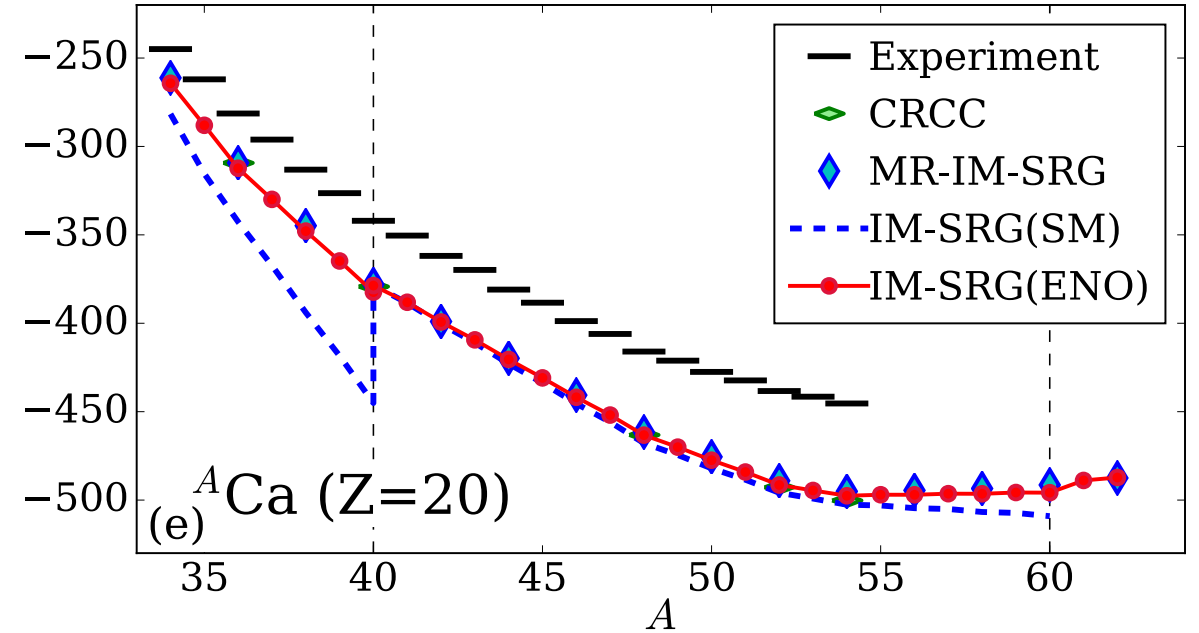
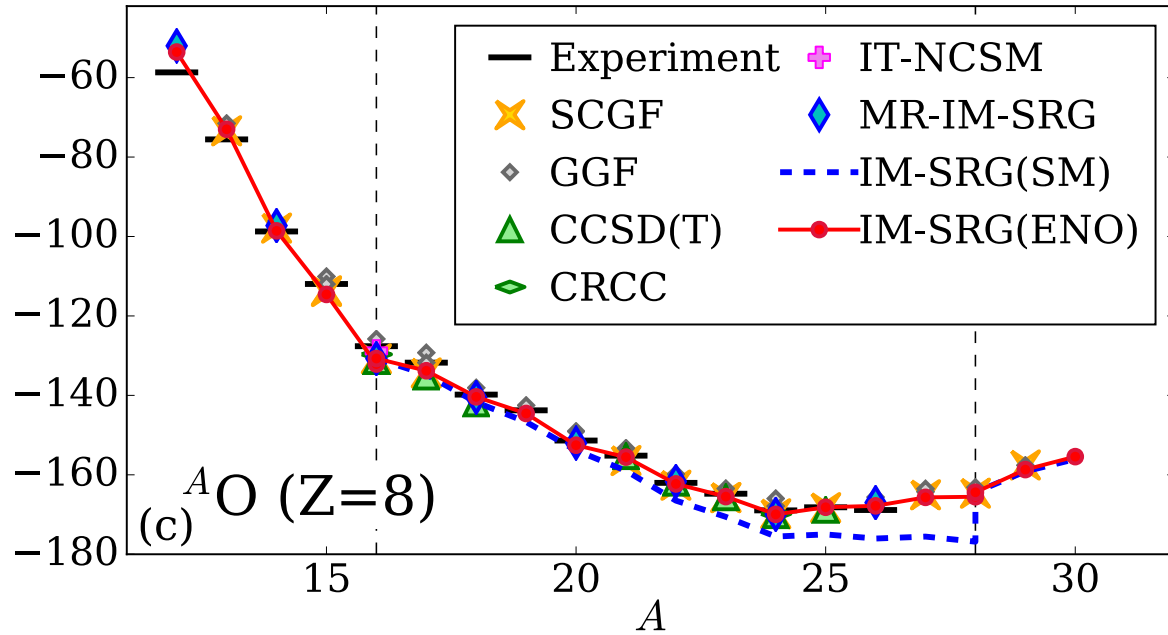
$$\langle \tilde{\Psi}_n | P \tilde{M}_{0\nu} P | \tilde{\Psi}_n \rangle \approx \langle \Psi_i | M_{0\nu} | \Psi_i \rangle$$

Careful benchmarking essential

$$|\Psi_i\rangle = |^{16}\text{O}\rangle$$

$\langle P H P \rangle$	$\langle P H Q \rangle \rightarrow 0$
$\langle Q H P \rangle \rightarrow 0$	$\langle Q H Q \rangle$

New approach accesses **all nuclei:** agrees to 1% with large-space methods



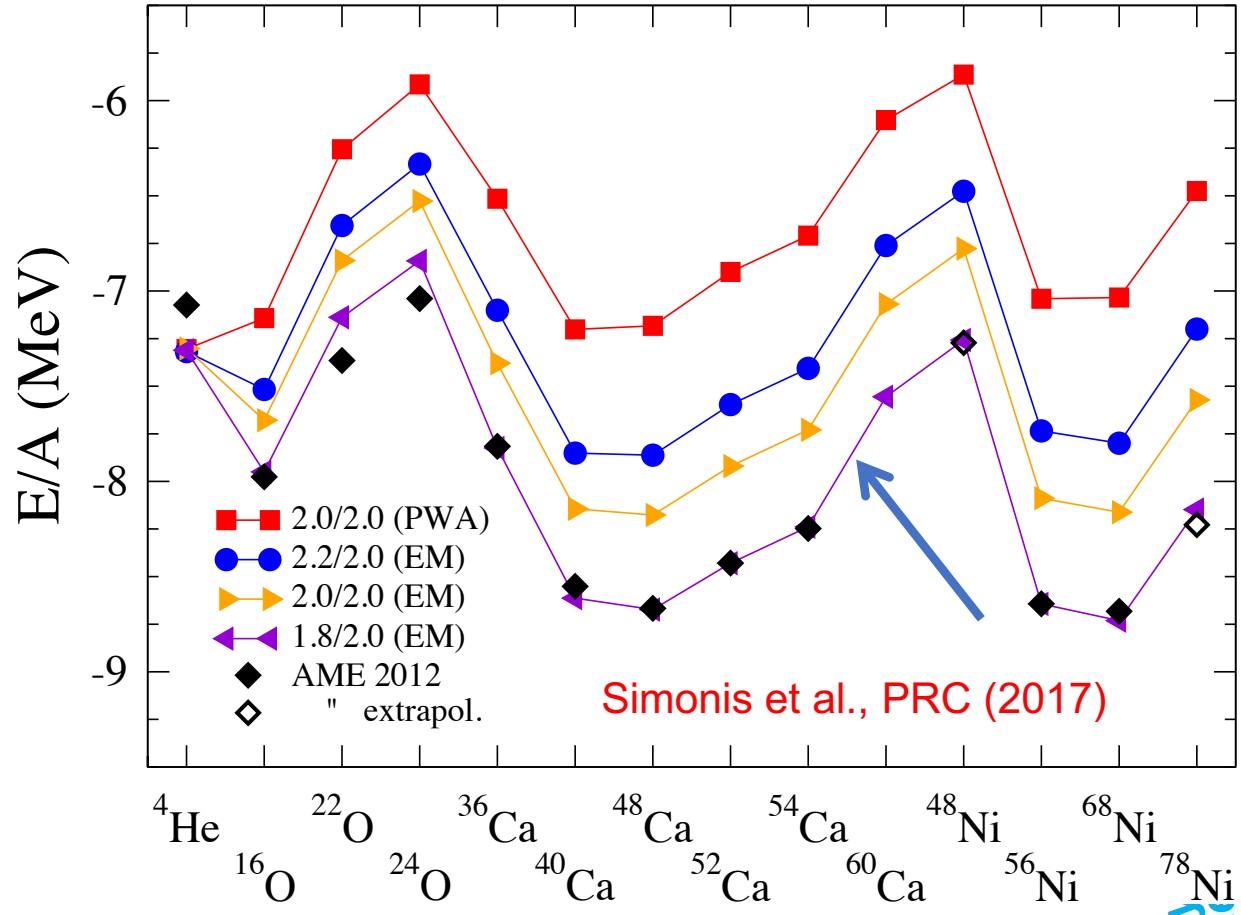
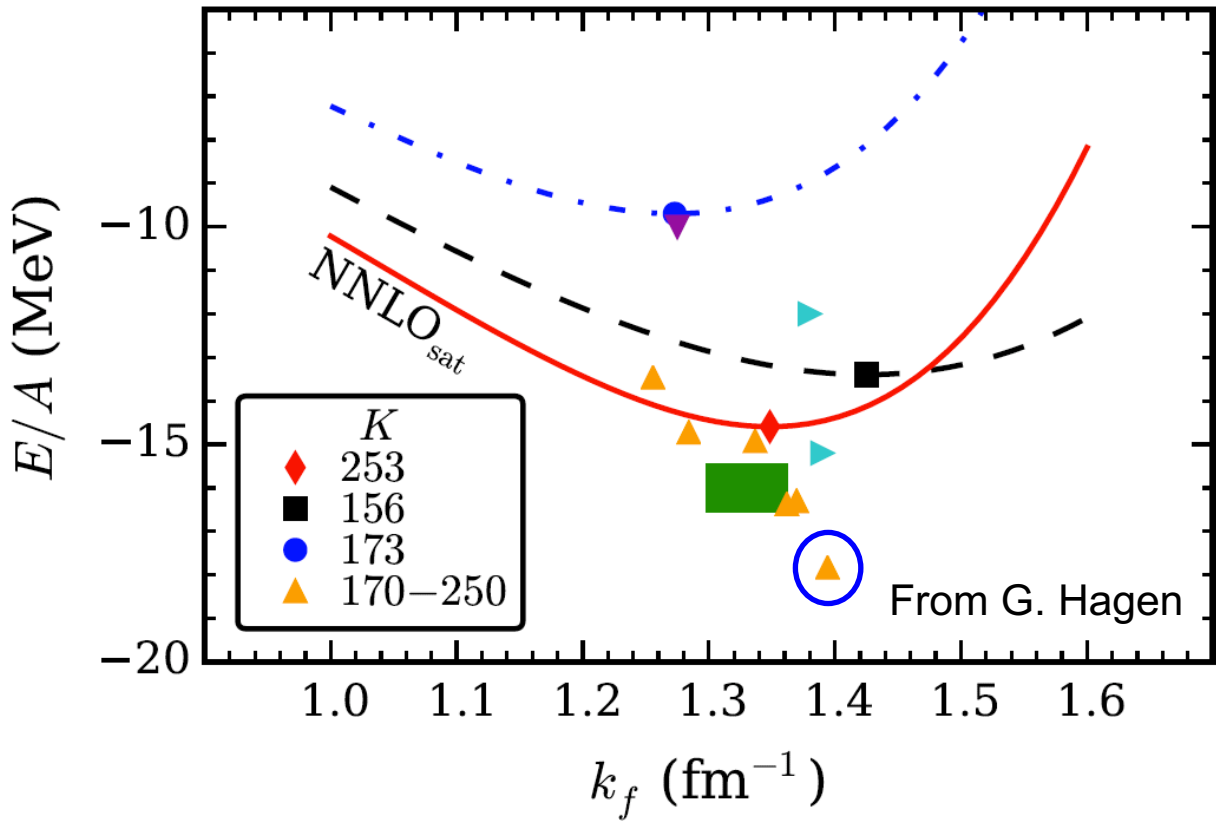
Stroberg et al., PRL (2017)

Agreement with *experiment* deteriorates for heavy chains (due to input Hamiltonian)

Significant gain in applicability with little/no sacrifice in accuracy

Low computational cost: ~1 node-day/nucleus

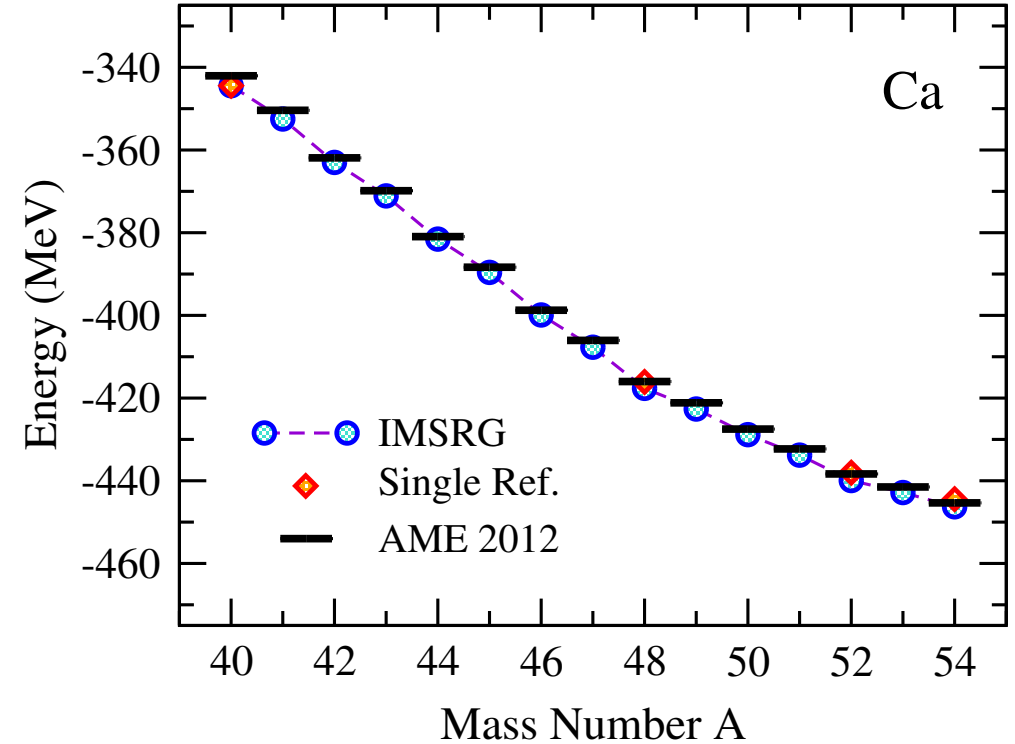
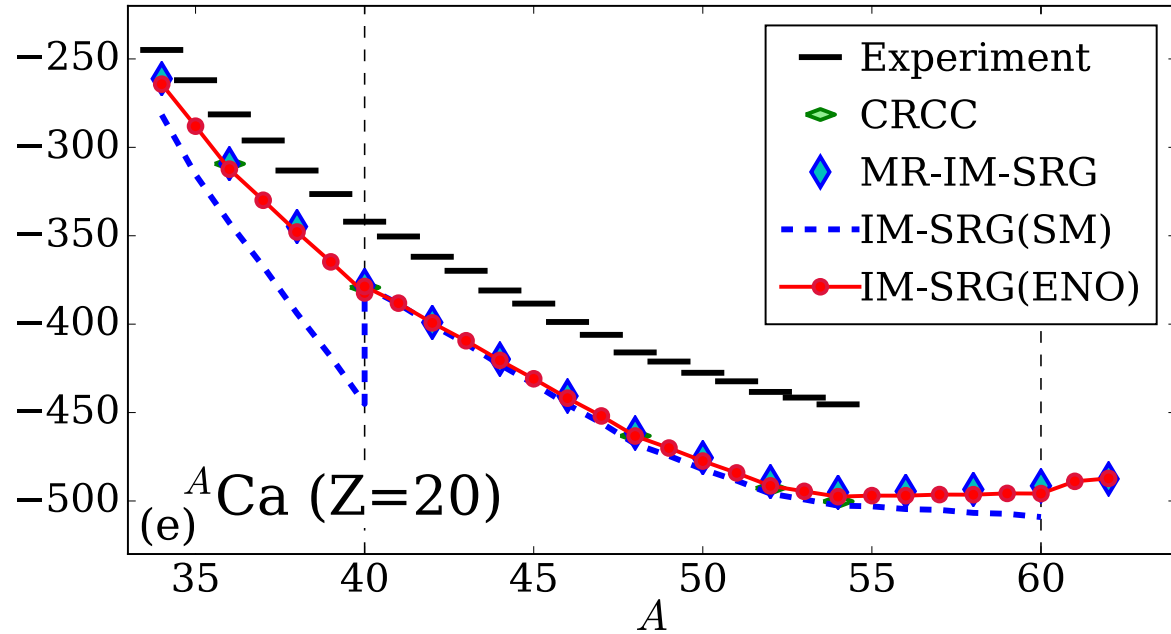
NN+3N force with good reproduction of ground-state energies (but poor radii)



1.8/2.0 (EM) reproduces ground-state energies through ^{78}Ni

Slight underbinding for neutron-rich oxygen

Dramatic improvement with respect to experimental data



Opens possibility for reliable ab initio predictions across the nuclear chart!

Accesses **all** properties of **all** nuclei:

- Ground states, excited states, radii, electroweak transitions...