## The Experimental Study of Shape Coexistence in ${ }^{114}$ Sn via GRIFFIN

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## Shell Model and "Magic" Nuclei

ELECTRONS
NUCLEONS

- Nucleons arranged in respective shells
- Filled valence shells are associated with increased stability
- "Doubly- / Singly-Magic"
- "Magic" nuclei characteristically spherical in ground state



## Quadrupole Deformation



Oblate (earth)


Prolate (rugby ball)

from NNDC NuDat

## Signatures of Nuclear Shape: B(E2)

- Non-magic ${ }^{130} \mathrm{Ba}$ shows highly collective excitations
- High B(E2) values
- Indicative of the rotational band and deformed nuclear shape
- Singly-magic ${ }^{134} \mathrm{Te}$ shows non-collective excitations
- Low B(E2) values
- Seniority scheme implies sphericity



## ${ }^{186} \mathrm{~Pb}$ and Shape Coexistence

- $\mathrm{Z}=82$ closed proton shell implying spherical shape in g.s.
- Shape coexistence is Two or more states having distinct properties and different intrinsic shapes within a narrow energy range
- Characterized by rotational bands of excited states allowed by deformed shapes (prolate \& oblate, etc.)


Ojala, J. et al. Reassigning the shapes of the $0^{+}$states in the ${ }^{186} \mathrm{~Pb}$ nucleus. Commun Phys 5, 213 (2022)

## Shape Coexistence in Sn Isotopes

- Closed proton shell @ Z=50
- Near spherical g.s.
- First excited $2^{+}$corresponds to a noncollective breaking of neutron-pair
- Excitation $\mathrm{E} \approx 1.3 \mathrm{MeV}$
- Low B(E2; $2_{1}{ }^{+} \rightarrow 0_{1}{ }^{+}$)
- Mid-shell rotational band built upon 2p-2h configuration
- Hypothesised to be built upon $\mathrm{O}_{2}{ }^{+}$ state (blue)



## ${ }^{116}$ Sn Shape Coexistence

- Findings from Pore et. al (2016) regarding ${ }^{116}$ Sn suggest a reevaluation of the head of the $2 p-2 h$ band within this nucleus
- $\mathrm{B}\left(\mathrm{E} 2 ; 2^{+}{ }_{2} \rightarrow \mathrm{O}^{+}{ }_{3}\right) / \mathrm{B}\left(\mathrm{E} 2 ; 2^{+}{ }_{2} \rightarrow 0^{+}{ }_{2}\right) \approx 2.2$
- Based upon intensity measurement of very weak $85-\mathrm{keV}$ transition


| $E_{\text {level }}$ <br> $(\mathrm{keV})$ | $T_{1 / 2}$ <br> ref. $[5]$ | $J_{i}^{\pi} \rightarrow J_{f}^{\pi}$ | $E_{\gamma}$ <br> $(\mathrm{keV})$ | $I_{\gamma}$ | $B R_{\gamma}$ | $B(E 2)$ <br> (W.u.) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $2112.19(14)$ | $1.89(10) \mathrm{ps}$ | $2_{2}^{+} \rightarrow 0_{3}^{+}$ | $85.294(88)$ | $0.00166(10)$ | $0.0091(6)$ | $99.7(84)$ |
|  |  | $2_{2}^{+} \rightarrow 0_{2}^{+}$ | $355.432(18)$ | $0.939(23)$ | $5.16(14)$ | $44.4(28)$ |

## A Case for ${ }^{114}$ Sn Inquiry

- ${ }^{114} \mathrm{Sn}$ level scheme is highly similar to that of ${ }^{116} \mathrm{Sn}$ and other mid-shell Tin isotopes
- Missing observation of key $2_{2}{ }^{+} \rightarrow 0_{3}{ }^{+}$transition
- No established lifetime or branching ratios from $2_{2}{ }^{+}$state of interest
- Existing lifetime lower limit of $\tau>2.1 \mathrm{ps}$
- Most recent $\beta$-decay study of ${ }^{114} \mathrm{Sb} \rightarrow{ }^{114} \mathrm{Sn}$ was M. E. J. Wigmans et. Al, Phys. Rev. C 14, 229 (1976)



## Challenge of the 82-keV Transition

$$
\frac{\lambda\left(2_{2}^{+} \rightarrow 0_{3}^{+}\right)}{\lambda\left(2_{2}^{+} \rightarrow 0_{1}^{+}\right)}=\left[\frac{E_{\gamma}\left(2_{2}^{+} \rightarrow 0_{3}^{+}\right)}{\left.E_{\gamma} 2_{2}^{+} \rightarrow 0_{1}^{+}\right)}\right]^{5}=\left[\frac{82 \mathrm{keV}}{2239 \mathrm{keV}}\right]^{5}=6.6 \times 10^{-8}
$$

Eqn. 1 - Decay rate ratio of competing $2_{2}{ }^{+} \rightarrow \mathrm{O}_{3}{ }^{+}(82 \mathrm{keV})$ to $2_{2}{ }^{+} \rightarrow \mathrm{O}_{1}{ }^{+}(2239 \mathrm{keV})$ transitions via
single particle estimate

- For E2 transitions, transition rate is proportional to $E_{\gamma}^{5}$
- Energetic favourability of $2239-\mathrm{keV}$ transition depopulating the $2_{2}{ }^{+}$state is predicted to occur $1.52 \times 10^{7}$ times for each $82-\mathrm{keV}$ transition
- If consistent with Pore et. al's measurements the relative intensity of the $82-\mathrm{keV}$ transition is predicted to be increased by a factor of $10^{3}$



## ISAC @ TRIUMF



## GRIFFIN Spectrometer



## $\gamma$-Events



- High intensity of ${ }^{114} \mathrm{In}$ imposed significant limitations on DAQ

|  | Proposal | Experiment |
| :---: | :---: | :---: |
| Beam <br> Intensity | 1.0 E 6 pps | 5.0 E 5 pps |
| $\mathbf{t}_{\text {implantation }}$ | 2100 s | 390 s |
| $\mathbf{t}_{\text {decay }}$ | 210 s | 390 s |

## $\gamma$-Efficiency

Simulated Efficiency
vs. Experimental Efficiency


## $\gamma-\gamma$ Coincidence




## Partial Level Scheme of ${ }^{114}$ Sn



## 856-keV Gate



## 856-keV Gate (zoom)



## Conclusions and Outlook

- ${ }^{114} \mathrm{Sn}^{*}$ populated via ${ }^{114} \mathrm{Sb}$ decay to GRIFFIN w/ intensity of 5E5 pps over $\sim 48$ hour experiment
- 5.7 TB of data collected over $\sim 48$ hours of beam-time
- Preliminary analysis of $\gamma-\gamma$ coincidences did not observe the weak $2^{+}{ }_{2} \rightarrow 0^{+}{ }_{3}$ transition
- Established the upper limit $B\left(E 2 ; 2^{+}{ }_{2} \rightarrow 0^{+}{ }_{3}\right) / B\left(E 2 ; 2^{+}{ }_{2} \rightarrow 0^{+}{ }_{2}\right) \leq 10$
- Established upper limit on Branching ratio $\left(2^{+}{ }_{2} \rightarrow 0^{+}{ }_{3}\right) /\left(2^{+}{ }_{2} \rightarrow 0^{+}{ }_{2}\right) \leq 0.0207$
- E0 transitions, $\gamma-\gamma-\gamma$ coincidences, and feeding ratios still to be investigated
- A large number of $\gamma-\gamma$ coincidences have been collected
- Extend level scheme of ${ }^{114} \mathrm{Sn}$
- $\quad \gamma-\gamma$ angular correlation measurements
- Fast-timing measurements with $\mathrm{LaBr}_{3}(\mathrm{Ce})$ detectors
- Significant amount of analysis ahead


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## Nuclear Shapes*

- Described by a multipole expansion in $\lambda$ :

$$
-R(\theta, \phi)=c(\alpha) R_{0}\left[1+\sum_{\lambda=0}^{\infty} \sum_{\mu=-\lambda}^{\lambda} \alpha_{\lambda \mu} Y_{\lambda \mu}(\theta, \phi)\right]
$$

- Multipole order: $2^{\lambda}$
- $2^{0}=$ monopole - breathing mode
- $2^{1}=$ dipole - center of mass shift
- $2^{2}=$ quadrupole - reflection symmetric deformation
- Deformed nuclear shape arises from long-range multipolemultipole interactions between protons and neutrons in the

Oblate (earth)


Prolate (rugby ball)
 nuclear valence space

## ${ }^{186}$ Pb Shape Coexistence*

- Two or more states having distinct properties and different intrinsic shapes within a narrow energy range
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## Decay of ${ }^{114} S b$ to ${ }^{114} S n * *$

## $\beta^{+}$-decay

- Protons are spontaneously converted to neutrons, releasing a positron and an electron neutrino


## Electron Capture (EC)

- Proton spontaneously captures an atomic electron, converting it to a neutron and neutrino



## GRIFFIN Spectrometer*



## GRIFFIN Spectrometer*



SFU

## $\gamma$-Events*



