## Update on 1st paper

- Most typos/format changes have been done based on the comments from the PRL. reviewers.
  - Proper way to cite from D-WAVE?
  - Plots for single particle?
  - Rewrite the theory part with clearer setup and definitions.

evidence lower bound (ELBO) to the true log-likelihood:

$$\log p_{\theta}(\mathbf{x}) \ge \mathbb{E}_{q_{\phi}(\mathbf{z}|\mathbf{x})}[\log p_{\theta}(\mathbf{x}|\mathbf{z})] - \text{KL}[q_{\phi}(\mathbf{z}|\mathbf{x})||p_{\theta}(\mathbf{z})]$$
(1)

 $\mathrm{KL}[Q||P]$  is the Kullback-Liebler divergence between two probability distributions, Q and P while  $\mathbb{E}_p$  denotes an expectation value over the distribution p. The variables  $\mathbf{x}$  and  $\mathbf{z}$  represent data (in this case a vector of calorimeter cell energies) and latent variable respectively. The approximating posterior,  $q_{\phi}(\mathbf{z}|\mathbf{x})$  and the generative,  $p_{\theta}(\mathbf{x}|\mathbf{z})$  distributions are often parameterized using neural networks. In the original VAE framework [6, 19],  $q_{\phi}(\mathbf{z}|\mathbf{x})$  and  $p_{\theta}(\mathbf{z})$  are assumed to be factorized Gaussian distributions,  $\mathcal{N}(\boldsymbol{\mu}_{\phi}(\mathbf{x}), \boldsymbol{\Sigma}_{\phi}^2(\mathbf{x}))$  and  $\mathcal{N}(\mathbf{0}, \mathbf{I})$  respectively.

CaloDVAE [7, 8] is a hierarchical discrete VAE which extends the VAE framework by introducing discrete latent variables  $\mathbf{z}_i \in \{0,1\}$  in the latent space. Both the encoder,  $q_{\phi}(\mathbf{z}|\mathbf{x},\mathbf{e})$ , and decoder,  $p_{\theta}(\mathbf{x}|\mathbf{z},\mathbf{e})$ , are conditioned on energy [18, 20] and are modelled by fully connected neural networks. The approximate posterior of the VAE has a hierarchical structure  $q_{\phi}(\mathbf{z}|\mathbf{x},\mathbf{e}) = \prod_i q_{\phi_i}(\mathbf{z}_i|\mathbf{z}_{j< i},\mathbf{x},\mathbf{e})$  with N latent groups and the latent distribution of the VAE is modelled by an RBM where  $\mathbf{z} = [\mathbf{z}_1,...,\mathbf{z}_N]$  are partitioned into 2 equal subsets to make the 2 sides of the RBM [18]. The RBM is modeled by probability distribution  $p_{RBM} = e^{\mathbf{a}_t^T \mathbf{z}_l + \mathbf{a}_r^T \mathbf{z}_r + \mathbf{z}_t^T \mathbf{W} \mathbf{z}_r / Z}$  where Z is the partition function and  $(\mathbf{a}_l, \mathbf{a}_r, \mathbf{W})$  are the RBM parameters which are trained along with the VAE parameters  $(\theta, \phi)$ .



