



Centre Canadien de Recherche en  
Physique des Astroparticules  
Arthur B. McDonald  
Canadian Astroparticle Physics Research Institute

# The flavour of high-energy neutrinos

Aaron Vincent



# Featuring



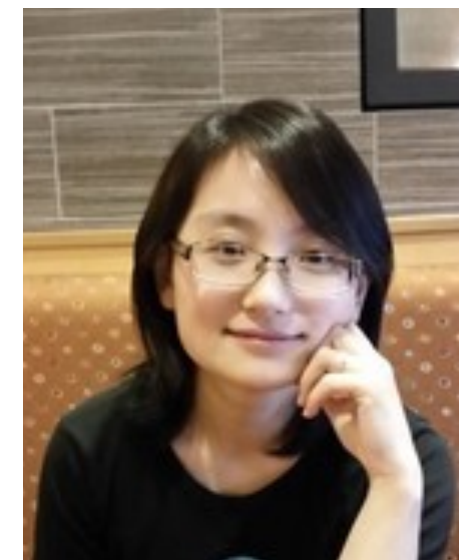
Carlos Argüelles  
Harvard



Ali Kheirandish  
Las Vegas



Mauricio Bustamante  
Niels Bohr Institute



Shirley Li  
UC Irvine



Ningqiang Song  
CN Yang ITP

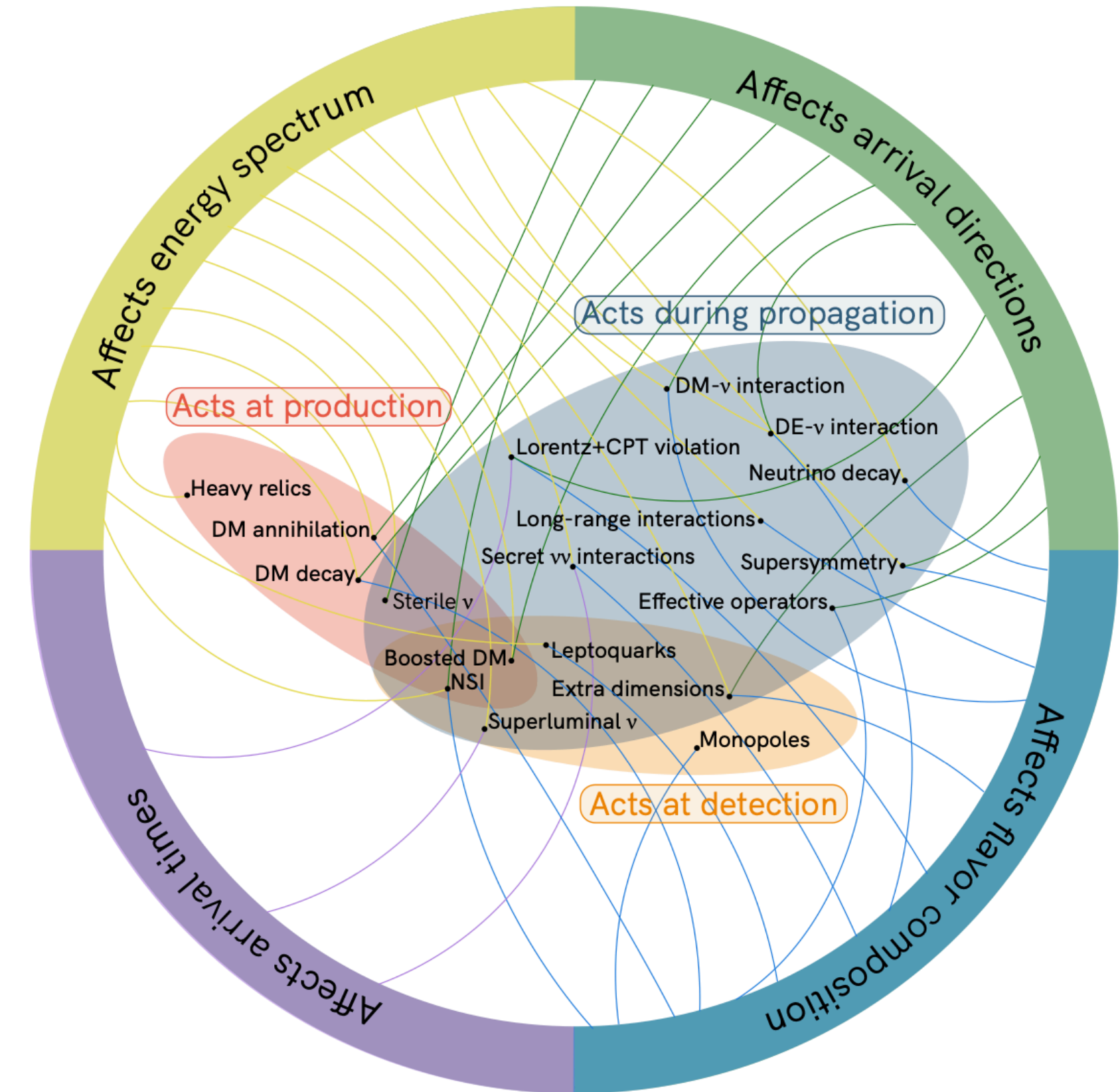
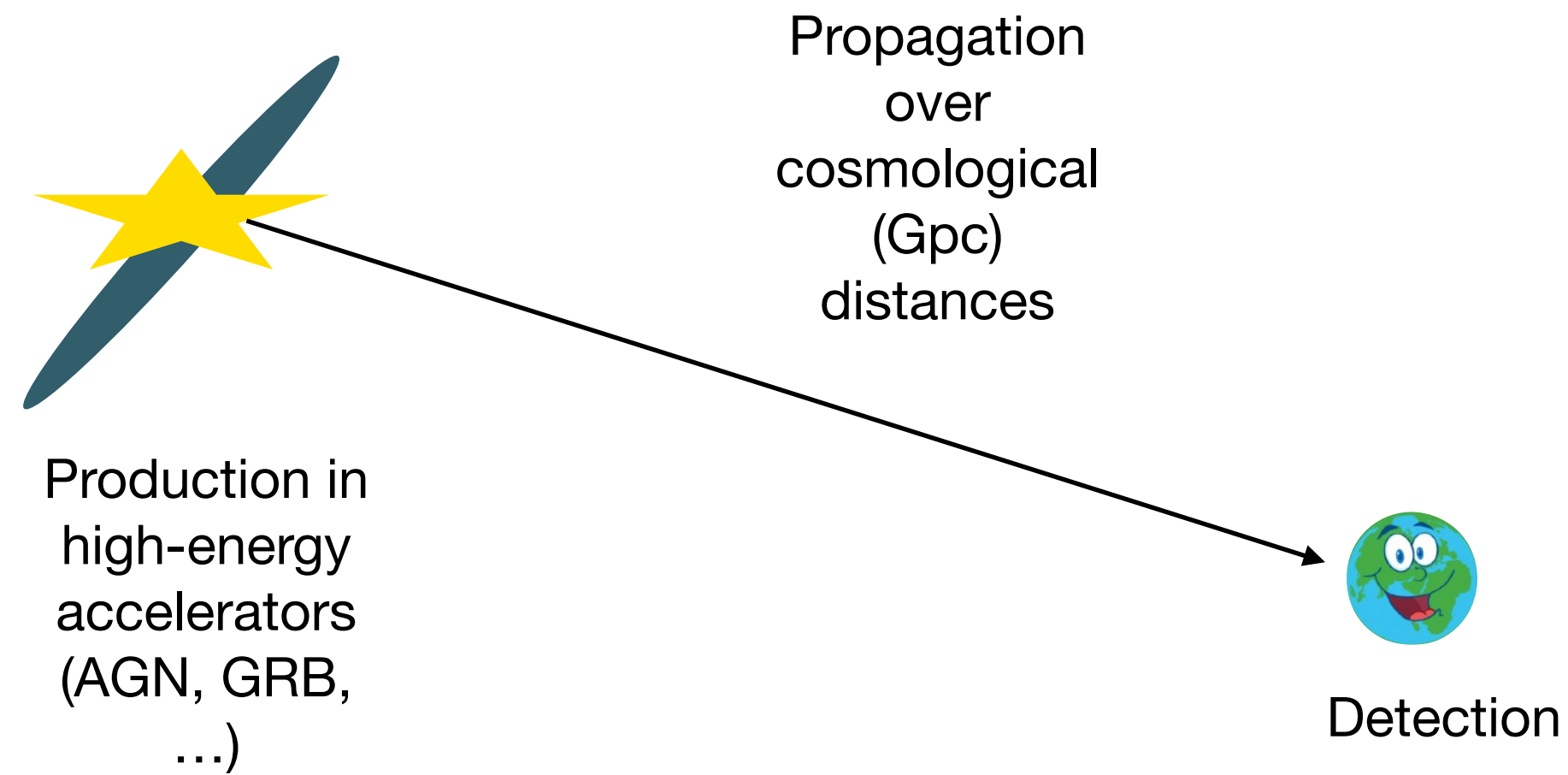


**Damiano  
Fiorillo  
NBI**

**Qinrui Liu  
Queen's**



# High-energy neutrinos



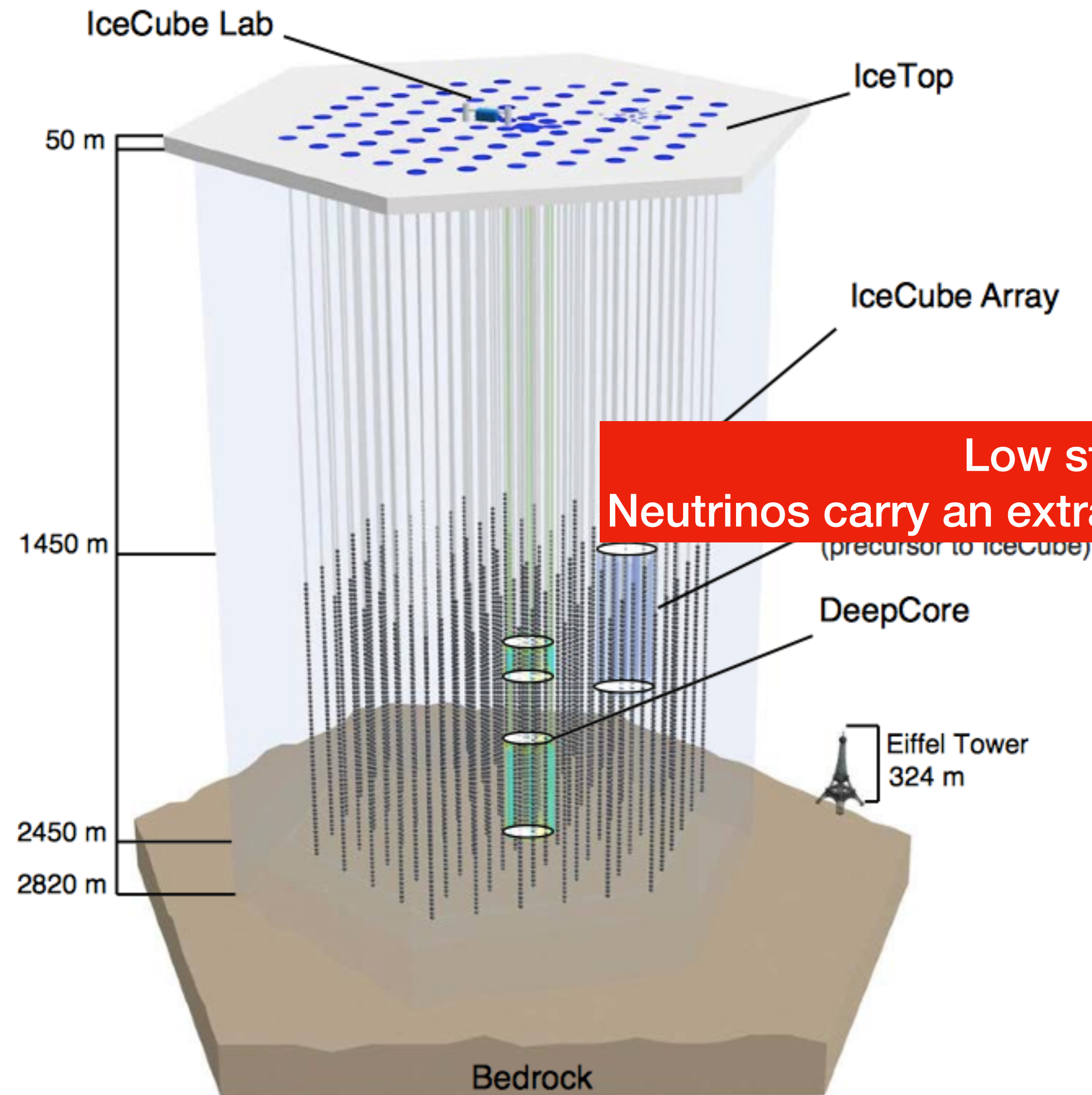
Neutrinos can tell us about “standard model” physics:

- Nature of these accelerators
- Oscillation, interaction with intergalactic medium
- Detection: high-energy neutrino-nucleus cross sections

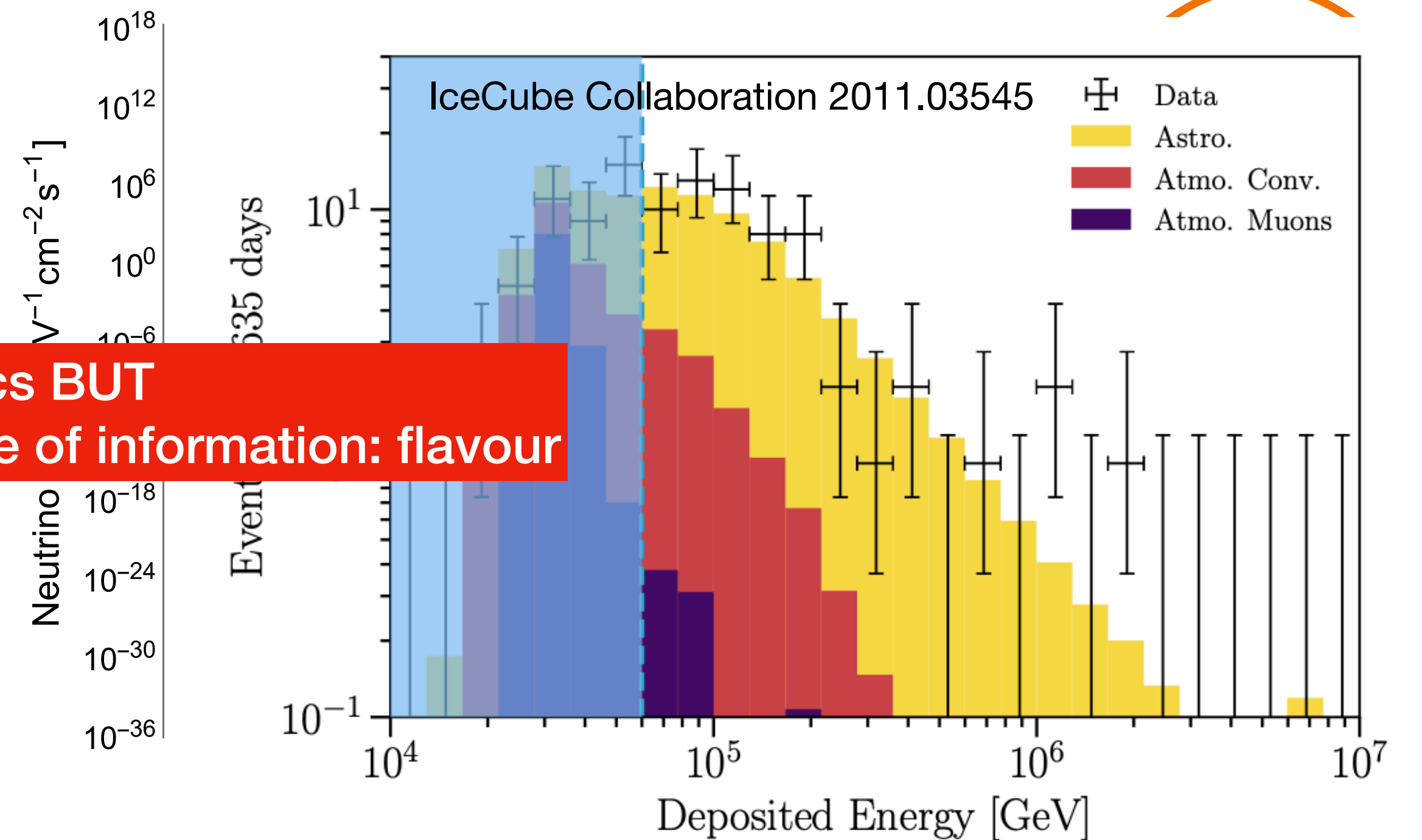
## New Physics?

# Current observations: IceCube (south pole)

Effective volume  $\sim 1 \text{ km}^3$



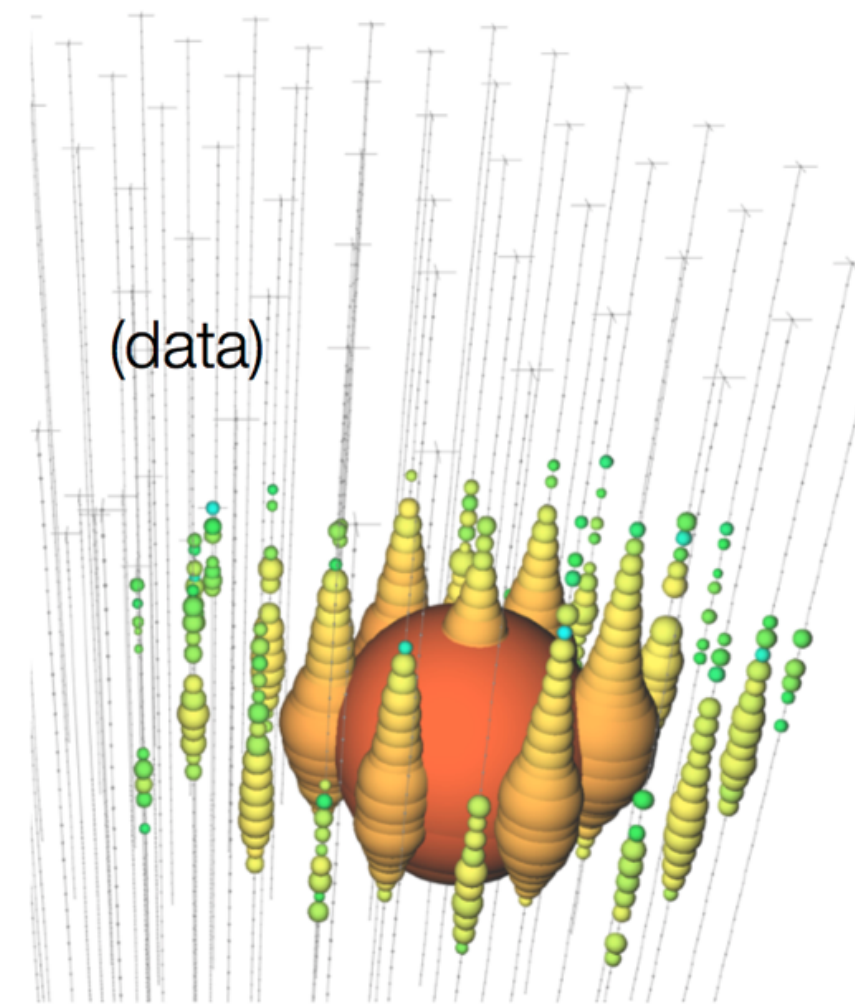
Low statistics BUT  
Neutrinos carry an extra piece of information: flavour



large exposures necessary  
due to low fluxes

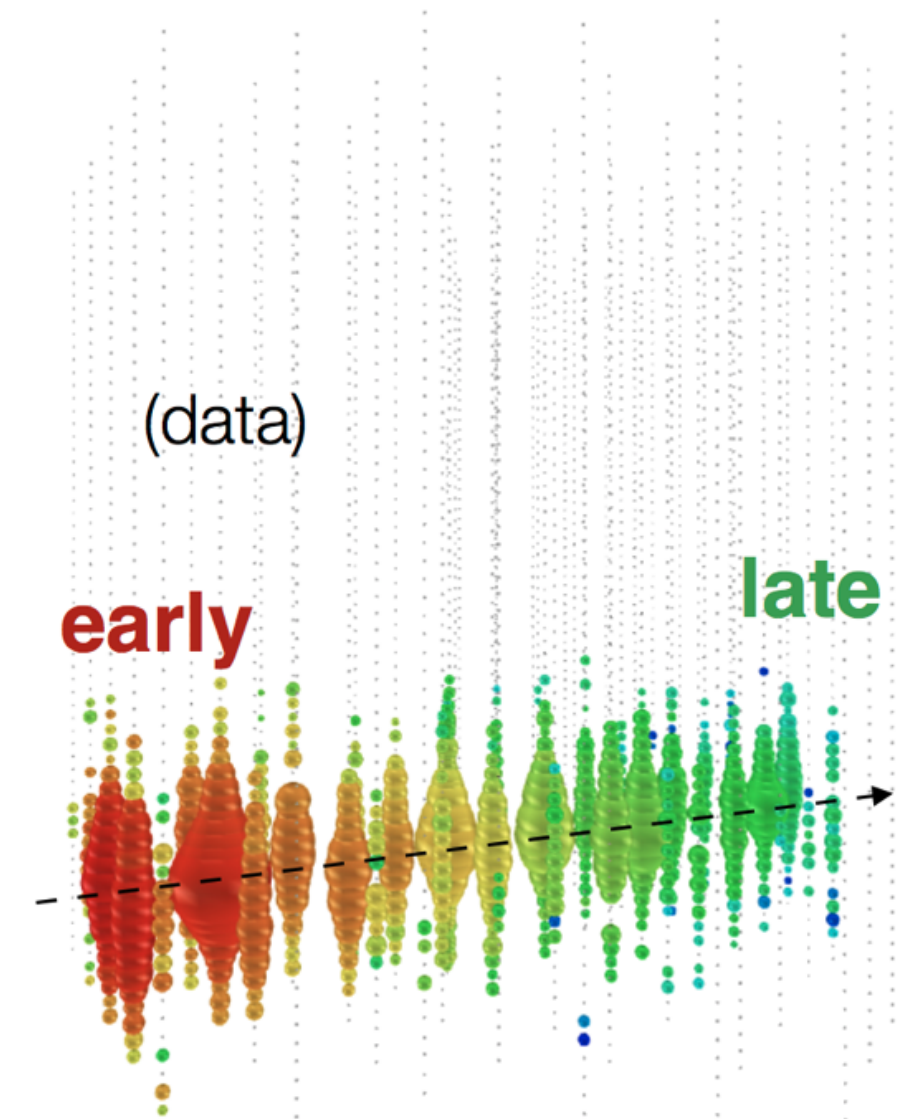
# Flavour: event morphology

Neutral-current /  $\nu_e$



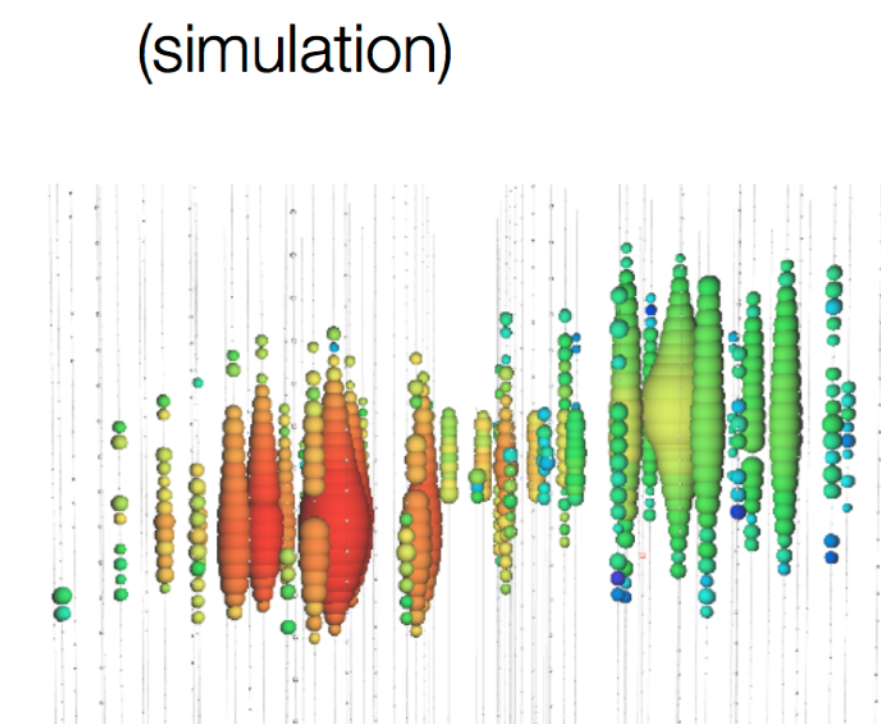
Isolated energy  
deposition (cascade)  
with no track

Charged-current  $\nu_\mu$



Up-going track

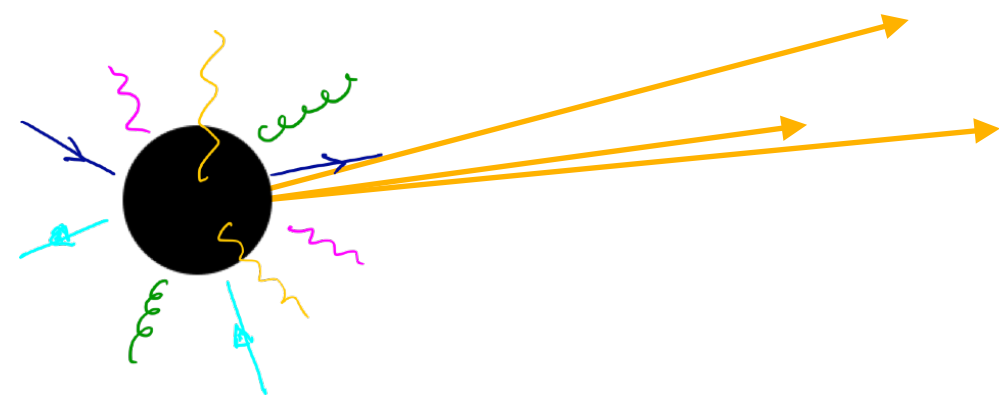
Charged-current  $\nu_\tau$



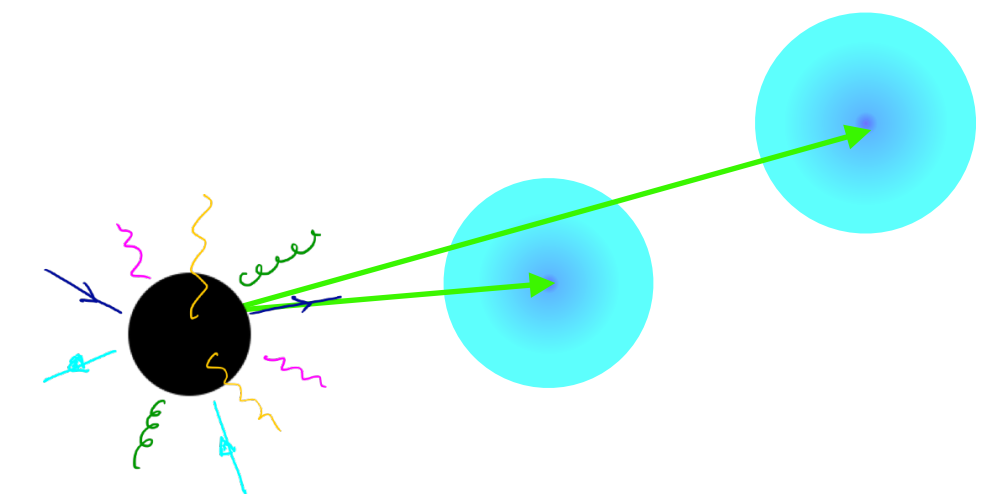
Double cascade

# Aside: new physics can give new morphologies

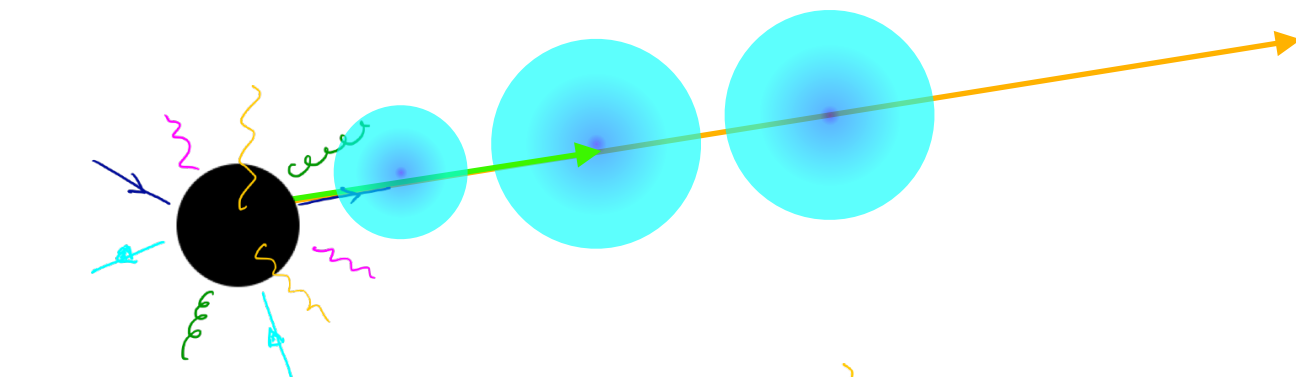
Microscopic black hole signatures: Mack, Song, ACV 1912.06656



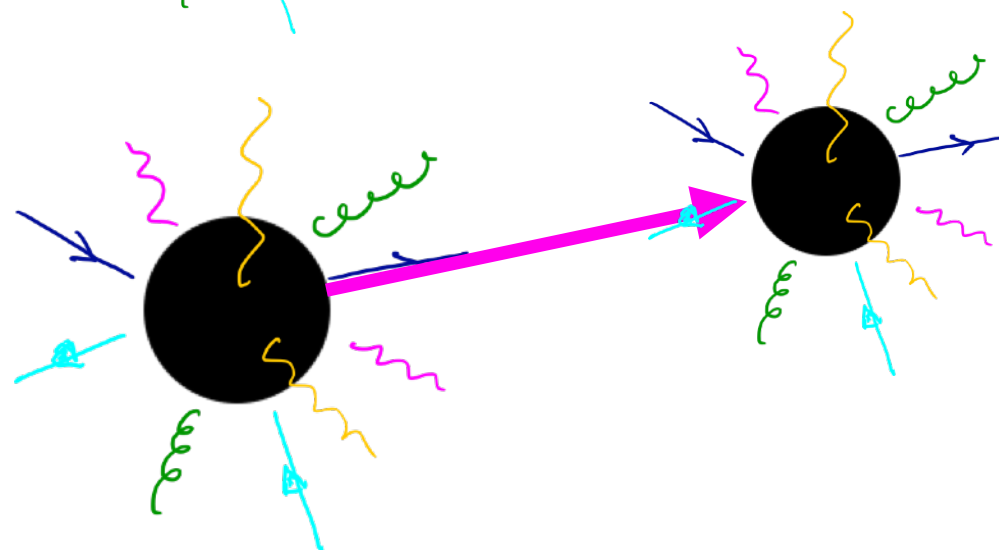
**Multitrack** (hard to see)



**n-bang** (only 0.2% of black hole events)



**Kebab:** (About 3% of cases)

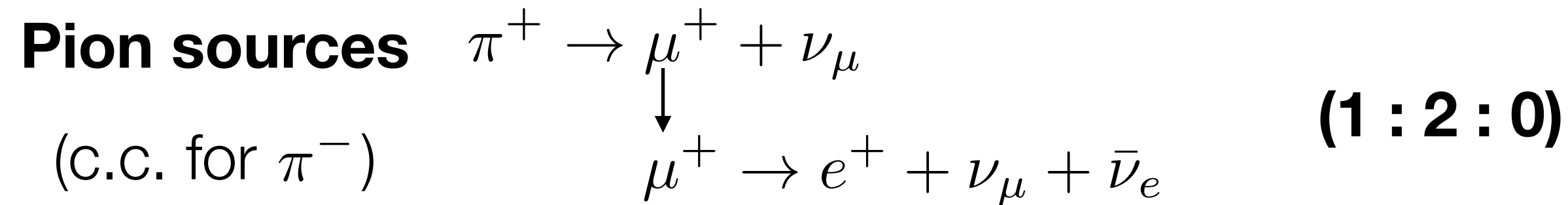


**Double black hole bang:** (very rare!!)

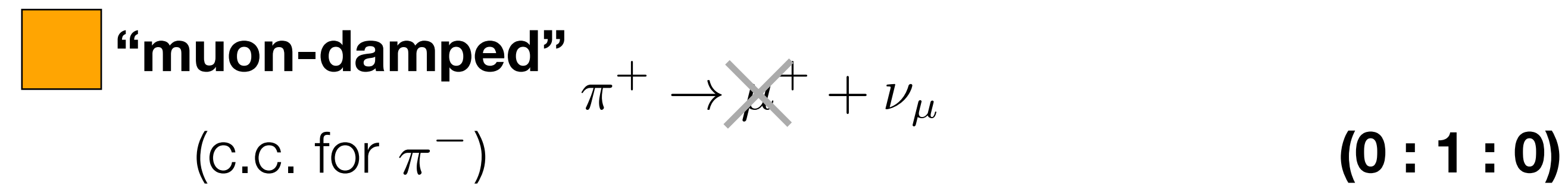
# Flavour composition in astrophysical sources

(GRBs, AGNs, blazars, pulsars...)

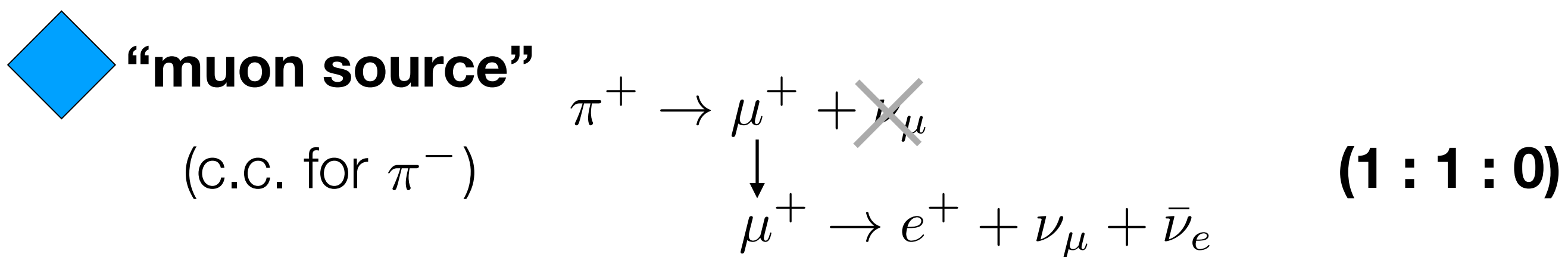
$(\alpha_e : \alpha_\mu : \alpha_\tau)$



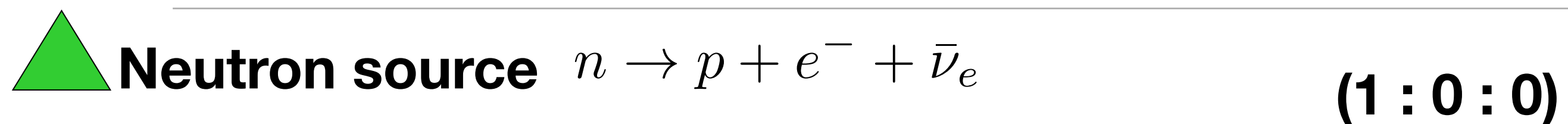
Different scenarios: different production environments

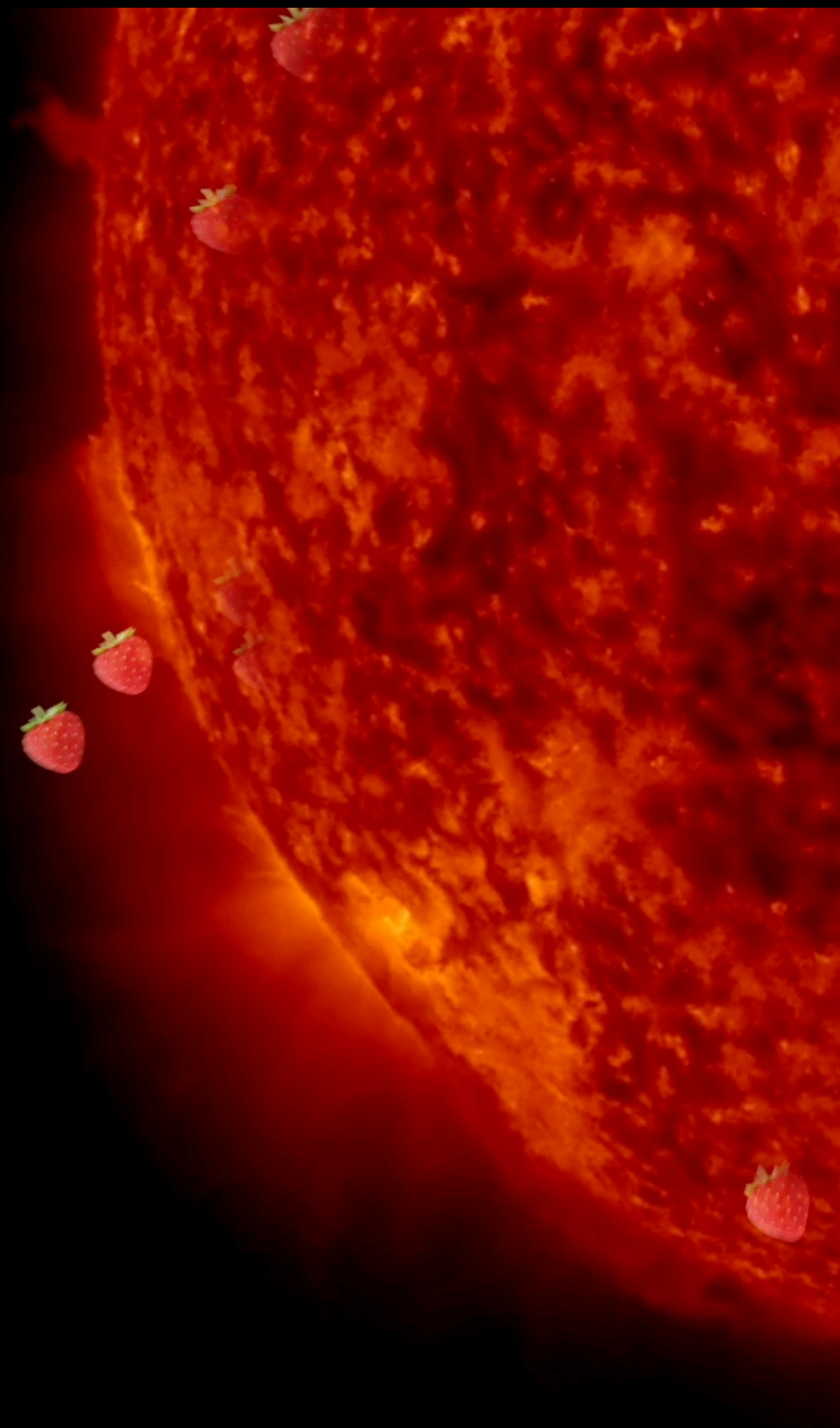


Flavour can be distinguished **statistically** in neutrino detectors: different charged-current interactions lead to different event **morphologies** (there is some degeneracy)



Can we learn the flavour composition at the source to understand the production of astrophysical neutrinos?





Stan Yen



# Oscillation

Flavour eigenstates ( $\alpha = e, \mu, \tau$ ) are not eigenstates of the Hamiltonian ( $i = 1, 2, 3$ )

$$|\nu_\alpha\rangle = \sum_{i=1}^3 U_{\alpha i}^* |\nu_i\rangle,$$

Flavour basis

PMNS  
mixing  
matrix

mass basis

Distances are **large and uncorrelated** -> mixing **averages out**:

$$P_{\alpha \rightarrow \beta} = \sum_{i=1}^3 |U_{\alpha i}|^2 |U_{\beta i}|^2$$

$$f_{\beta, \oplus} = \sum_{\alpha=e, \mu, \tau} P_{\alpha\beta} f_{\alpha, S}$$

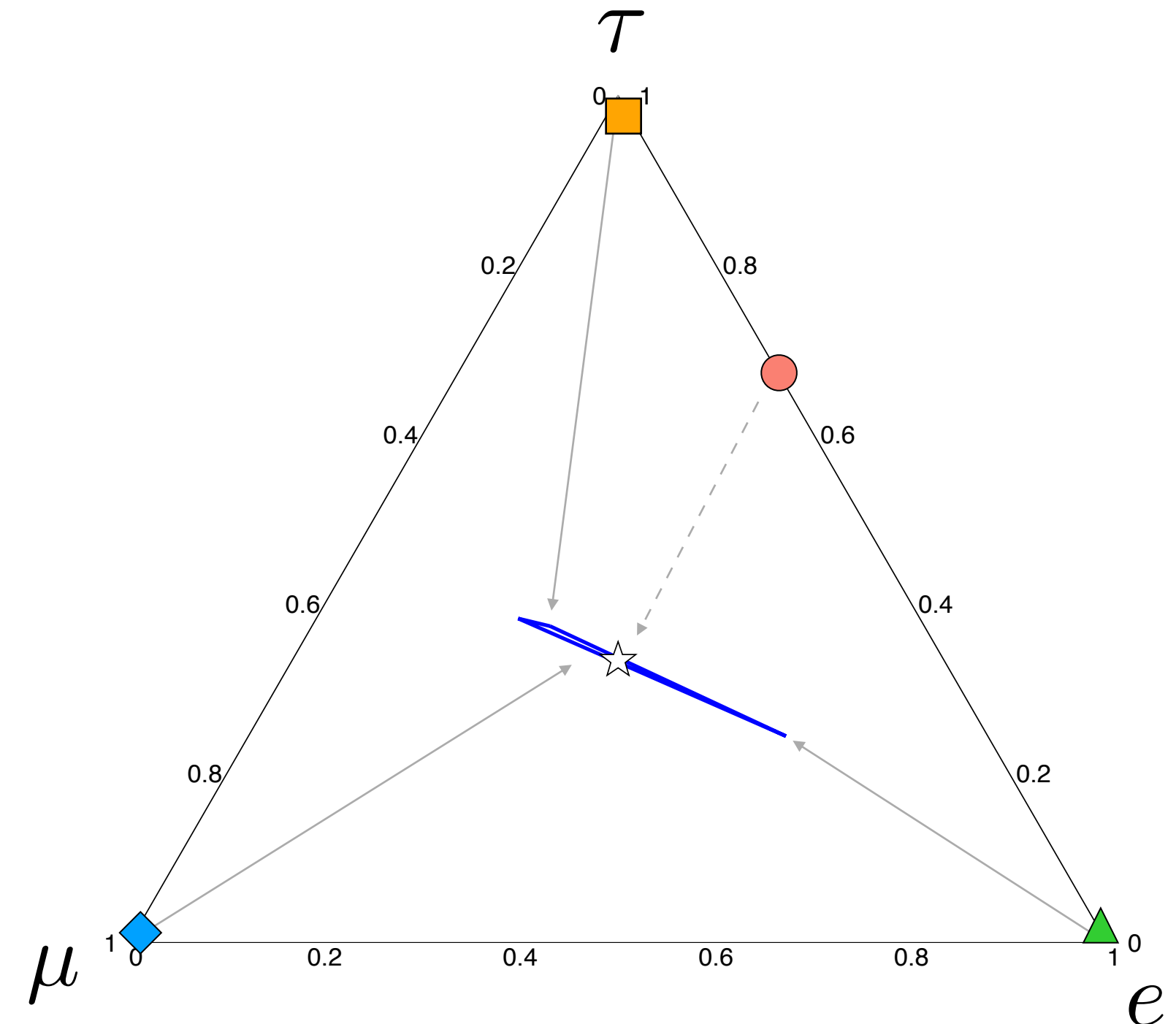
flavour composition  
at Earth

flavour composition  
at source

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{CP}} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta_{CP}} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta_{CP}} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta_{CP}} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta_{CP}} & c_{13}c_{23} \end{pmatrix}$$

$$c_{ij} \equiv \cos \theta_{ij}$$

$$s_{ij} \equiv \sin \theta_{ij}$$



# Flavour composition at Earth

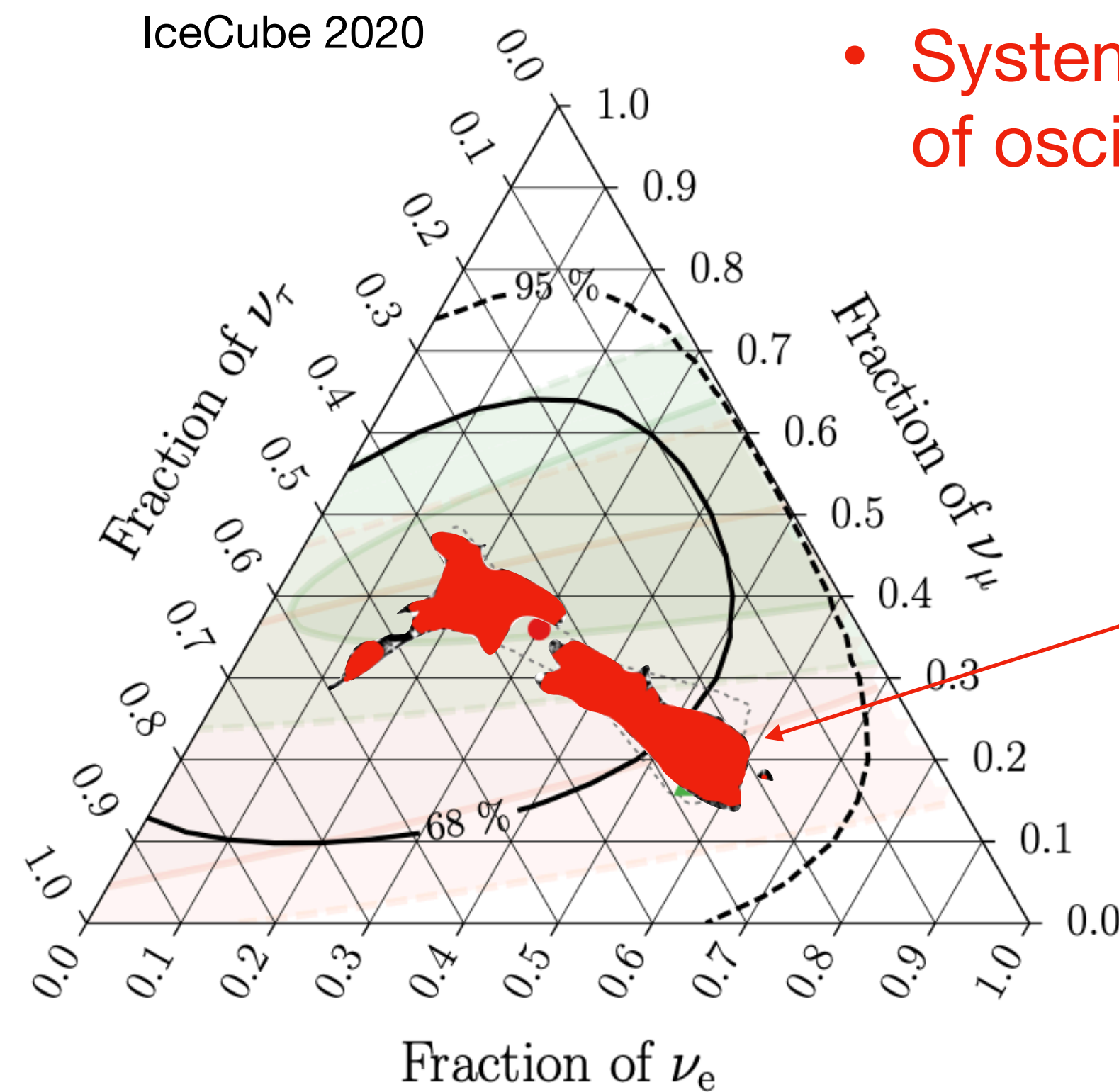
$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{CP}} \\ -s_{12}c_{23} - c_{12}s_{13}s_{23}e^{i\delta_{CP}} & c_{12}c_{23} - s_{12}s_{13}s_{23}e^{i\delta_{CP}} & c_{13}s_{23} \\ s_{12}s_{23} - c_{12}s_{13}c_{23}e^{i\delta_{CP}} & -c_{12}s_{23} - s_{12}s_{13}c_{23}e^{i\delta_{CP}} & c_{13}c_{23} \end{pmatrix}$$

NuFit 5.0 global fit

Parameter	Normal ordering	Inverted ordering
$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	$0.304^{+0.013}_{-0.012}$
$\sin^2 \theta_{23}$	$0.573^{+0.016}_{-0.020}$	$0.575^{+0.016}_{-0.019}$
$\sin^2 \theta_{13}$	$0.02219^{+0.00062}_{-0.00063}$	$0.02238^{+0.00063}_{-0.00062}$
$\delta_{CP} (\circ)$	$197^{+27}_{-24}$	$282^{+26}_{-30}$

Two limits:

- **Statistics** (astrophysical neutrinos)
- **Systematics: precise knowledge of oscillation parameters**



A flavour composition outside of this region = new physics (or you messed up)

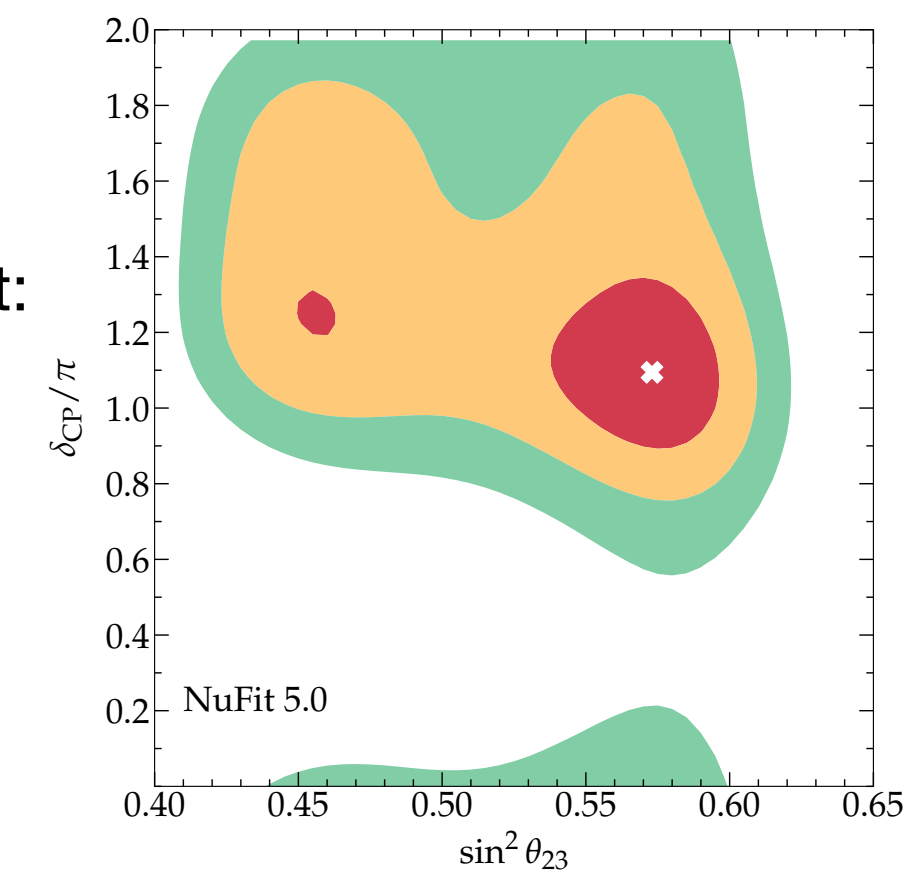
Mostly uncorrelated except:

$\theta_{12}$  (“solar angle”): Solar, reactor experiments

$\theta_{23}$  (“atmospheric angle”) Atmospheric, long-baseline

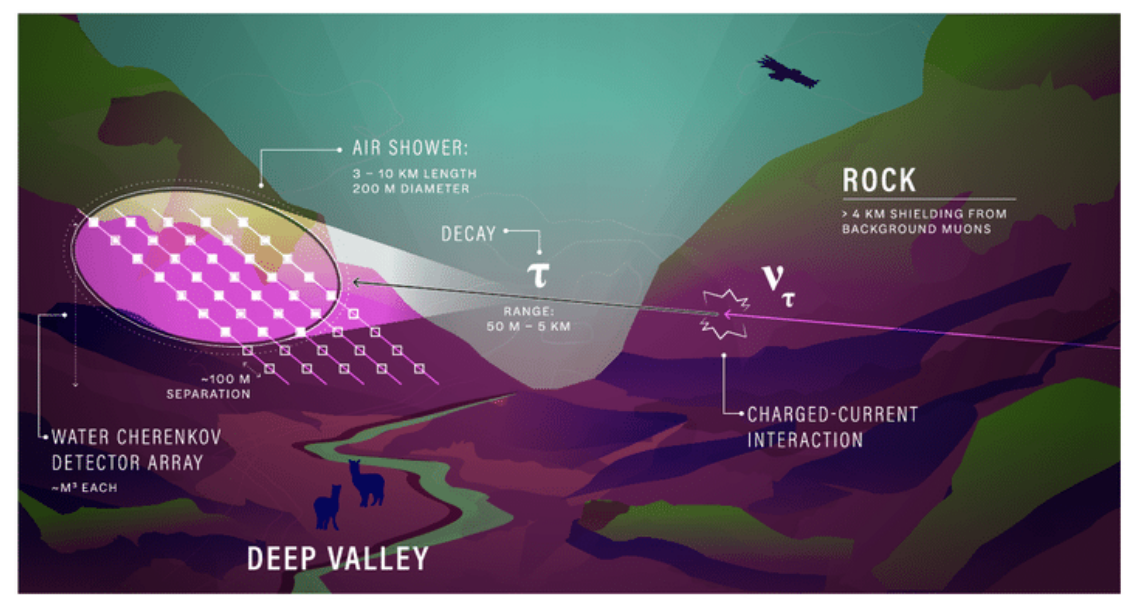
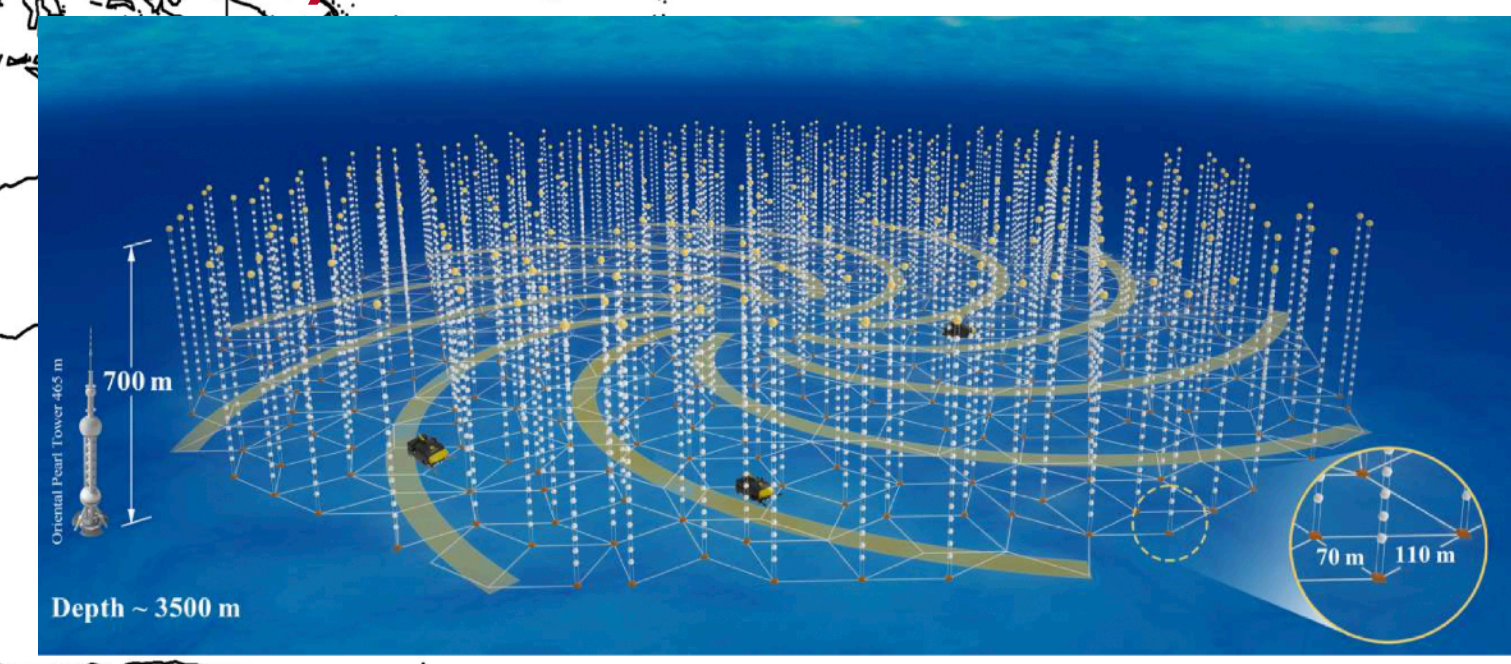
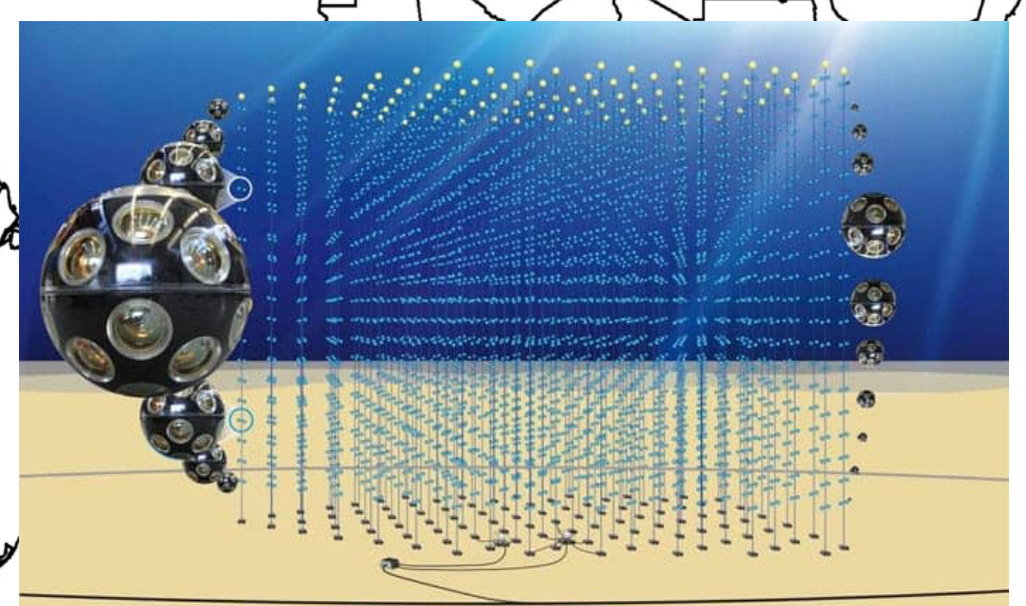
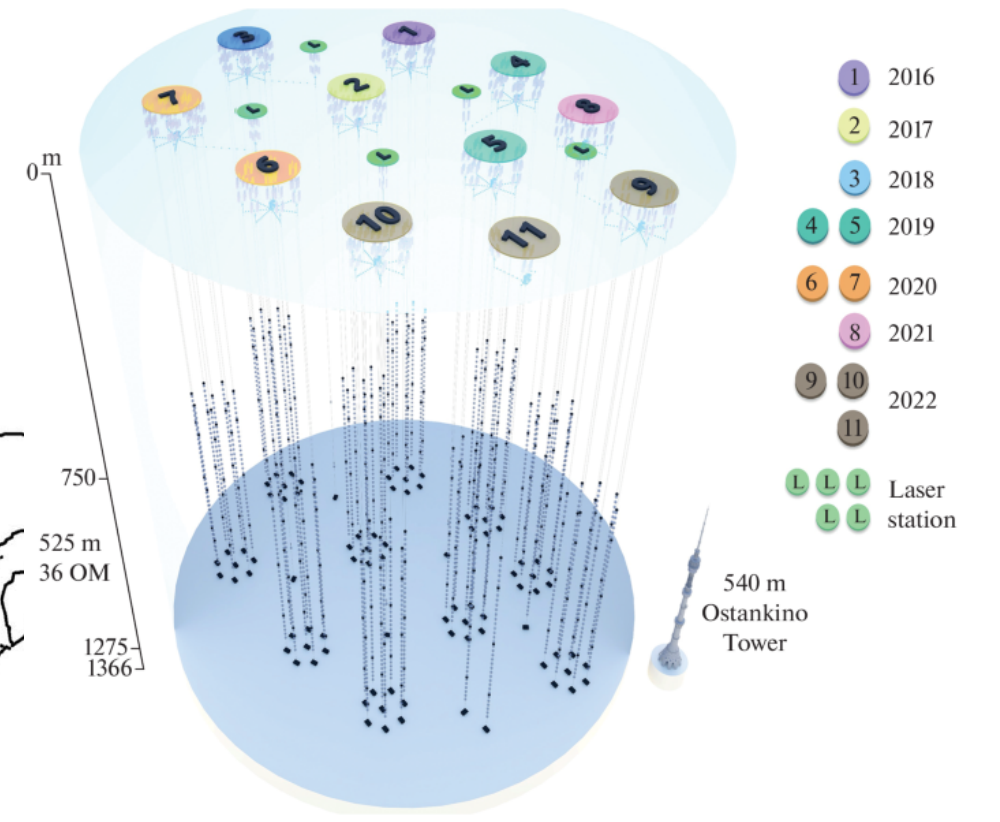
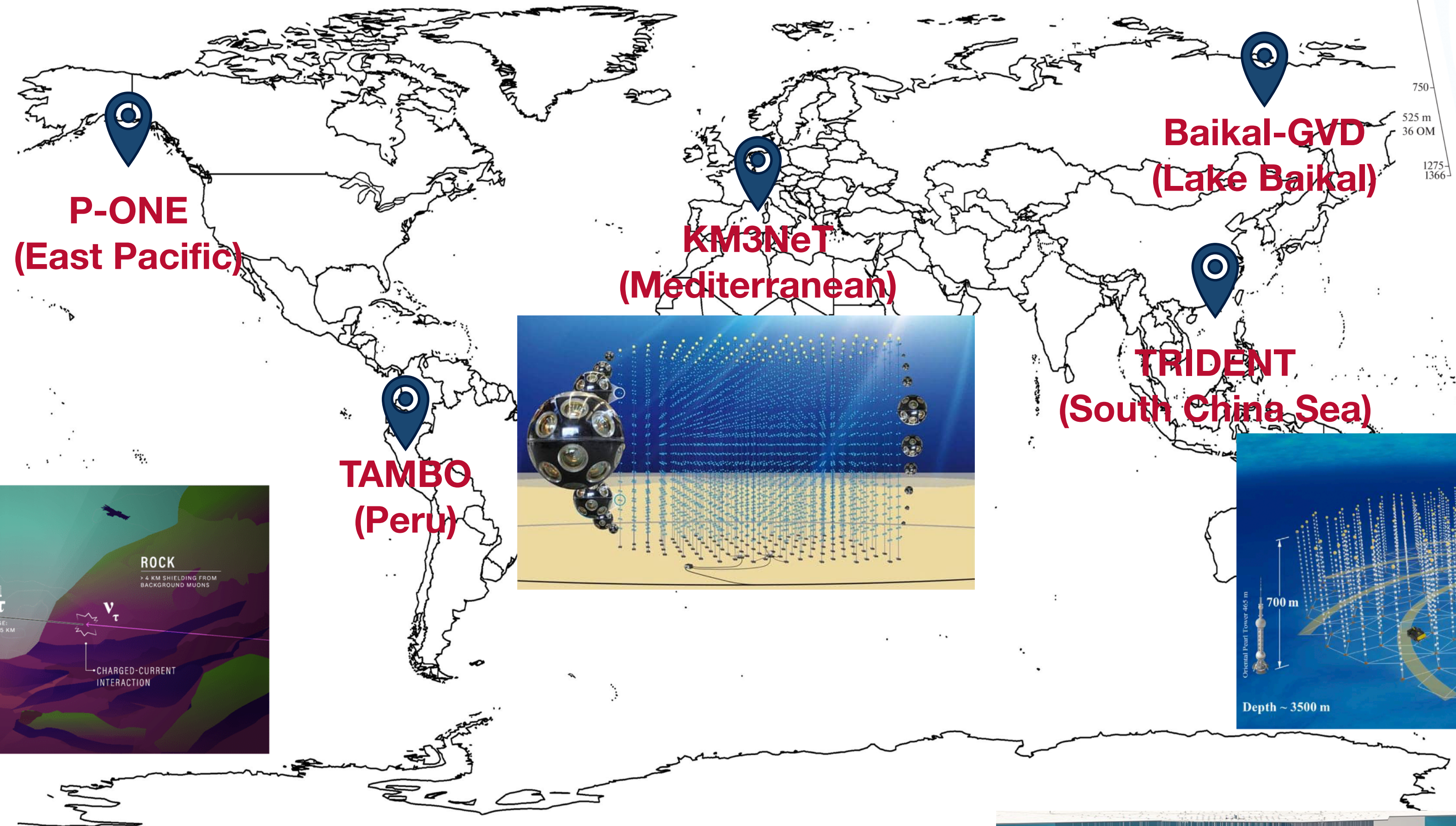
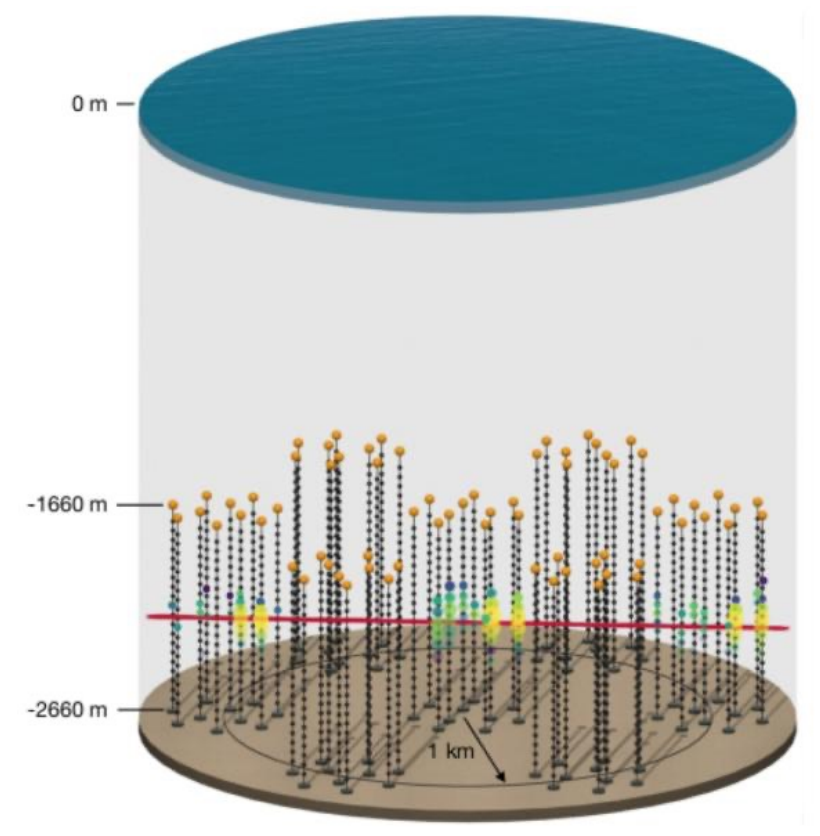
$\theta_{13}$  Reactor experiments

$\delta_{CP}$  Long-baseline experiments

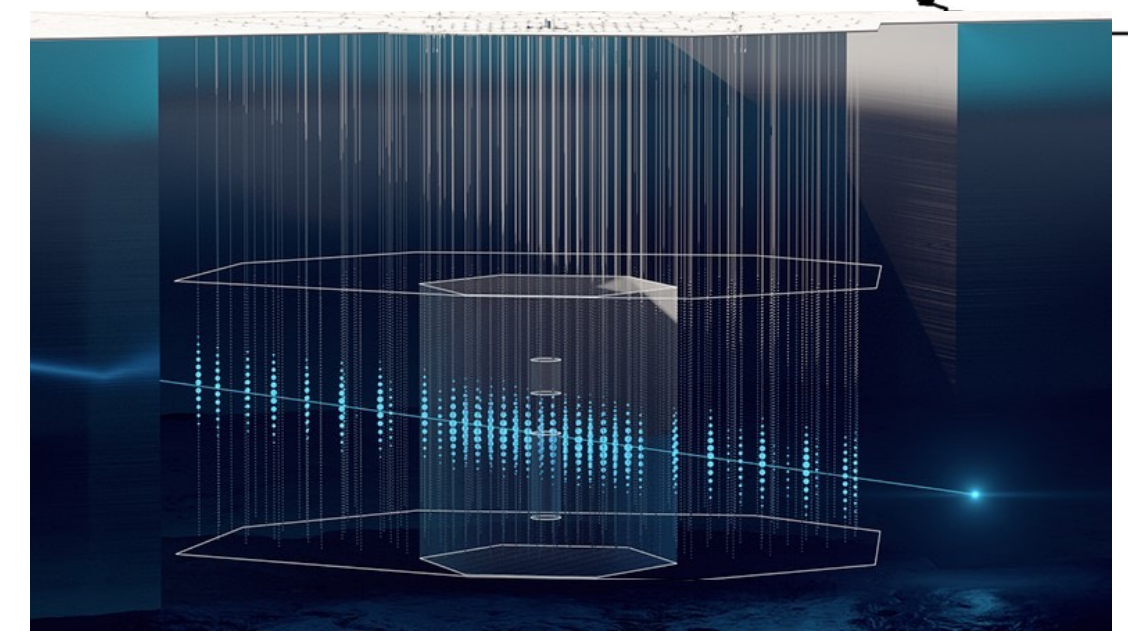


What does the future say about this?

# Next-Generation High-Energy Neutrino Telescopes



**IceCube-Gen2 (South Pole)**



# TAMBO

AIR SHOWER:

3 - 10 KM LENGTH  
200 M DIAMETER

DECAY

$\tau$

RANGE:  
50 M - 5 KM

ROCK

> 4 KM SHIELDING FROM  
BACKGROUND MUONS

$\nu_\tau$

CHARGED-CURRENT  
INTERACTION

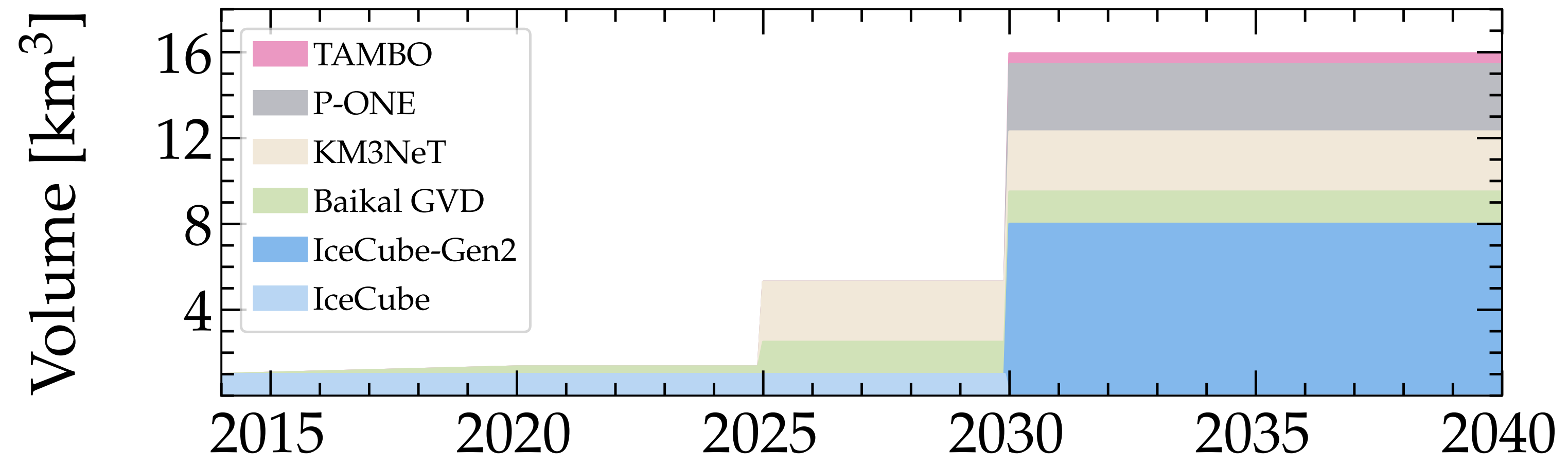
~100 M  
SEPARATION

WATER CHERENKOV  
DETECTOR ARRAY

~M<sup>3</sup> EACH

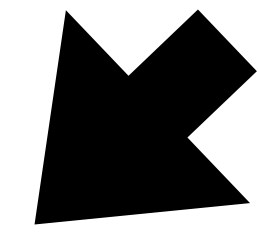
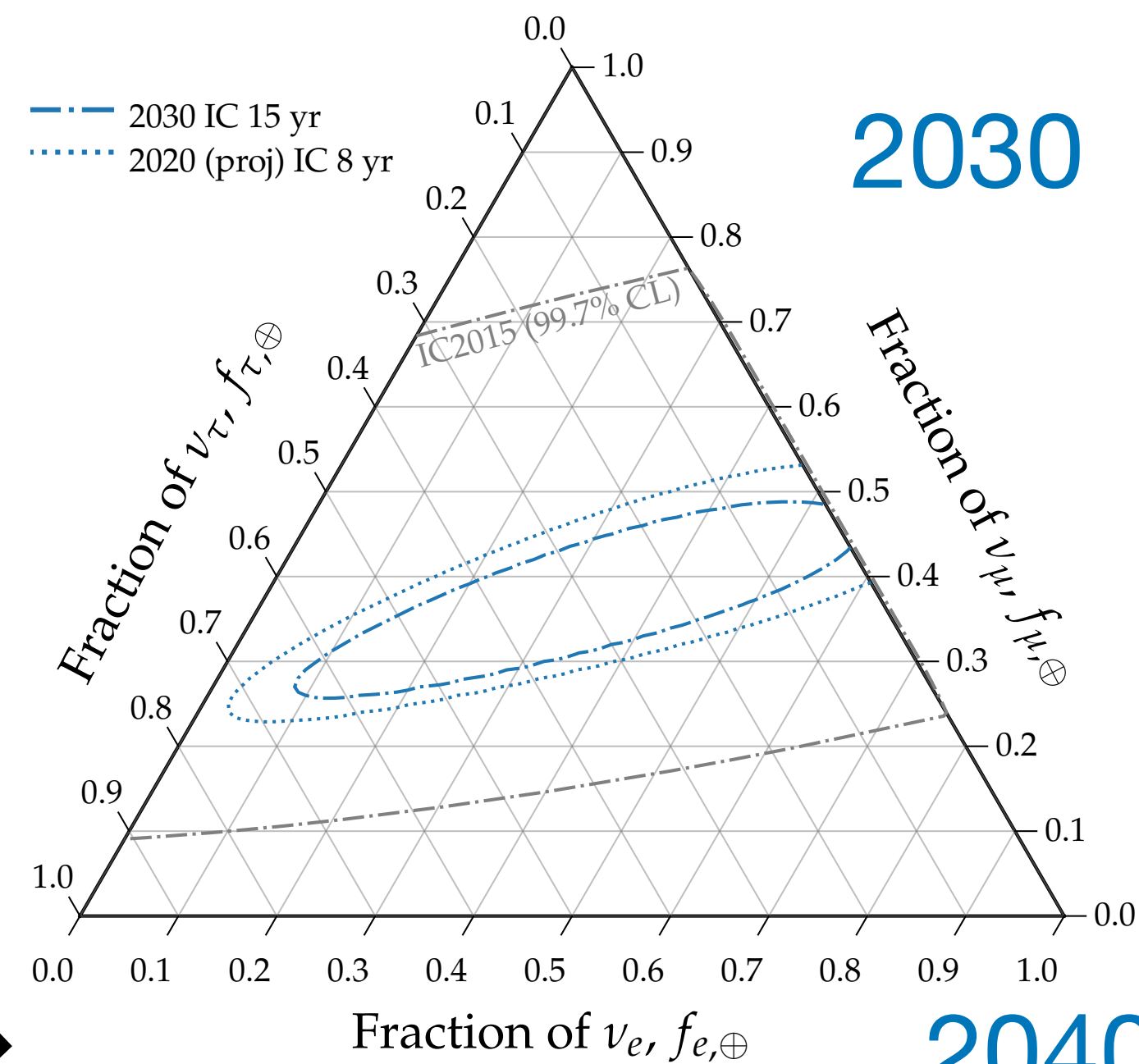
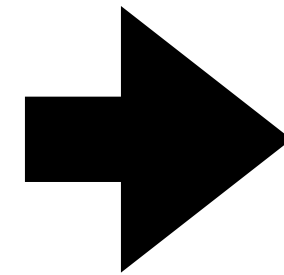
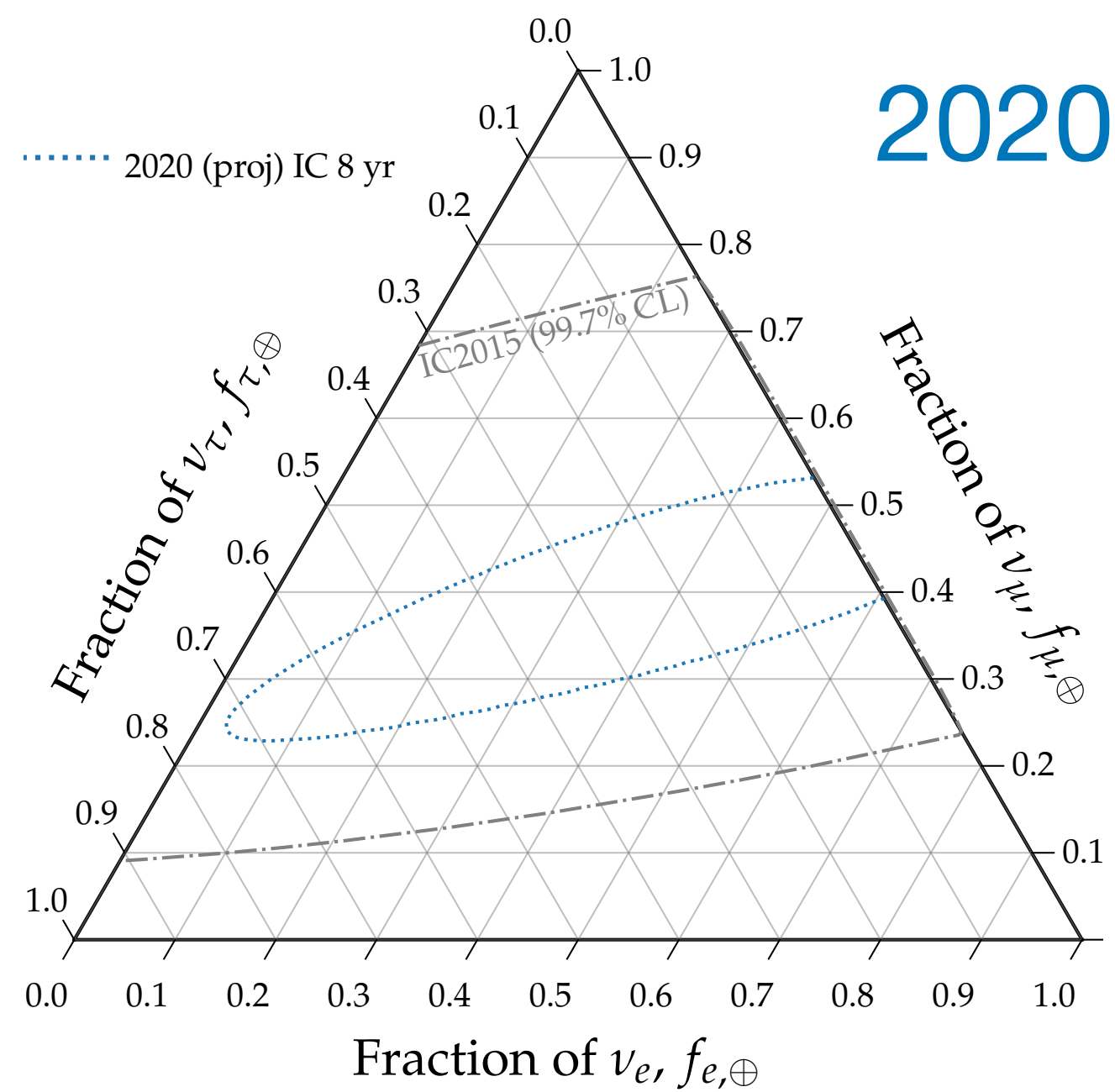
## DEEP VALLEY

# Statistics: need more Cherenkov telescopes!

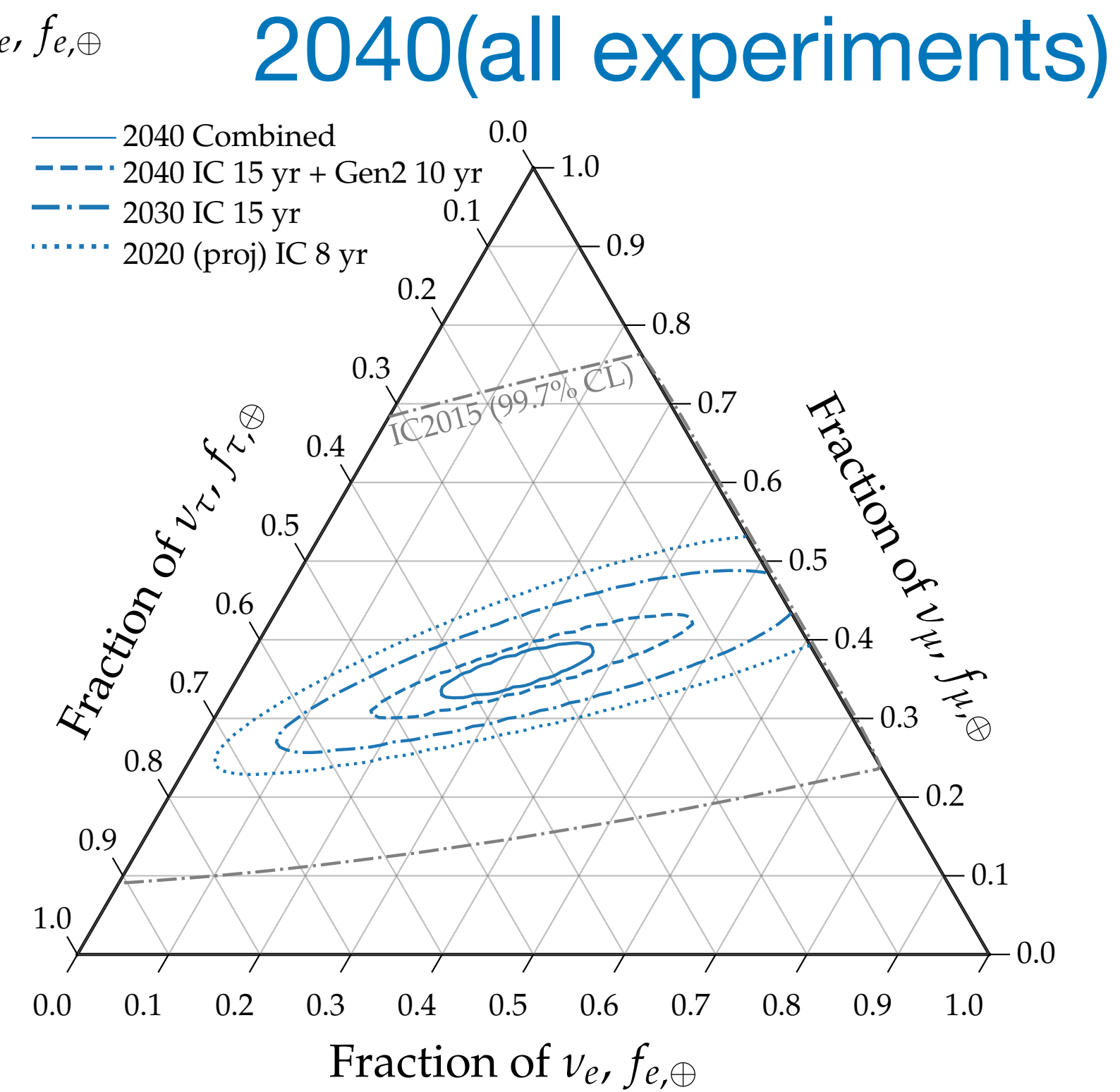
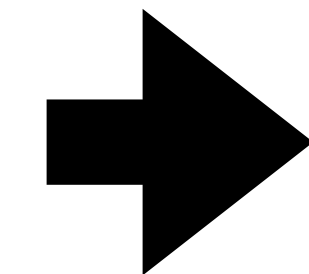
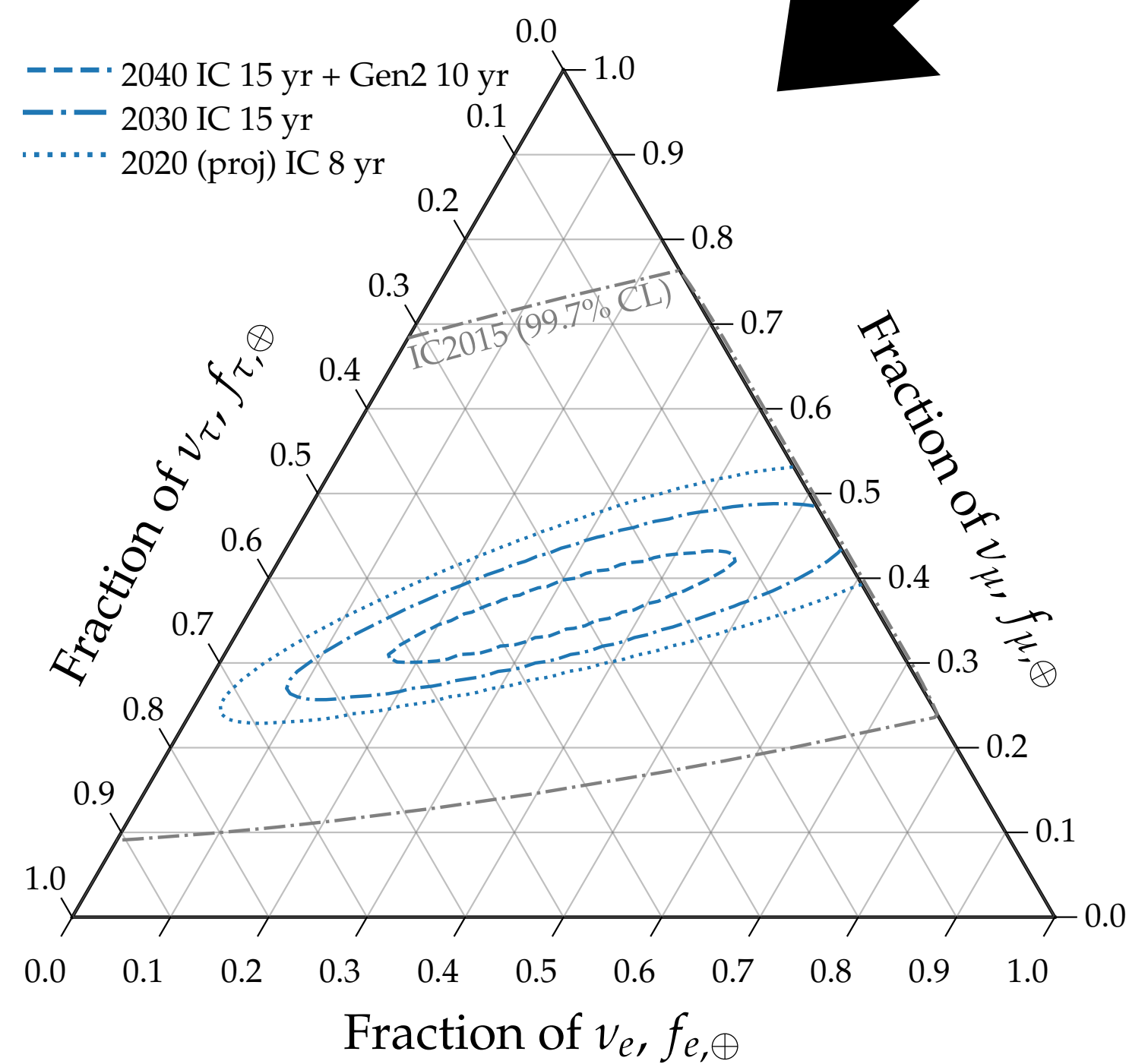


Telescope	Medium	Location	Exposure (km <sup>3</sup> )
<b>IceCube-Gen2</b>	Ice	South pole (HE upgrade of IceCube)	~6-9
<b>KM3NeT</b>	Seawater	Mediterranean Sea (successor to ANTARES)	~2-3
<b>GVD</b>	Freshwater	Lake Baikal	1.5
<b>P-ONE</b>	Seawater	Cascadia Basin (Pacific Ocean)	$\pi$
<b>TAMBO</b>	Rock/air/water Cherenkov	Peru	~10 (very high E, tau only)

# Statistics

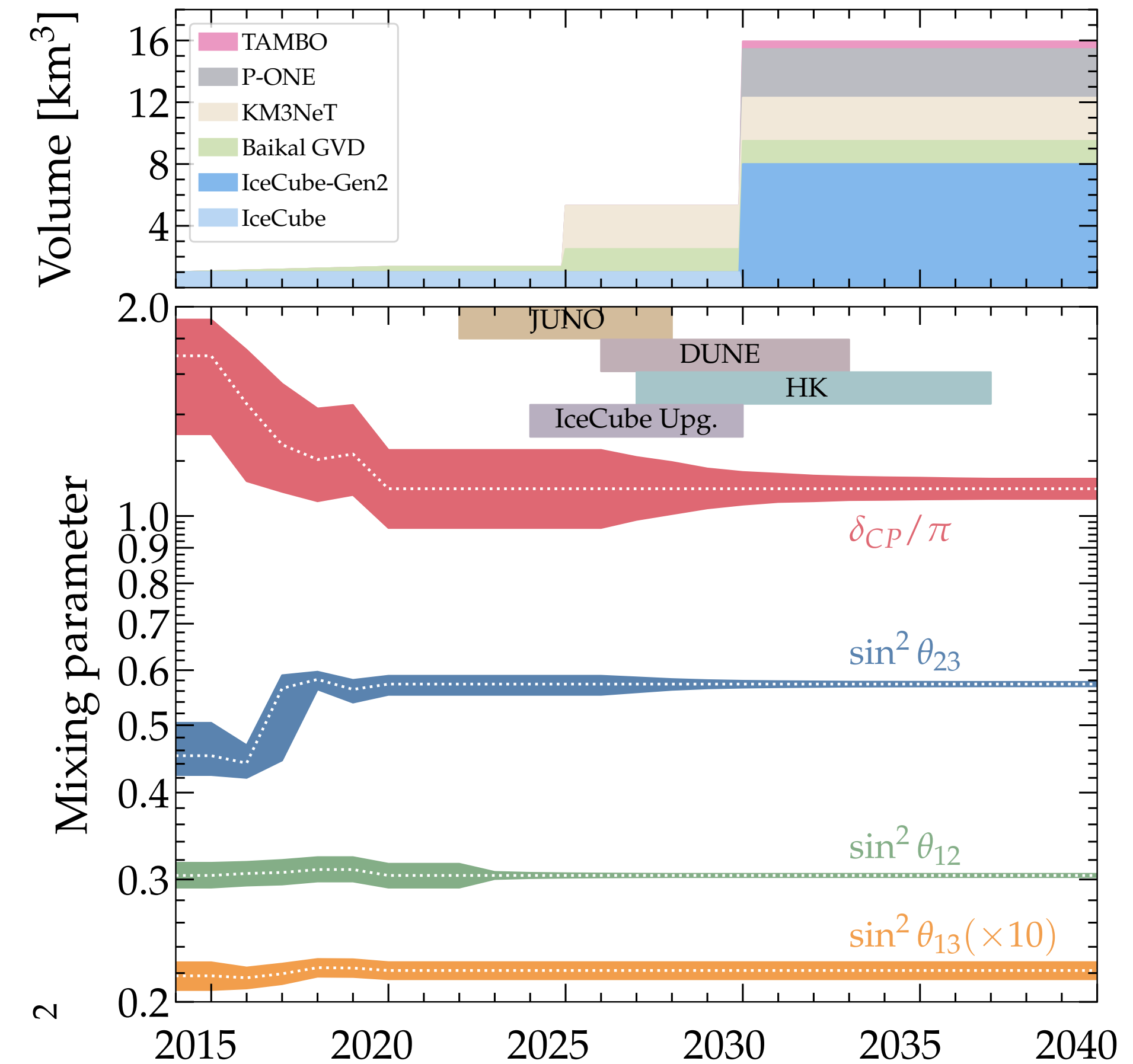
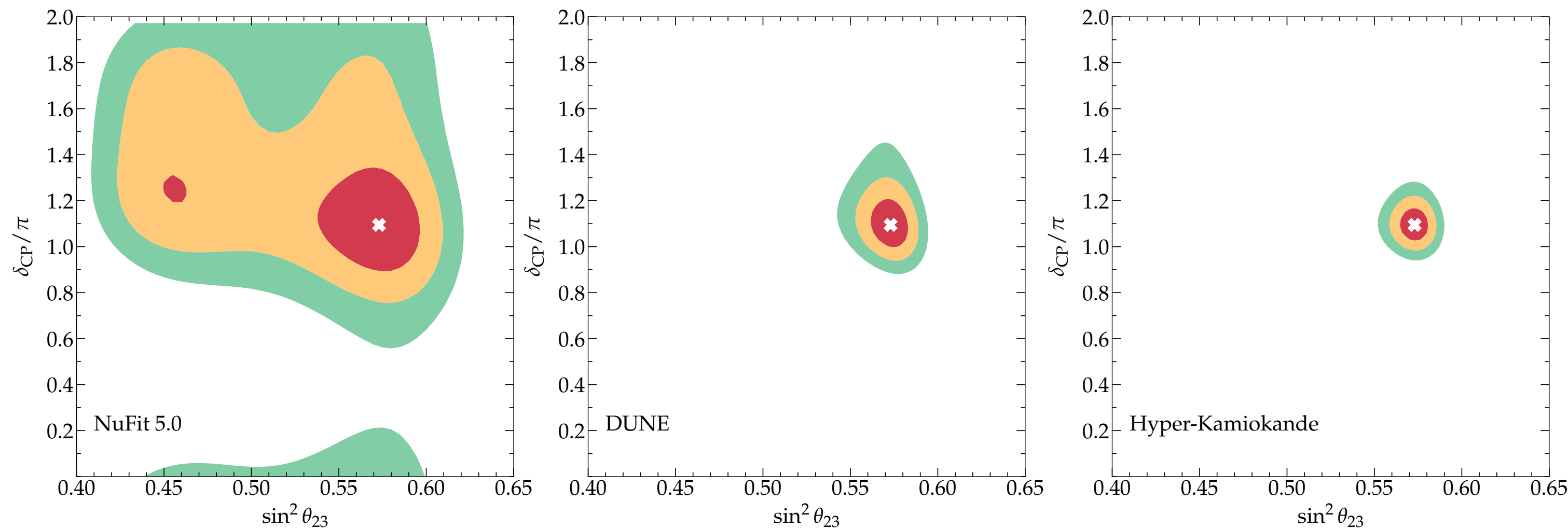


**2040 (IceCube-Gen2)**



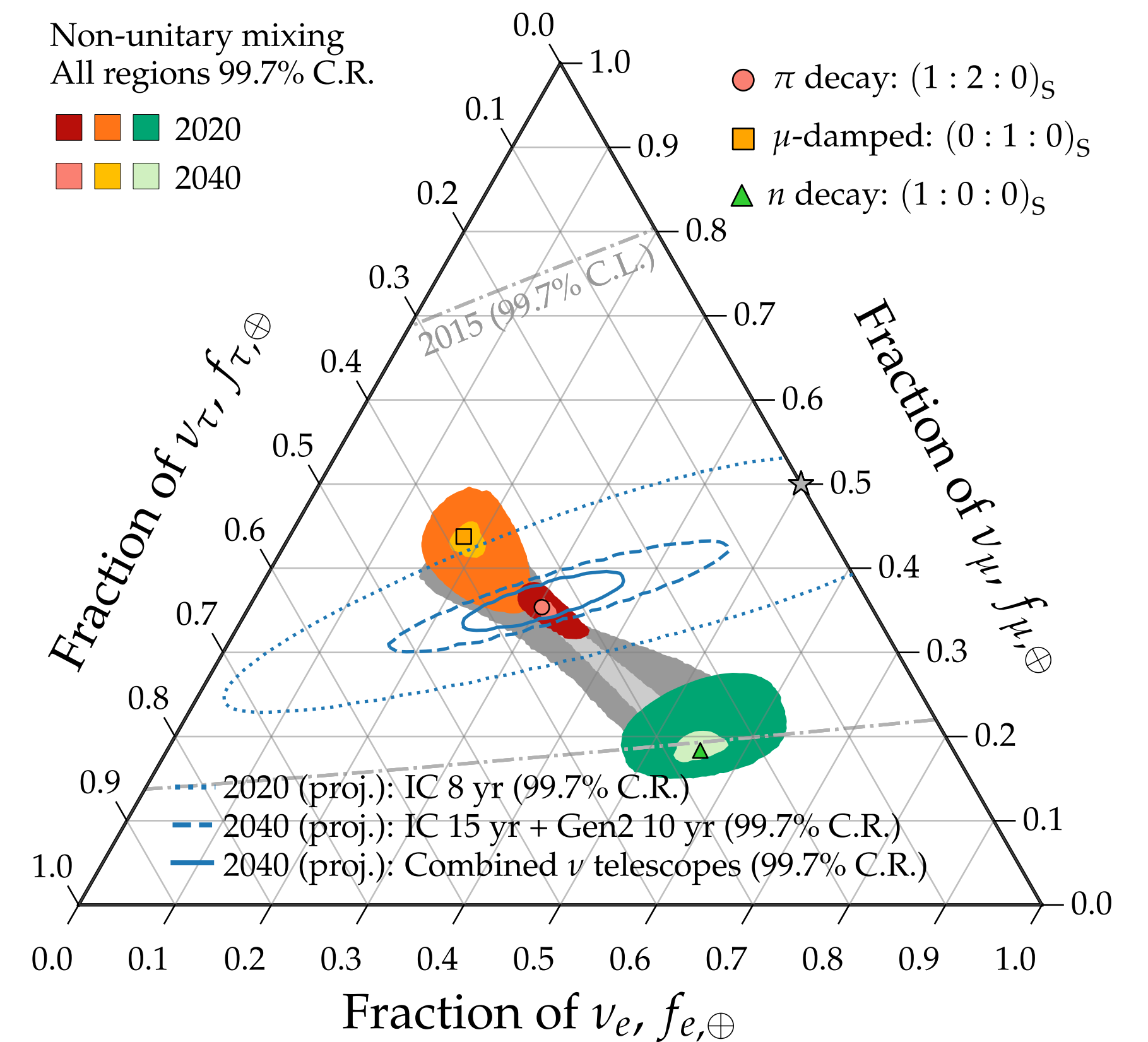
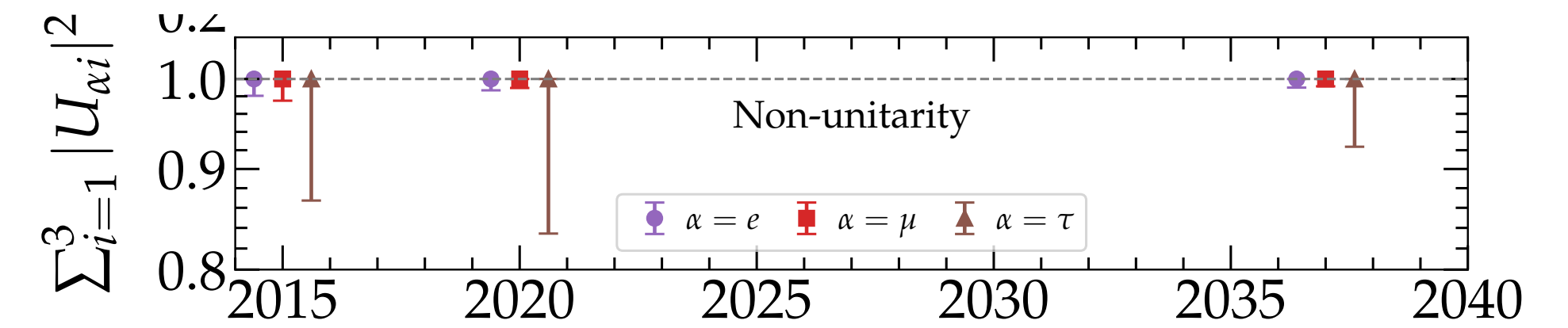
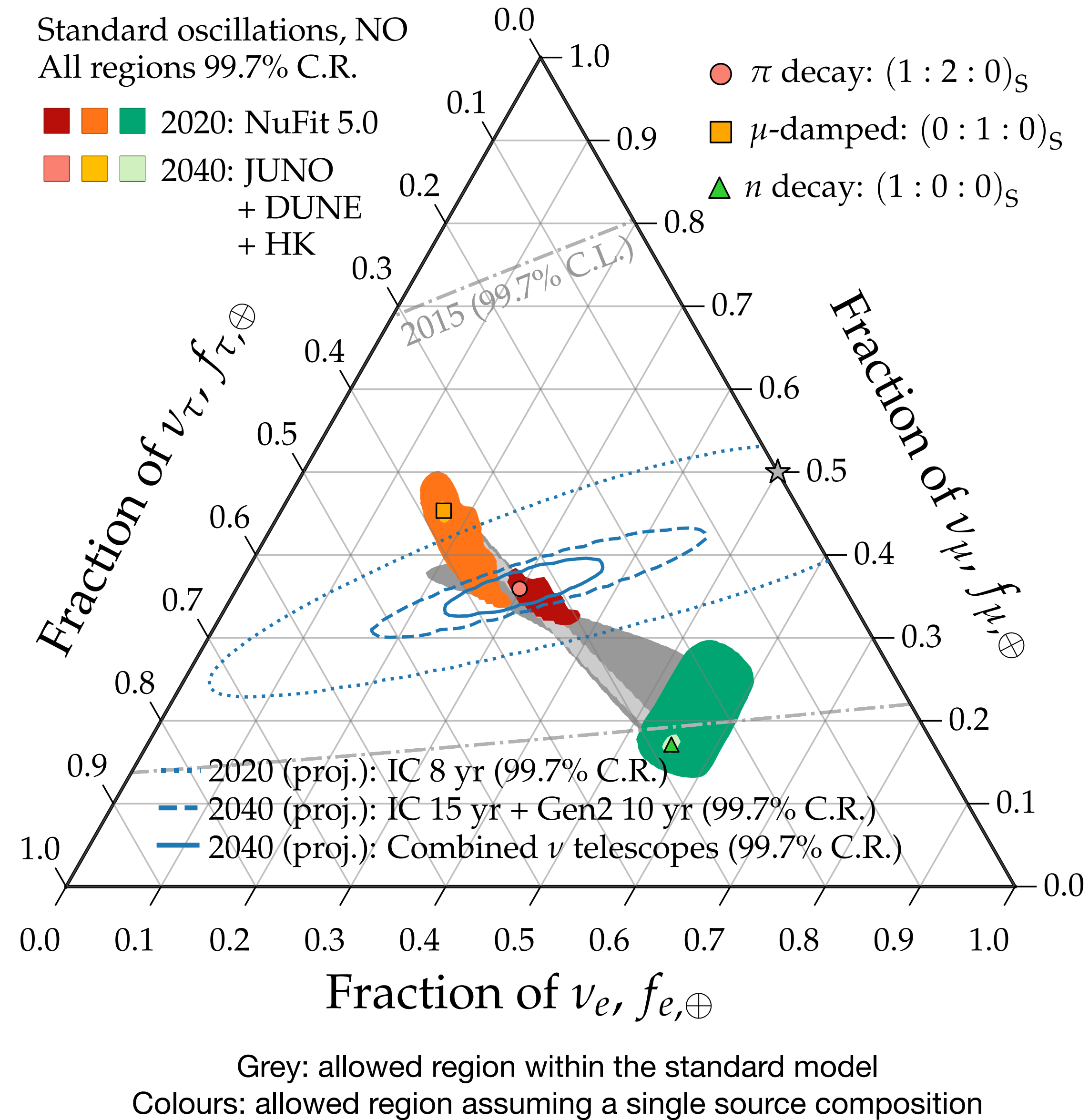
# Systematics: terrestrial experiments

- JUNO (Jiangmeng): 2022-2028: 20kt liquid scintillator reactor measurement. 0.52% uncertainty on  $\sin^2 \theta_{12}$
- DUNE (US): ~2026-2033: 40kt liquid argon long baseline experiment.  $\theta_{23}$  &  $\delta_{CP}$
- Hyper-Kamiokande: 187 kt water Cherenkov.  $\theta_{23}$  &  $\delta_{CP}$
- IceCube Upgrade: dense instrumentation: constrain unitarity



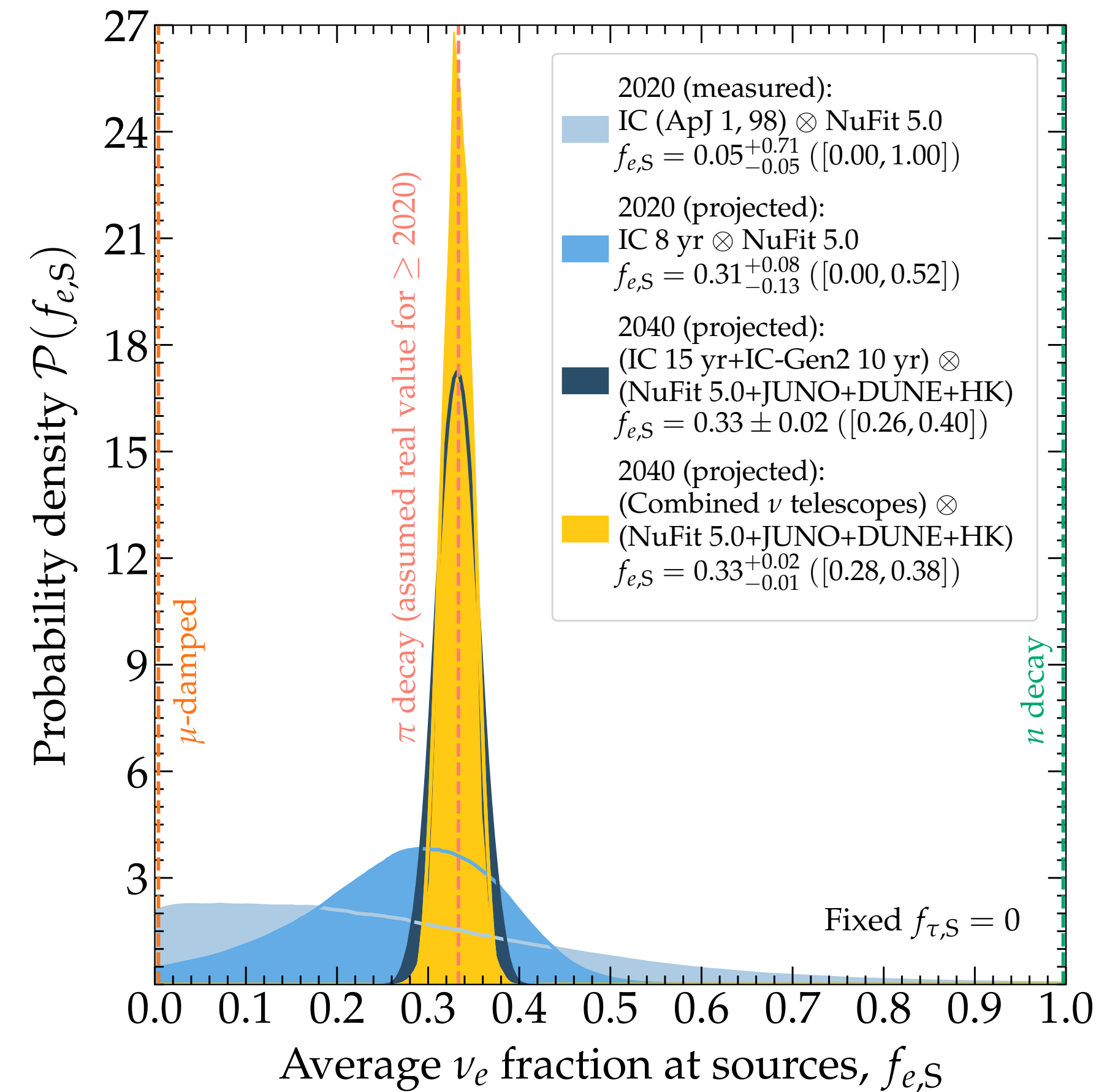
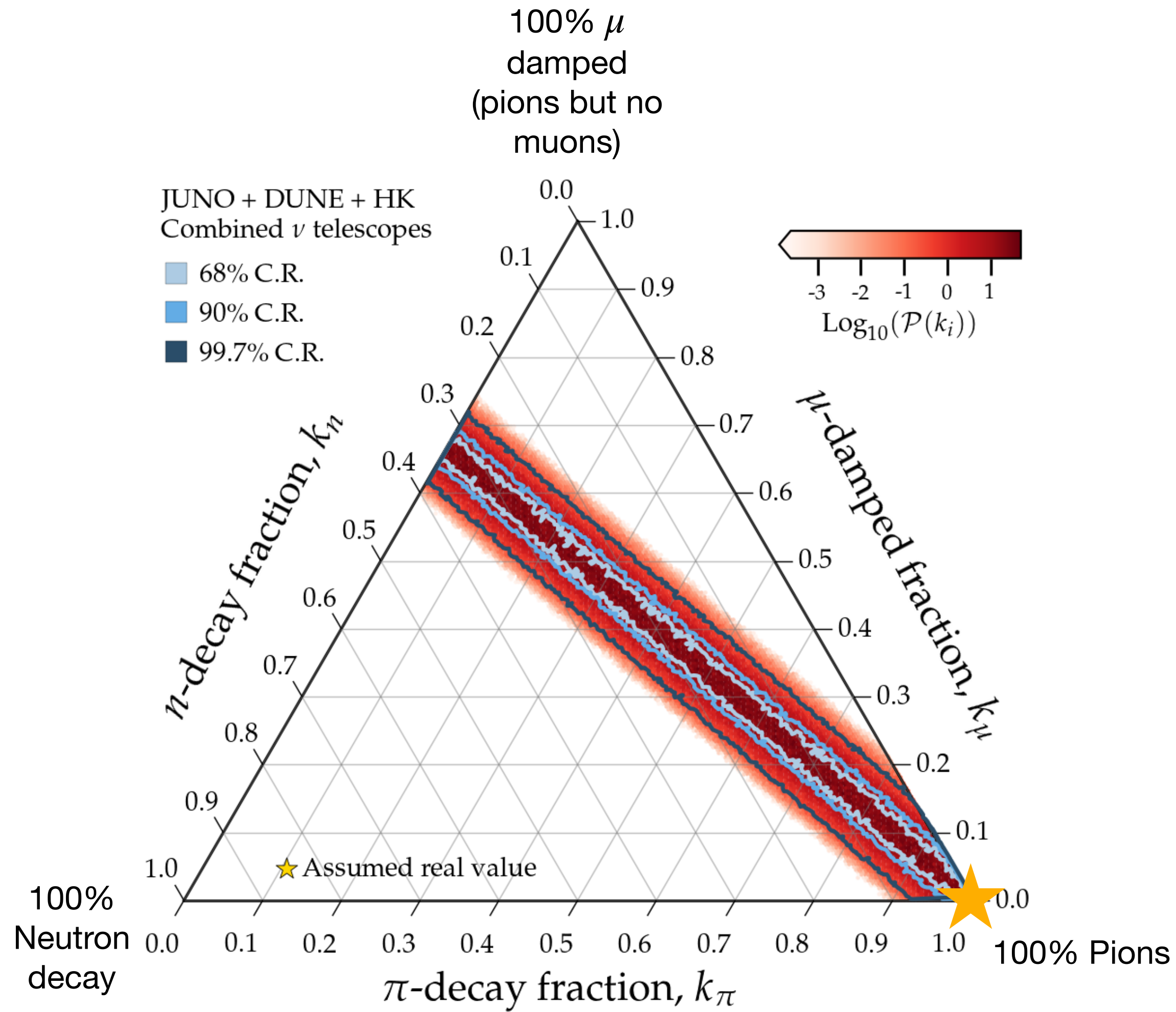
$$|\nu_\alpha\rangle = \frac{1}{\sqrt{N_\alpha}} \sum_{i=1}^3 U_{\alpha i}^* |\nu_i\rangle$$

## Without assuming unitary 3x3 PMNS matrix?





# Flavour composition at the source?

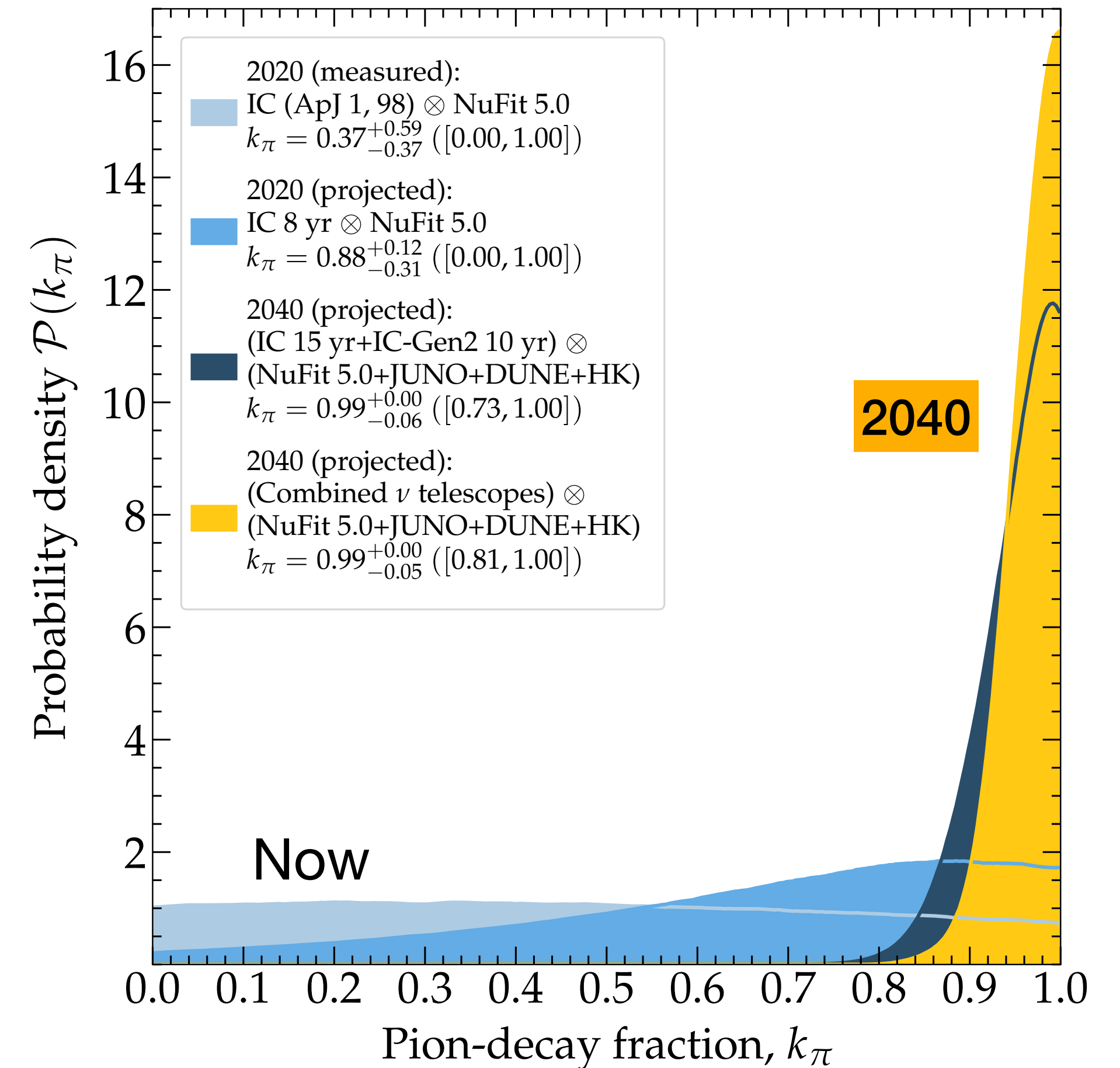


# Flavour composition at the source



Dominant production mechanism can be pinned down to within 20% *using neutrino flavour alone.*

Assuming no neutron decay



# New physics: neutrino decay

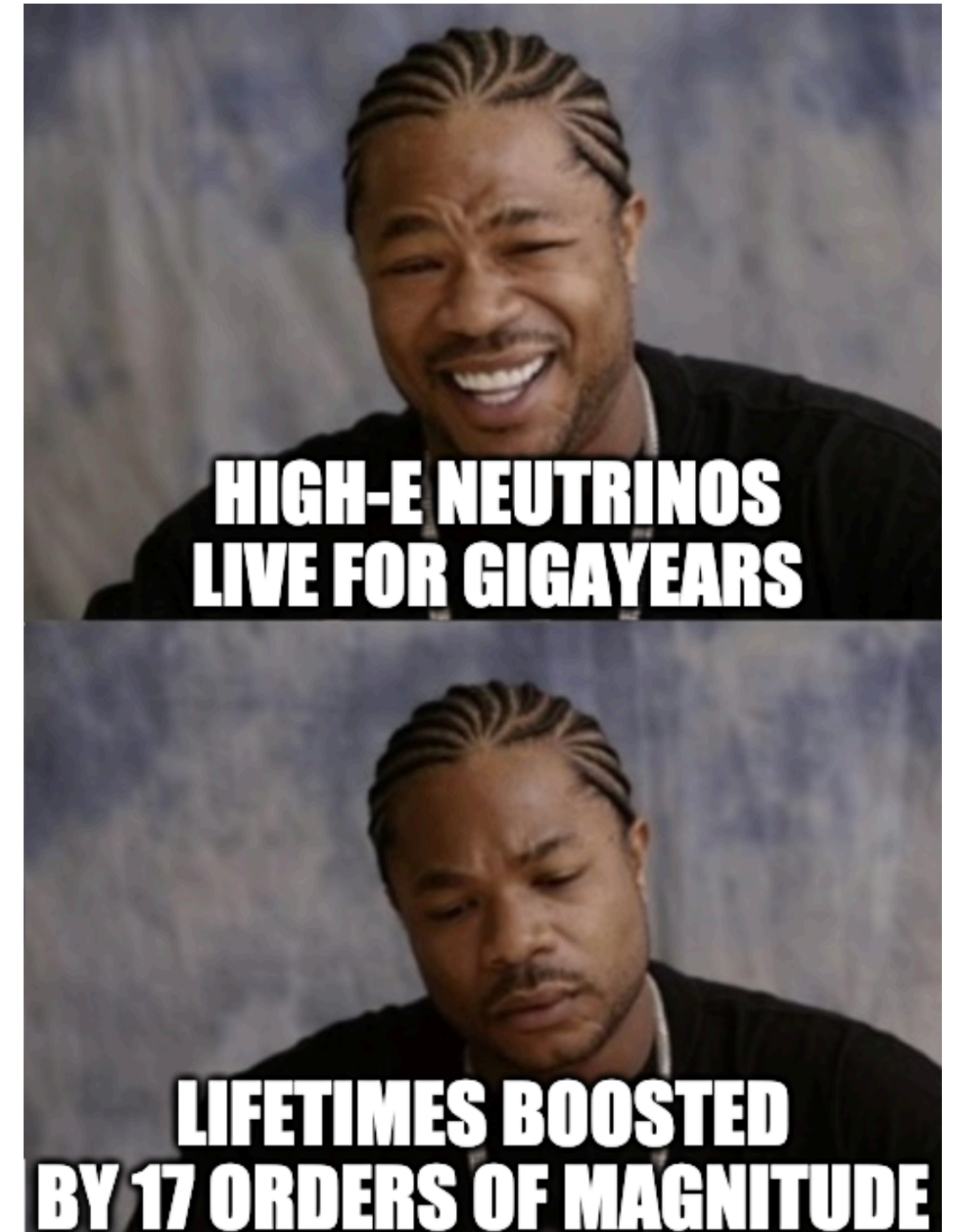
# Neutrino decay

Invisible decay: all but one mass eigenstate decays to invisible species.

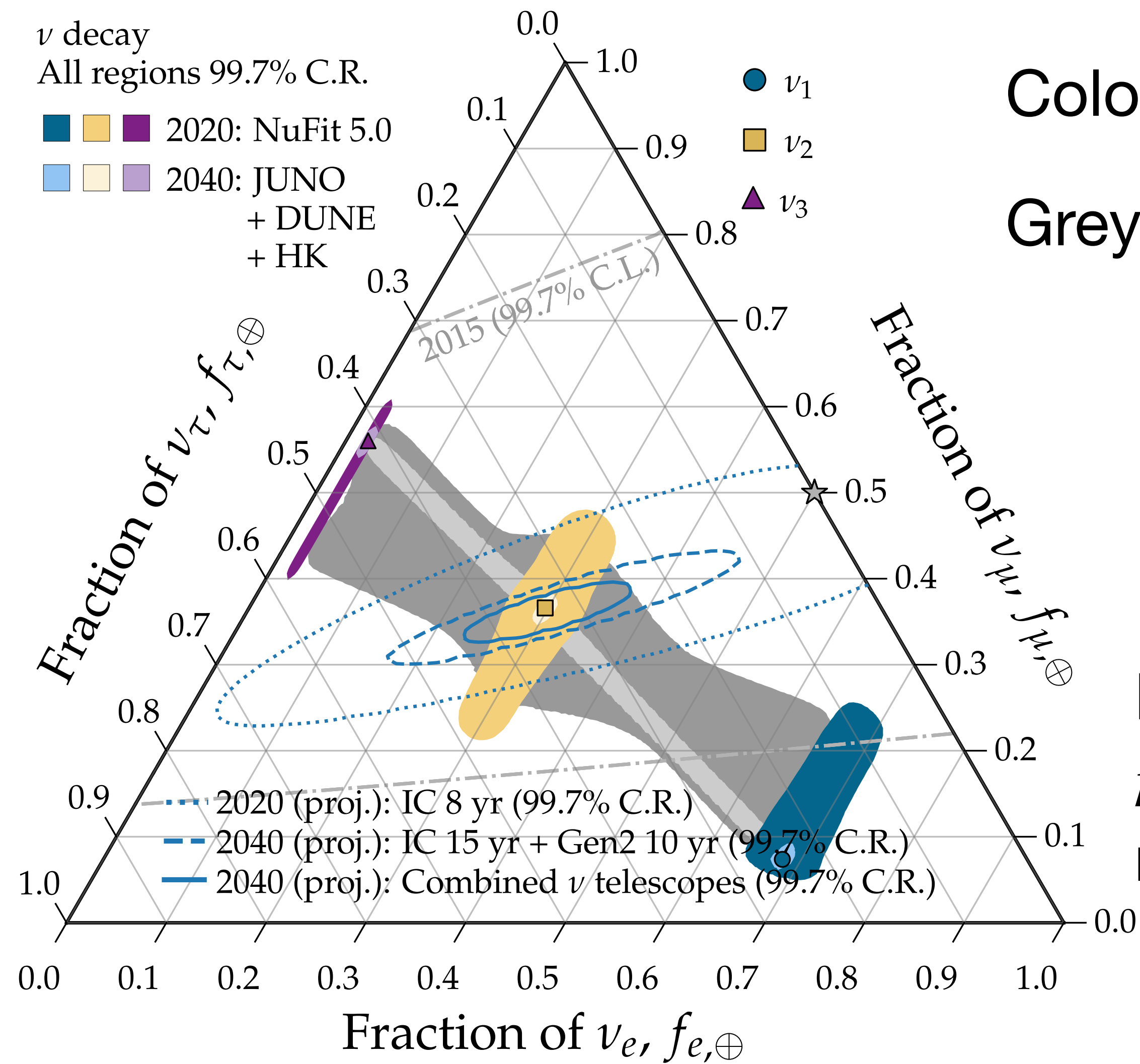
$$N_\nu = N(z_0) \exp \left\{ - \frac{m_\nu}{\tau E_\nu} \int_0^{z_0} \frac{dz}{(1+z)^2 H_0 \sqrt{\Omega(z)}} \right\}$$

↑  
neutrino lifetime at rest

Must be integrated over distribution of cosmic sources

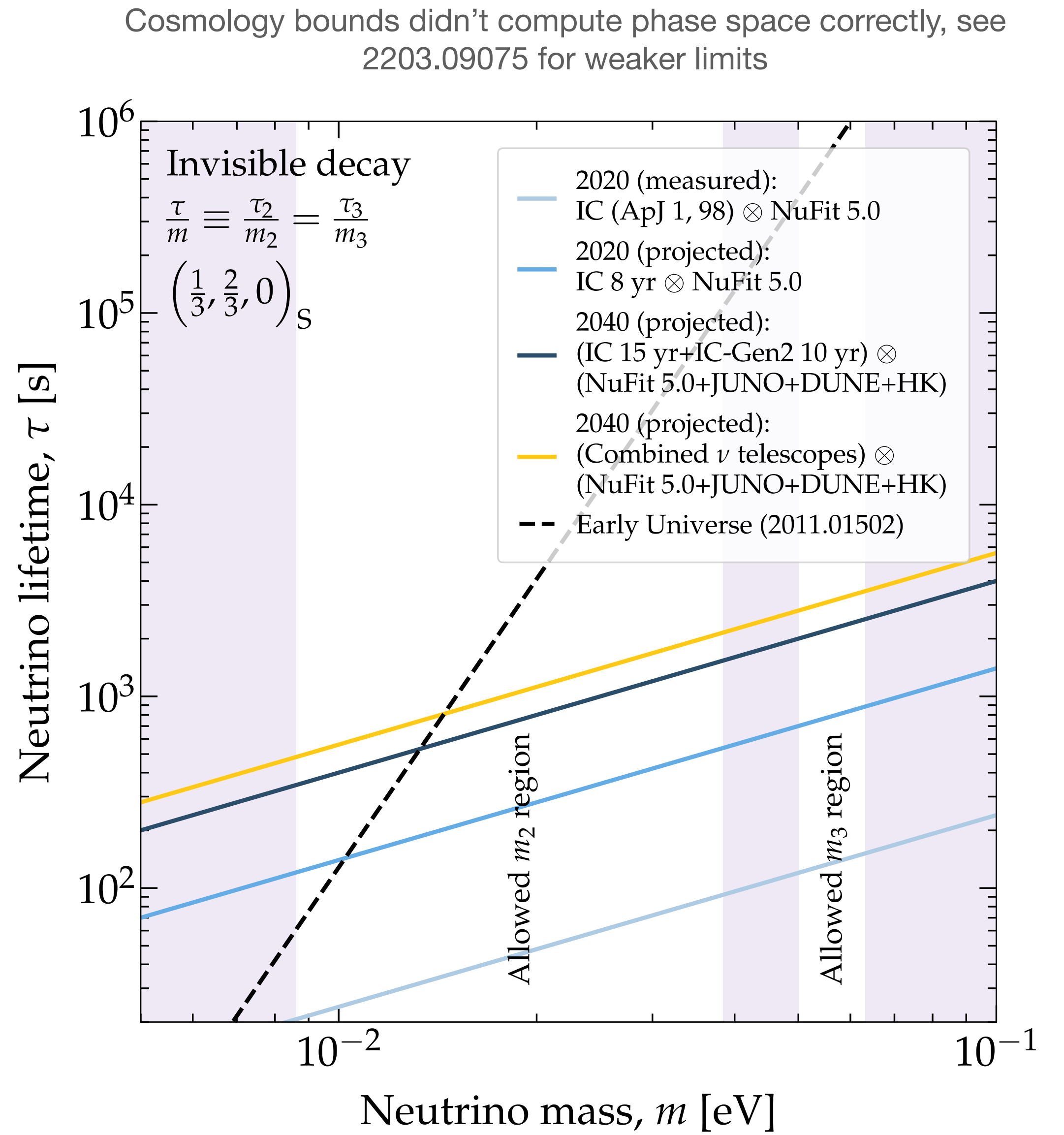
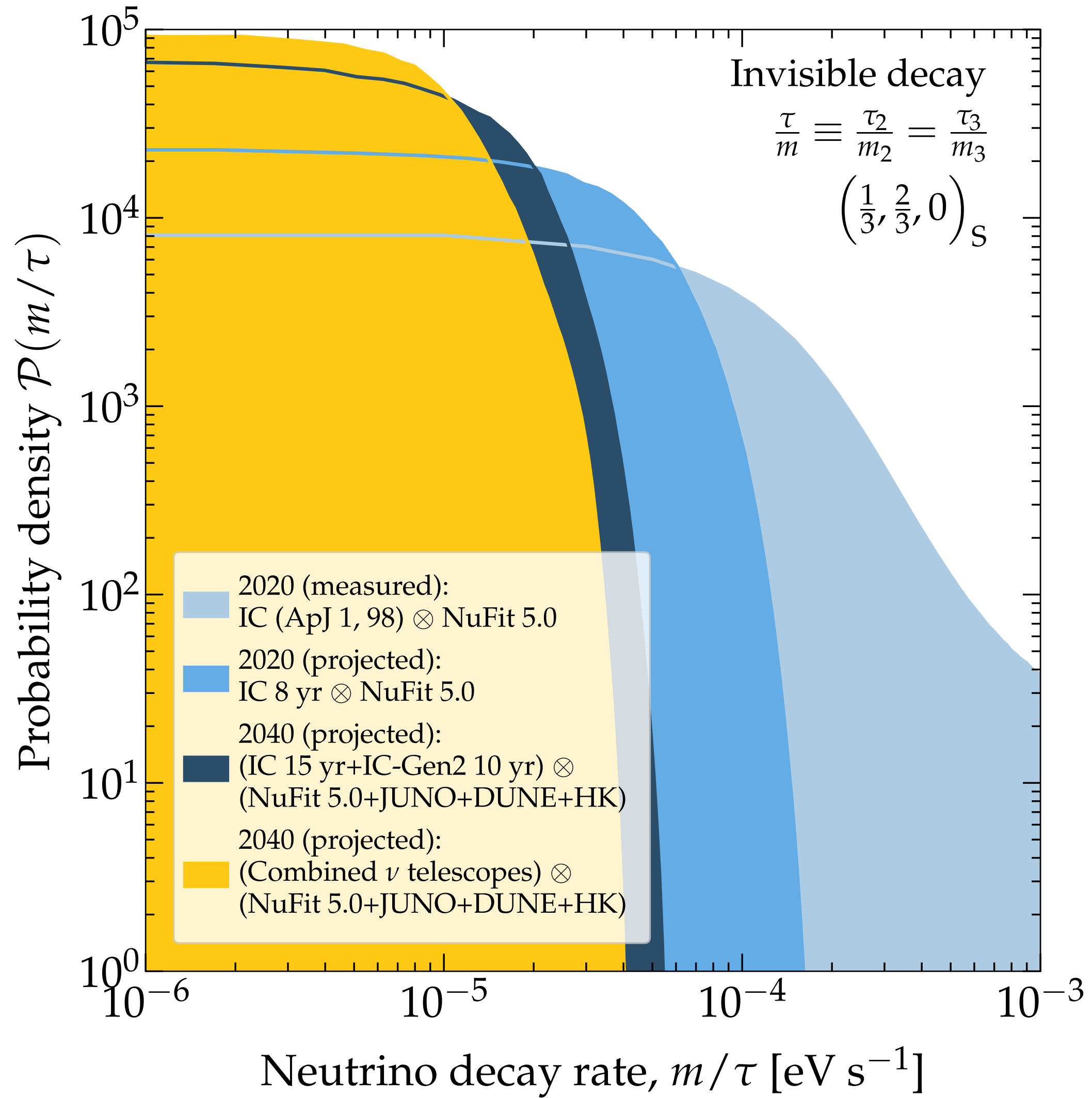


See Abdullah & Denton 2005.07200 for a complete treatment of *visible* decay



Full decay of  $m_2$  and  $m_3$  almost excluded now

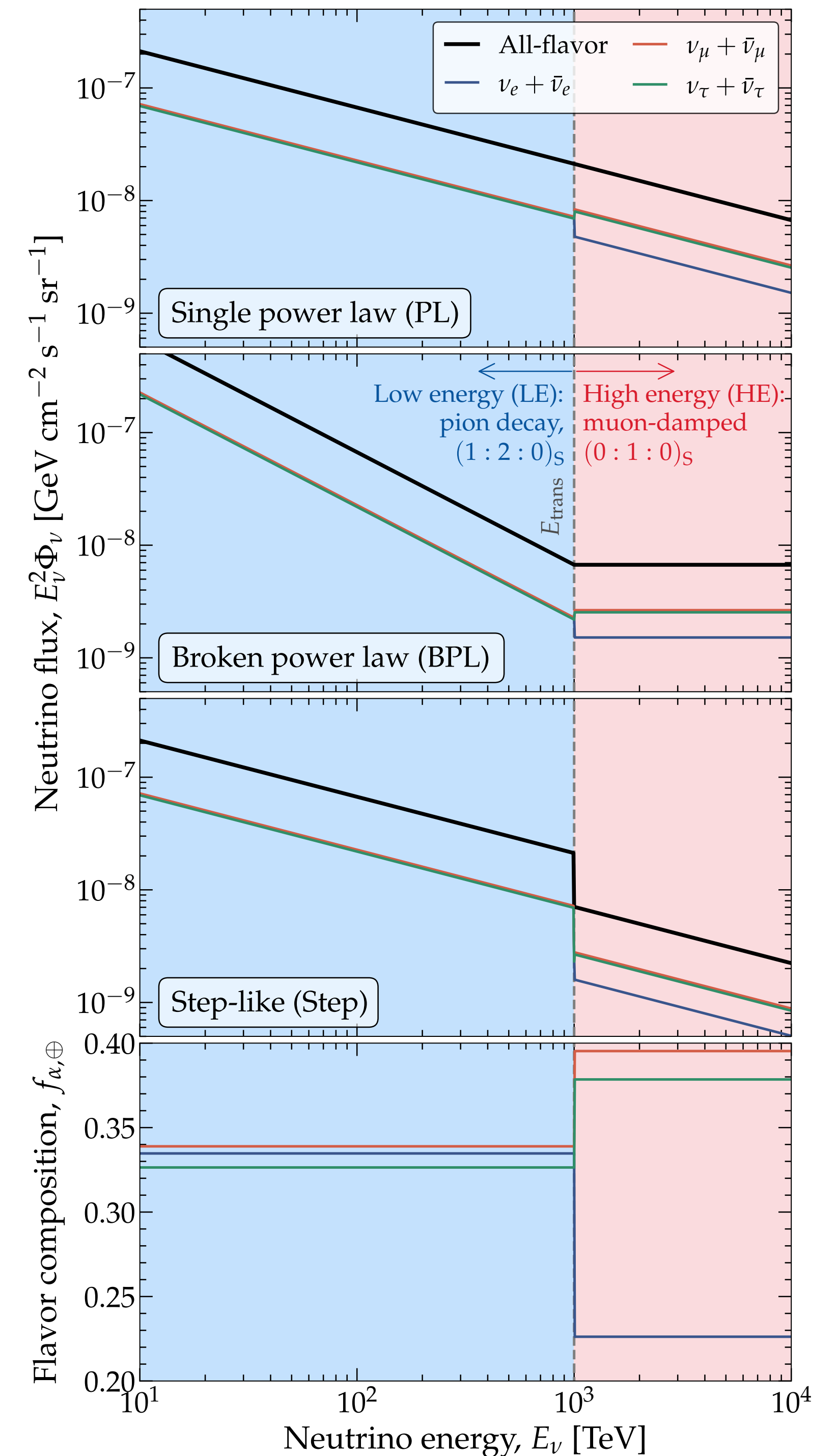
# Sensitivity to single mass eigenstates



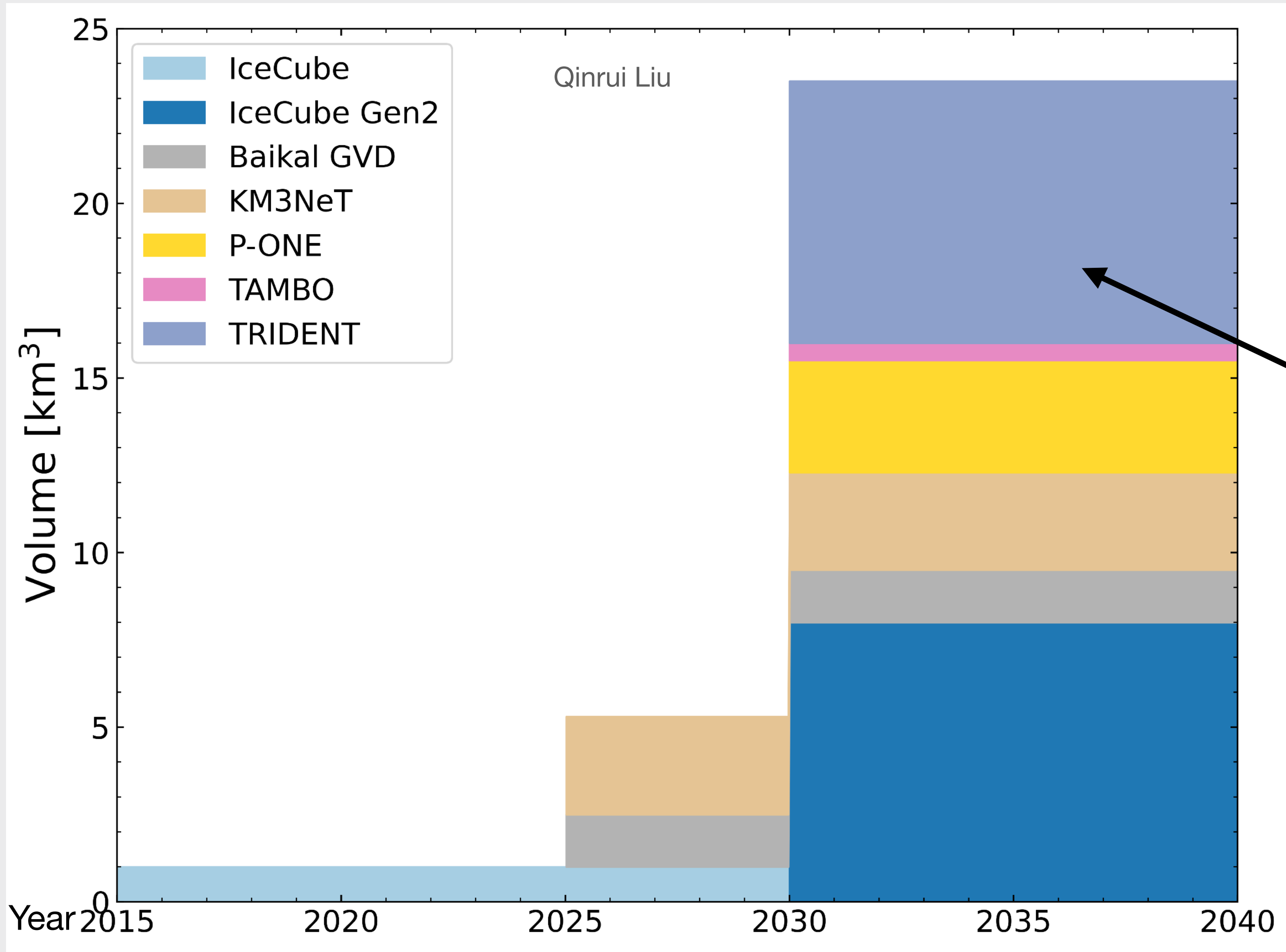
**But these don't include energy  
dependence**

# The flavour composition can depend on energy

- Muon-damping: we see the neutrinos from the pion at high-energy, and from the muon at lower energy
- Neutrino decay, Lorentz-invariance violation can give an E-dependent step
- Different sources could dominate at different energy ranges
- We test three generic **benchmark scenarios**:
  - **Single power law with a flavour transition**
  - **Broken power law, transition at the break**
  - **Step, transition at the step**







We've added TRIDENT to the mix

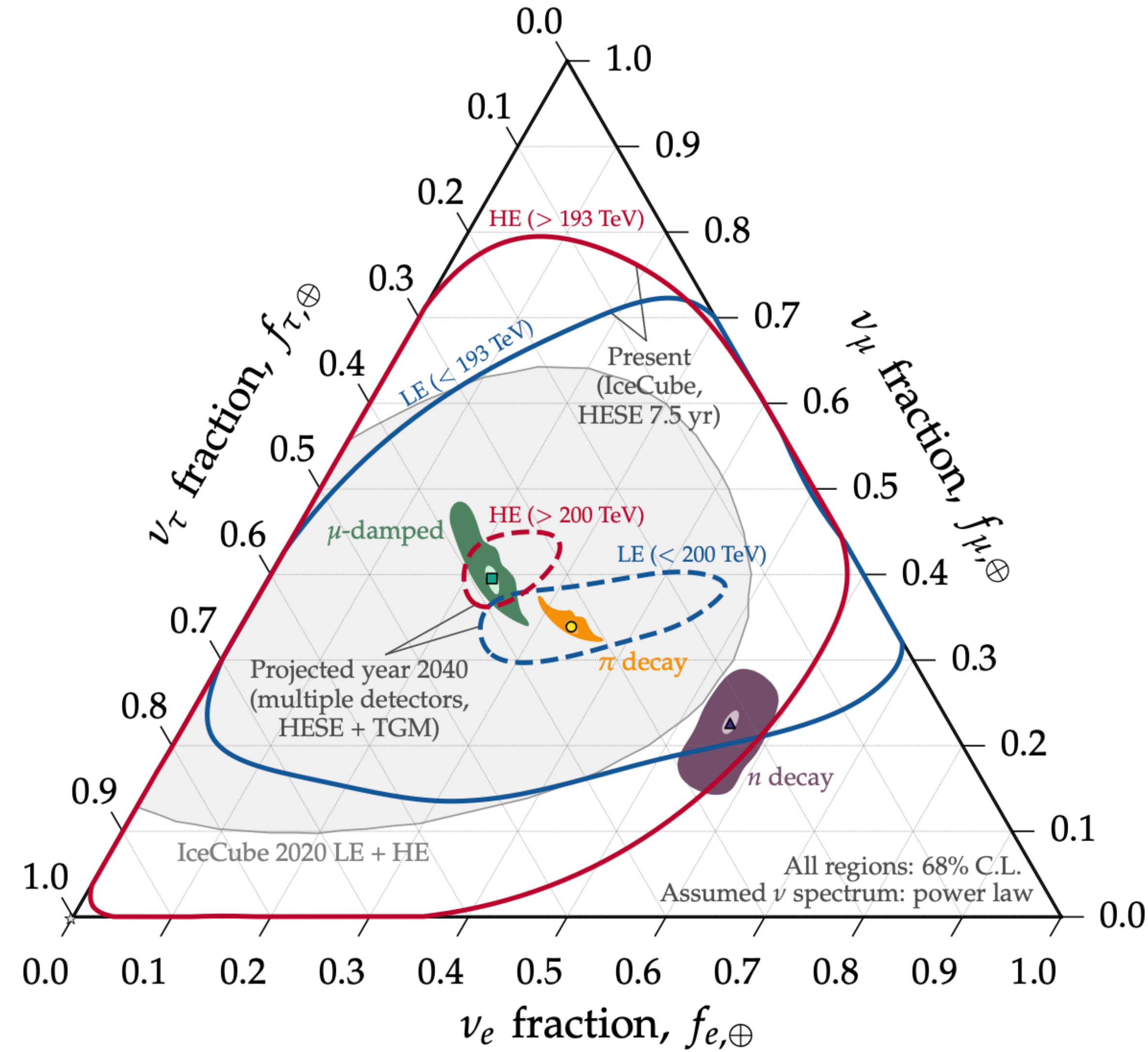
**More telescopes with larger exposure!  
Combine the exposure to reach the optimal sensitivity.**

Parameter	Symbol	Units	Used in flux model			True value (in proj.) <sup>a</sup>	Prior
			PL	BPL	Step		
Spectrum shape parameters (Section IID)							
All-flavor flux normalization at 100 TeV, common to LE and HE	$\Phi_{\nu,0}$	$10^{-18} \text{ GeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$	✓	✓		6.7	Uniform $\in [0, 10]$
LE all-flavor flux normalization at 100 TeV	$\Phi_{\nu,0}^{\text{LE}}$	$10^{-18} \text{ GeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$			✓	6.7	Uniform $\in [0, 10]$
HE all-flavor flux normalization at 100 TeV	$\Phi_{\nu,0}^{\text{HE}}$	$10^{-18} \text{ GeV}^{-1} \text{ cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$			✓	(6.7/3)	Uniform $\in [0, 10]$
Energy of flavor transition, LE to HE	$E_{\text{trans}}$	TeV	✓	✓	✓	200 or $10^3$	Log <sub>10</sub> -uniform $\in [60, 10^4]$
Spectral index, common to LE and HE	$\gamma$	...	✓		✓	2.5	Uniform $\in [1, 4]$
LE spectral index	$\gamma^{\text{LE}}$	...		✓		3.0	Uniform $\in [1, 4]$
HE spectral index	$\gamma^{\text{HE}}$	...		✓		2.0	Uniform $\in [1, 4]$
Additional parameters used when measuring the flavor composition at Earth (Section IV A)							
LE angle of flavor composition at Earth	$\sin^4 \theta_{\oplus}^{\text{LE}}$	...	✓	✓	✓	0.45	Uniform $\in [0, 1]$
LE angle of flavor composition at Earth	$\cos 2\psi_{\oplus}^{\text{LE}}$	...	✓	✓	✓	-0.01	Uniform $\in [-1, 1]$
HE angle of flavor composition at Earth	$\sin^4 \theta_{\oplus}^{\text{HE}}$	...	✓	✓	✓	0.39	Uniform $\in [0, 1]$
HE angle of flavor composition at Earth	$\cos 2\psi_{\oplus}^{\text{HE}}$	...	✓	✓	✓	-0.27	Uniform $\in [-1, 1]$
Additional parameters used when inferring the flavor composition at the sources (Section IV B)							
LE electron flavor fraction	$f_{e,\oplus}^{\text{LE}}$	...	✓	✓	✓	0.33	Uniform $\in [0, 1]$
HE electron flavor fraction	$f_{e,\oplus}^{\text{HE}}$	...	✓	✓	✓	0.23	Uniform $\in [0, 1]$
Solar mixing angle	$\sin^2 \theta_{12}$	...	✓	✓	✓	0.304	Present <sup>b</sup> : $0.304 \pm 0.012$ Proj. <sup>c</sup> : Normal, $\sigma = 0.002$
Atmospheric	$\sin^2 \theta_{23}$	...	✓	✓	✓	0.450	Present <sup>??</sup> : $0.450_{-0.019}^{+0.016}$ Proj. <sup>??</sup> : Normal, $\sigma = 0.004$
Reactor mixing angle	$\sin^2 \theta_{13}$	...	✓	✓	✓	0.304	Present <sup>??</sup> : $0.02246 \pm 0.00062$ Proj. <sup>??</sup> : Normal, $\sigma = 0.00062$
CP-violation phase	$\delta_{\text{CP}}$	°	✓	✓	✓	230	Present <sup>??</sup> : $230_{-36}^{+25}$ Proj. <sup>??</sup> : Normal, $\sigma = 6.687$



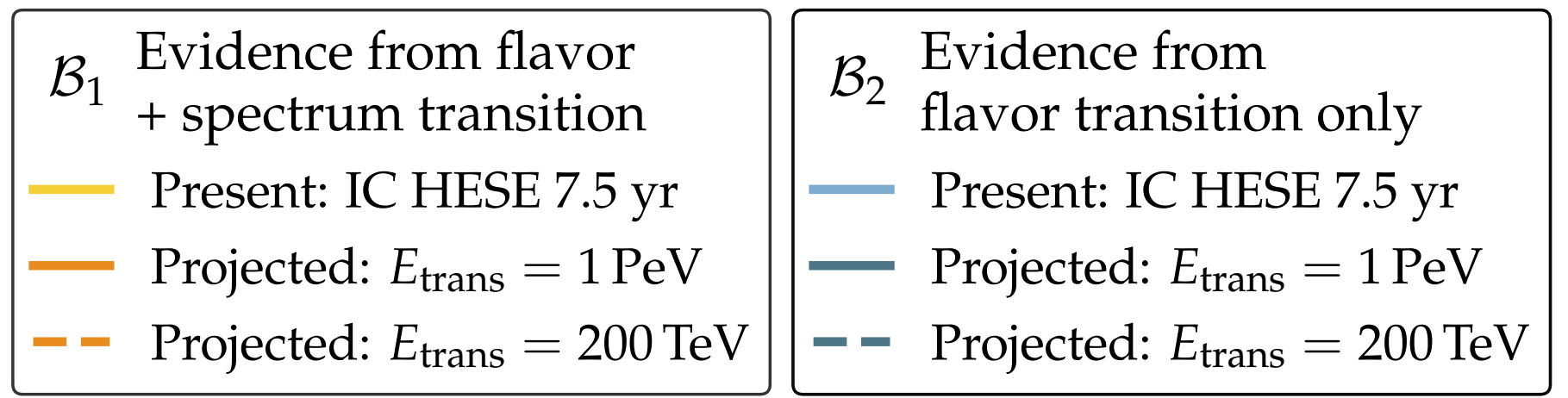
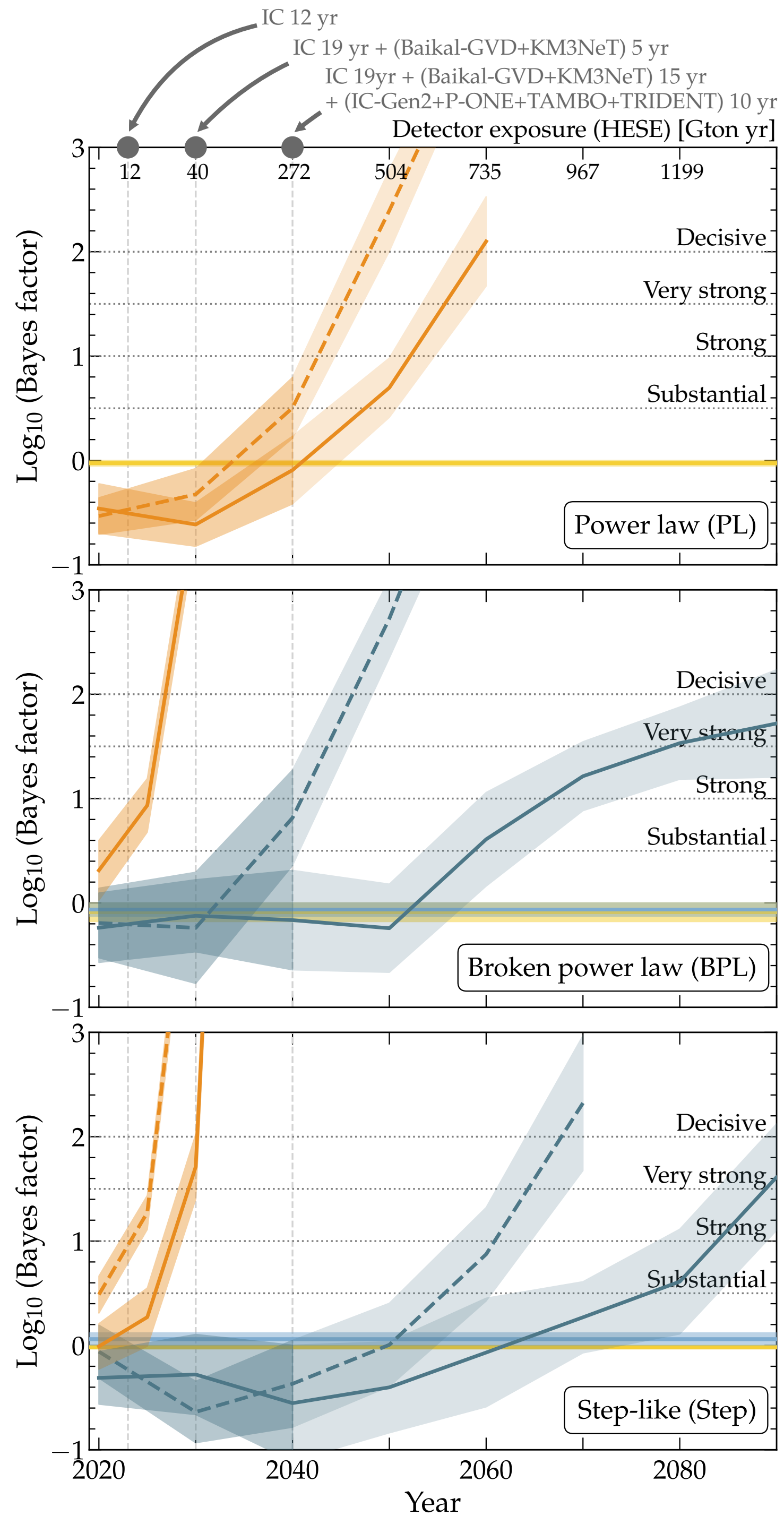
Very numbers

Much statistics



Future combined exposure:  
IceCube/IceCube-Gen2+KM3NeT+Baikal-GVD  
+P-ONE+TAMBO+TRIDENT

The HE flavor composition can be marginally distinguished from the LE composition at  $1\sigma$  level by 2040



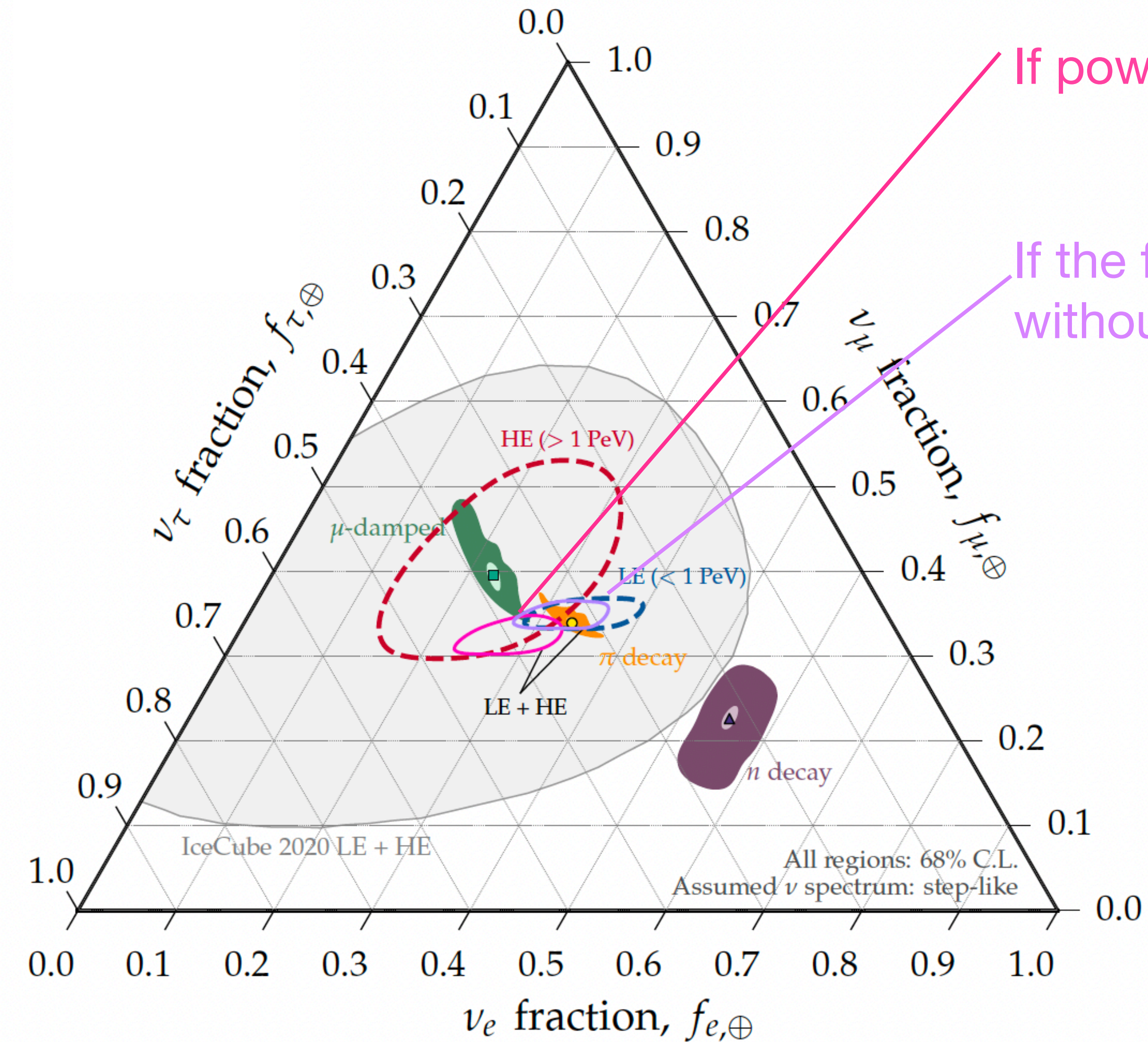
# Bayes factor

$Z_{\text{transition}}$

$Z_{\text{no transition}}$

- From Flavour + spectrum transition
- From Flavour transition only

# Comparison with the General Approach

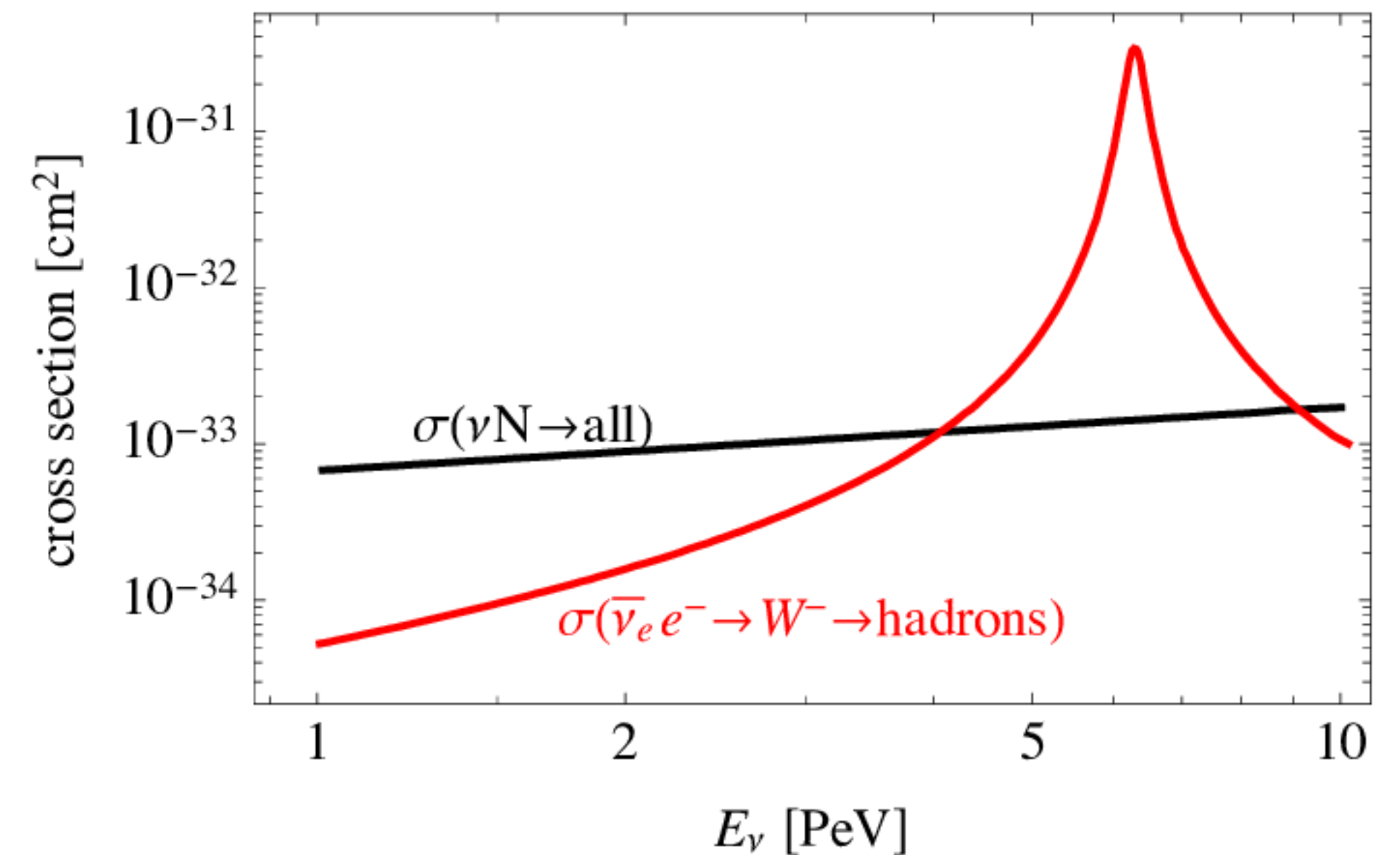
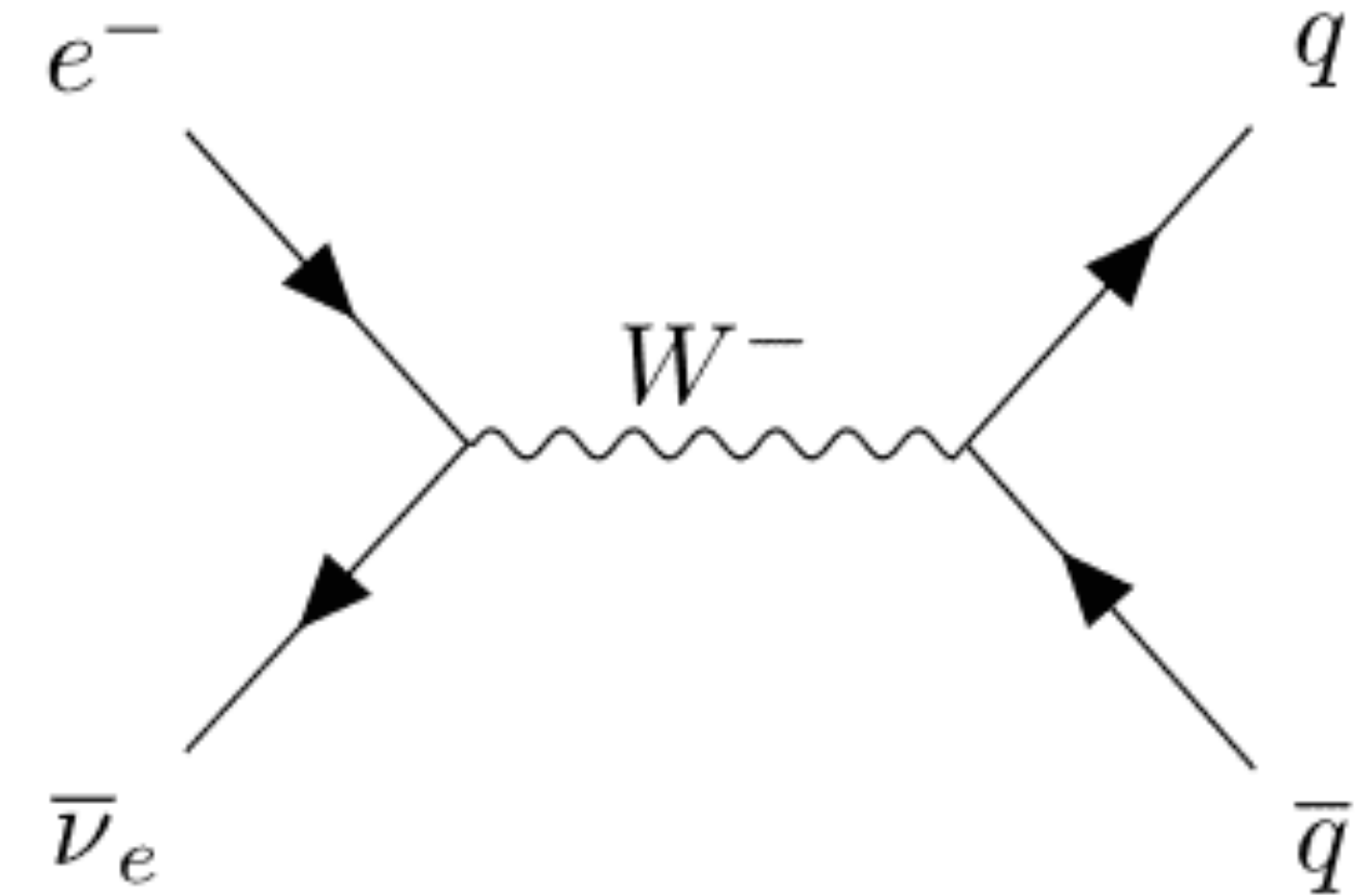


Assuming there is a flavor transition, if the measurement models that there is no flavor transition, more constrained contours can be obtained but no accurate detail is told.

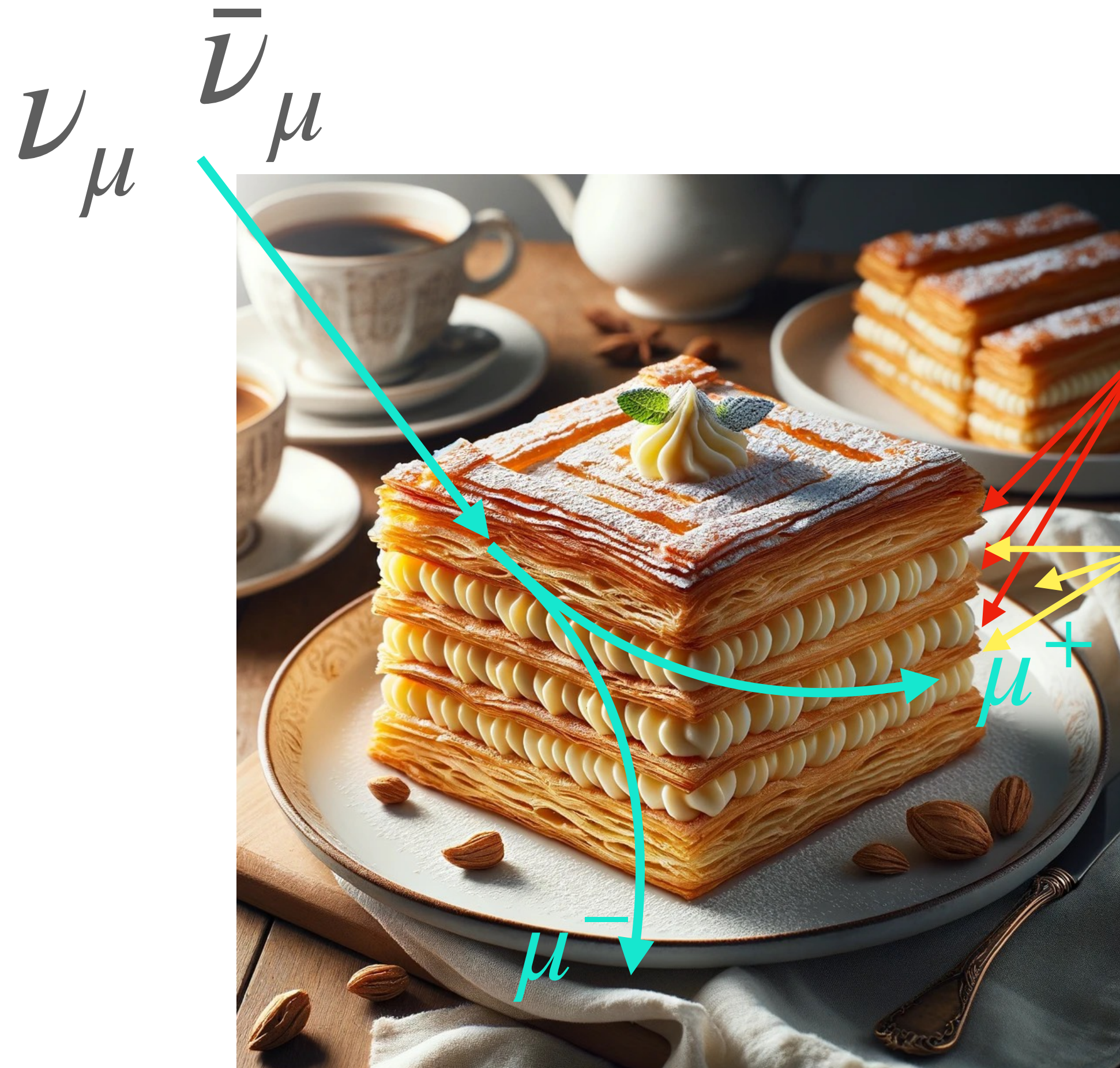
Flavor measurements must use flexible descriptions of the neutrino spectrum to avoid reporting inaccurate flavor composition measurements.

# Distinguishing $\nu$ vs $\bar{\nu}$ ?

- At high energies, neutrino/antineutrino separation is almost impossible
- Exception: the Glashow resonance.  
At  $E_{CM} = M_W$ , or  $E_\nu = 6.3$  PeV, can produce on-shell  $W$  for  $\bar{\nu}_e$  only.



# (Aside: India-based Neutrino Observatory proposal)



50,000 tons magnetized iron leaves

Resistive plate chambers

Currently stalled due to ecological concerns (blasting, excavation, ...)

# What does $\nu$ vs $\bar{\nu}$ do for you?

Are neutrinos coming from  $pp$  or  $p\gamma$  collisions? These give different  $\pi^+/\pi^-$  ratios

$$\{\nu_e, \bar{\nu}_e\} : \{\nu_\mu, \bar{\nu}_\mu\} : \{\nu_\tau, \bar{\nu}_\tau\}$$

$$p + p \rightarrow n_\pi [\pi^0 + \pi^+ + \pi^-]$$

$$p + \gamma \rightarrow \Delta^+ \rightarrow \pi^+ + n$$

Production	Source flavor ratio	Earth flavor ratio $\nu + \bar{\nu}$	Earth flavor ratio	$f_{\bar{\nu}_e}$
$pp$	$\{1, 1\} : \{2, 2\} : \{0, 0\}$	$0.33 : 0.34 : 0.33$	$\{0.17, 0.17\} : \{0.17, 0.17\} : \{0.16, 0.16\}$	0.17
$p\gamma$	$\{1, 0\} : \{1, 1\} : \{0, 0\}$	$0.33 : 0.34 : 0.33$	$\{0.26, 0.08\} : \{0.21, 0.13\} : \{0.20, 0.13\}$	0.08



# Event-Wise Identification

The case where Glashow resonant events can be identified on an event-by-event basis in the [4, 10] PeV deposited energy window. Only consider  $\bar{\nu}_e$  fraction.

$W^- \rightarrow \text{hadrons}$  BR ~67% ★

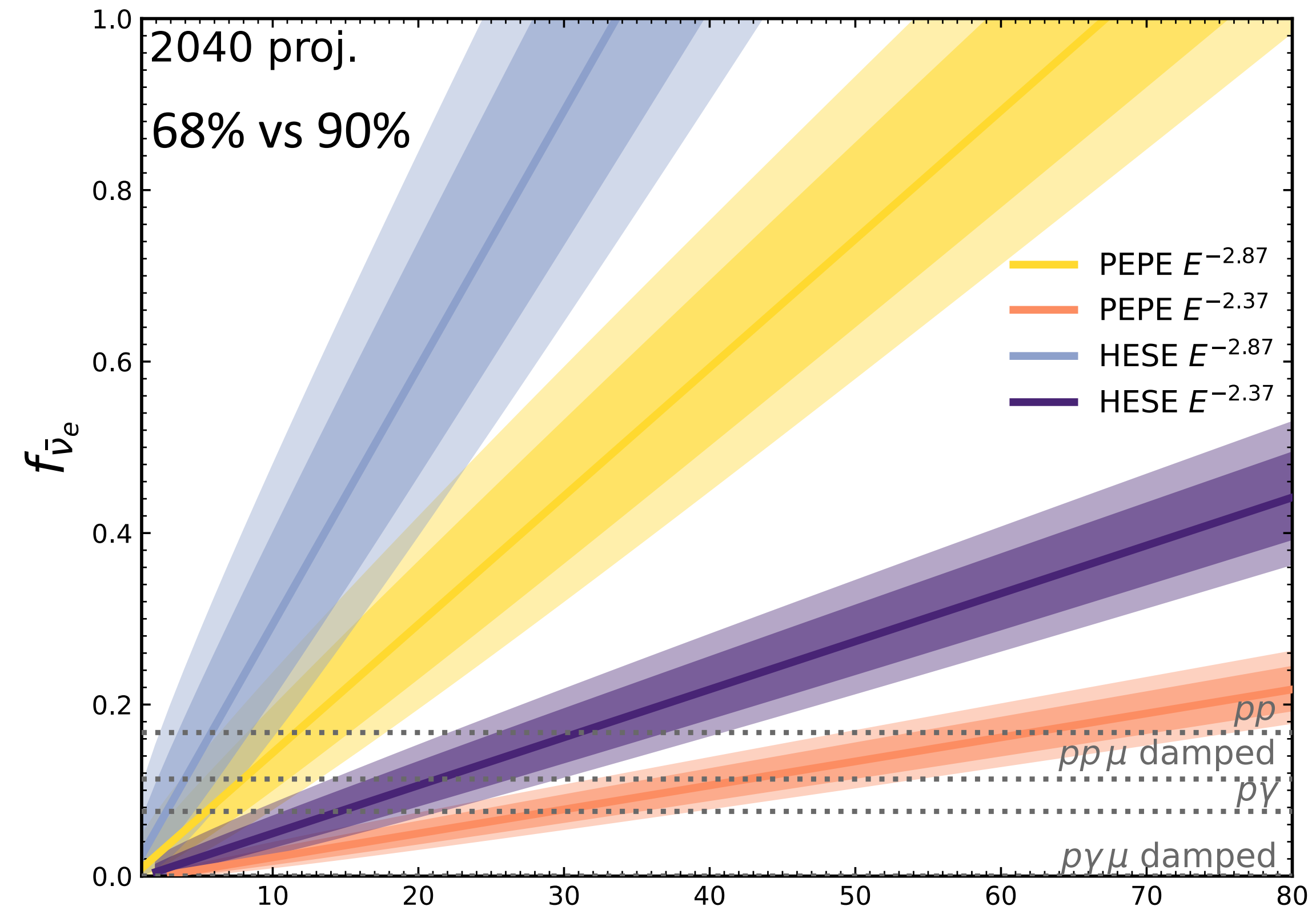
✓ escaping muons, the only irreducible background is from NCDIS events

$W^- \rightarrow e^- \bar{\nu}_e / \tau^- \bar{\nu}_\tau$  BR ~11%

✗ Undistinguishable to a DIS cascade

$W^- \rightarrow \mu^- \bar{\nu}_\mu$  BR ~11%

✓ track without the initial cascade comparing to  $\nu_\mu$  CCDIS



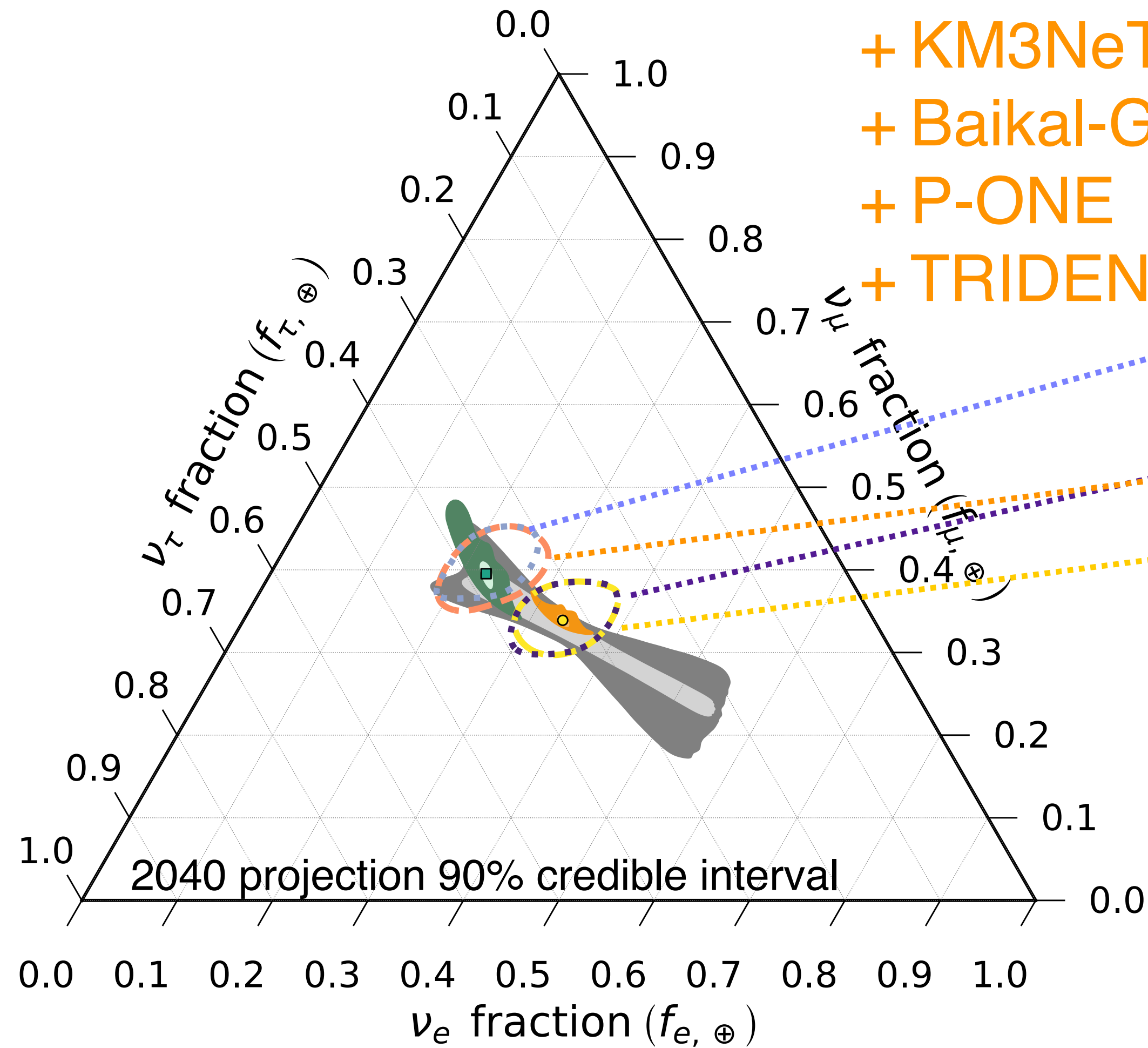
Number of Glashow resonant-like events observed

3-flavor degenerate scenarios can be distinguished at  $\gtrsim 2\sigma$  w/ the soft spectrum assumption and  $\sim 5\sigma$  w/ the hard spectrum assumption by 2040

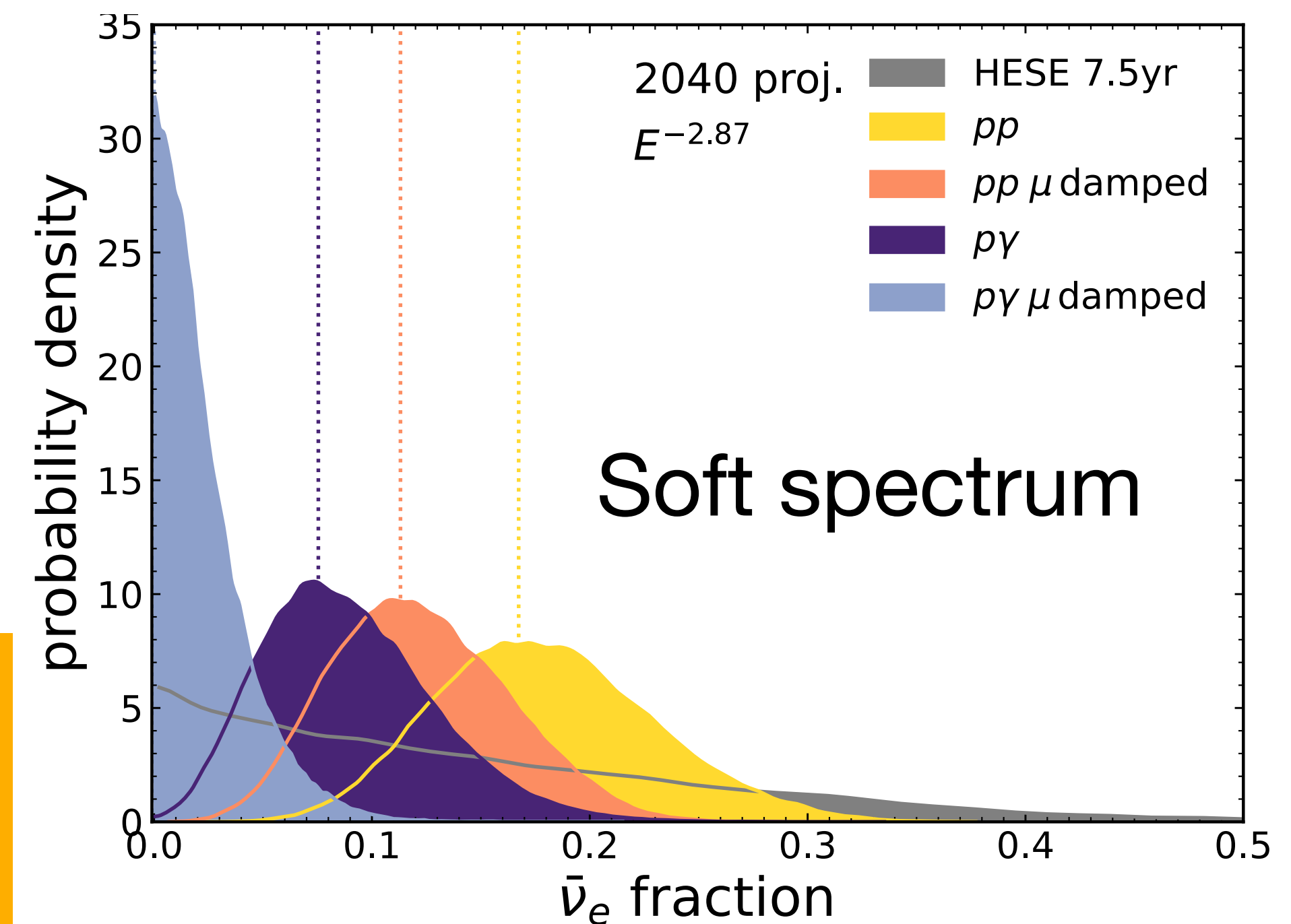
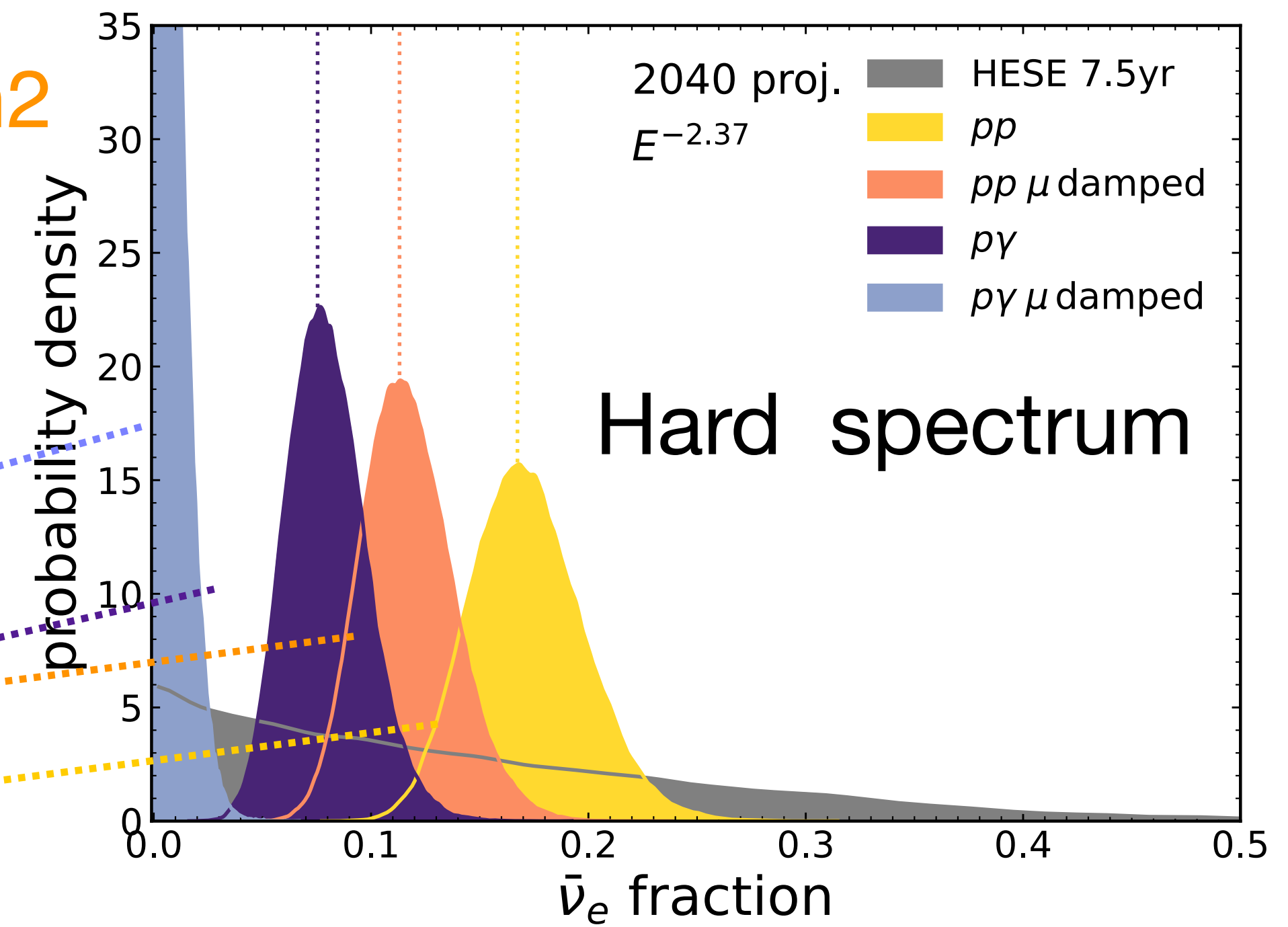
- IceCube/IceCube-Gen2
- + KM3NeT
- + Baikal-GVD
- + P-ONE
- + TRIDENT

# 4-Flavor Analysis

IceCube/IceCube-Gen2  
+ KM3NeT  
+ Baikal-GVD  
+ P-ONE  
+ TRIDENT



●  $\pi$  decay    ■  $\mu$  damped    QL, Song, Vincent [2304.06068]

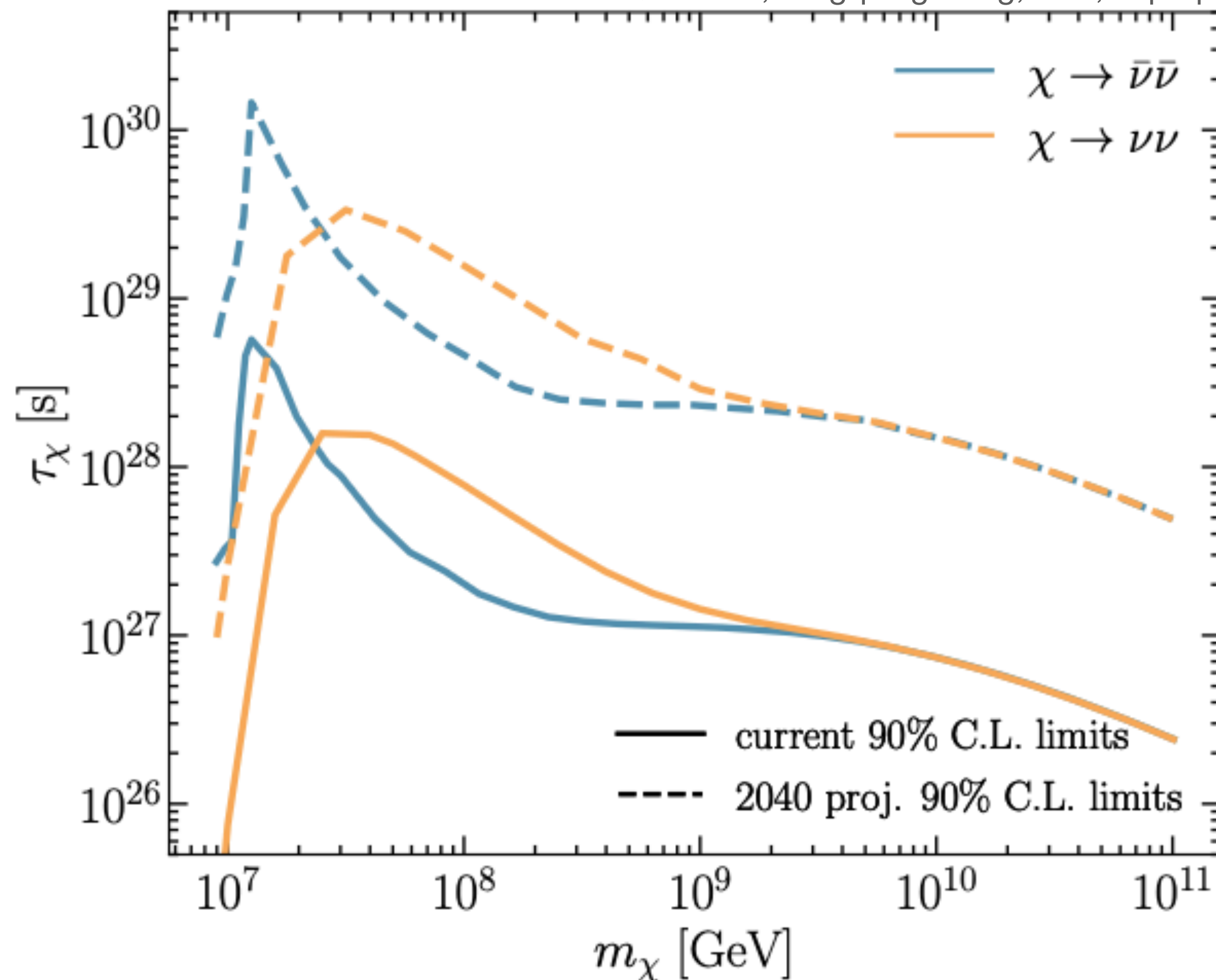


3-flavor can be reconstructed and degenerated scenarios can be distinguished at  $\gtrsim 2\sigma$  w/ the soft spectrum assumption and  $\gtrsim 4\sigma$  w/ the hard spectrum assumption by 2040

# New Physics? Dark matter decay to neutrinos

Qinrui Liu, Ningqiang Song, ACV, in prep

- High mass ( $> \text{PeV}$ ) decay to neutrinos produces an additional flux from **electroweak corrections**
- **The  $\nu$  or  $\bar{\nu}$  flux in the glashow window is different for asymmetric decay to  $\nu\nu$  vs  $\bar{\nu}\bar{\nu}$**



# Summary

- Our understanding of the high-energy neutrino sky will become **1-2 orders of magnitude more precise** over the coming two decades
- Neutrino telescopes cover at least **14 orders of magnitude in energy** & can say all sorts of things about the dark sector & new physics
  - neutrino decay
  - Dark matter
  - More!
- We can go beyond 3-flavours and break the neutrino-antineutrino degeneracy, and thus the  $pp-p\gamma$  degeneracy, by looking at the glashow resonance. This also allows new interesting probes of new physics.