

# Study of rare pion decays in the PiBeta and PEN experiments: a look forward

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# Topics discussed in the talk

## Goals and motivation of the PiBeta and PEN program

PiBeta: Quark-lepton universality, CKM unitarity, SM tests

PEN: Lepton universality, SM tests

## Experimental method: PiBeta

Apparatus and measurement method

Detector performance and results

## Experimental method: PEN

Modifications to apparatus and method

Current status of PEN

## Lessons for a possible future experiment



# Known and measured pion and muon decays

decay	B.R.	physics interest
$\pi^+ \rightarrow \mu^+ \nu$	0.9998770(4) $(\pi_{\mu 2})$	
$\mu^+ \nu \gamma$	$2.00(25) \times 10^{-4}$ $(\pi_{\mu 2\gamma})$	
$e^+ \nu$	$1.230(4) \times 10^{-4}$ $(\pi_{e2})$	$\Leftarrow$ lepton universality, beyond SM terms ( $T, \dots$ )
$e^+ \nu \gamma$	$7.39(5) \times 10^{-7}$ $(\pi_{e2\gamma})$	$\Leftarrow$ BSM terms ( $T, \dots$ ), form fact's: $F_A^{(\pi)}, F_V^{(\pi)}, \dots$
$\pi^0 e^+ \nu$	$1.036(6) \times 10^{-8}$ $(\pi_{e3})$	$\Leftarrow$ quark-lepton universality ( $V_{ud}$ ), BSM loops
$e^+ \nu e^+ e^-$	$3.2(5) \times 10^{-9}$ $(\pi_{e2ee})$	
$\pi^0 \rightarrow \gamma \gamma$	0.98798(32)	
$e^+ e^- \gamma$	$1.198(32) \times 10^{-2}$ (Dalitz)	$\Leftarrow$ $\chi$ anomaly, low energy chiral parameters
$e^+ e^- e^+ e^-$	$3.14(30) \times 10^{-5}$	
$e^+ e^-$	$6.2(5) \times 10^{-8}$	
$\mu^+ \rightarrow e^+ \nu \bar{\nu}$	$\sim 1.0$	(Michel)
$e^+ \nu \bar{\nu} \gamma$	0.014(4)	(RMD)
$e^+ \nu \bar{\nu} e^+ e^-$	$3.4(4) \times 10^{-5}$	$\Leftarrow$ beyond SM weak interaction terms



# Summary of PiBeta and PEN goals

Goals of the **PiBeta** experiment (data runs 1999-2004):

Decay	$\mathcal{O}(\text{B.R.})$	Goal $\delta R/R$	Attendant SM limits
$\pi_{e3(\gamma)} : \pi^+ \rightarrow \pi^0 e^+ \nu_e (\gamma)$	$R_{e3(\gamma)}^\pi \sim 10^{-8}$	$\sim 5 \times 10^{-3}$	(see below)
$\pi_{e2\gamma} : \pi^+ \rightarrow e^+ \nu_e \gamma$	$R_{e2\gamma}^\pi \sim 10^{-7}$	$\leq 1 \times 10^{-2}$	$F_A^\pi, F_V^\pi, F_T^\pi; \chi^{\text{PT}}$ l.e.c.
RMD: $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma$	$R_{e2\gamma}^\pi \sim 10^{-3}$	$\leq 1 \times 10^{-2}$	Michel param.: $\bar{\eta}$

Goals of the **PEN** experiment (data runs 2008-2010):

Decay	$\mathcal{O}(\text{B.R.})$	Goal $\delta R/R$	Attendant SM limits
$\pi_{e2(\gamma)} : \pi^+ \rightarrow e^+ \nu_e (\gamma)$	$R_{e2(\gamma)}^\pi \sim 10^{-4}$	$\sim 5 \times 10^{-4}$	(see below)
$\pi_{e2\gamma} : \pi^+ \rightarrow e^+ \nu_e \gamma$	$R_{e2\gamma}^\pi \sim 10^{-7}$	$\sim 1 \times 10^{-2}$	improve $F_V^\pi$ & limit on $F_T^\pi$
RMD: $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma$	$R_{e2\gamma}^\pi \sim 10^{-6}$	$\sim 1 \times 10^{-2}$	improve $\bar{\eta}$



## $\pi_{e3}$ decay rate in the SM (a pure vector $0^- \rightarrow 0^-$ decay)

$$\Gamma_{e3(\gamma)}^\pi = \Gamma_0(1 + \delta_\pi) = \frac{G_F^2 |V_{ud}|^2 \Delta^5}{30\pi^3} f(\epsilon, \Delta) \left(1 - \frac{\Delta}{2m_+}\right)^3 (1 + \delta_\pi) \quad \left[ \equiv R_{e3(\gamma)}^\pi / \tau_\pi \right],$$

where

$$\Delta = m_+ - m_0 = 4.5936(5) \text{ MeV} \quad \text{and} \quad \epsilon = \left(\frac{m_e}{\Delta}\right)^2 \simeq \frac{1}{81}$$

while

$$f(\epsilon, \Delta) = \sqrt{1-\epsilon} \left(1 - \frac{9}{2}\epsilon - 4\epsilon^2\right) + \frac{\epsilon^2}{4} \ln \left(\frac{1 - \sqrt{1-\epsilon}}{\sqrt{\epsilon}}\right) - \frac{3}{7} \frac{\Delta^2}{(m_+ + m_0)^2} \simeq 0.941$$

and  $\delta_\pi \sim 0.0335$  is the sum of radiative/loop corrections with  $\sim 0.03\%$  relative uncertainty.

This is the **theoretically cleanest** way to determine CKM  $V_{ud}$ , which leads to several interesting SM tests, but is at the same time **experimentally the hardest!**

[Physics reach of precise measurements of  $R_{e3(\gamma)}^{\pi\text{-exp}}$  and  $R_{e2(\gamma)}^{\pi\text{-exp}}$  has been discussed by Hoferichter, Bryman, and Cirigliano in talks at this meeting.]

Prior to 2004,  $\Gamma_{e3}^\pi$  and  $R_{e3}^\pi$  measured with about 4 % precision.



## $\pi_{e2}$ decay: SM calculations, lepton universality

- Early evidence for  $V - A$  nature of weak interaction.

$$R_{e/\mu}^\pi = \frac{\Gamma(\pi \rightarrow e\bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu\bar{\nu}(\gamma))} = \frac{g_e^2}{g_\mu^2} \frac{m_e^2}{m_\mu^2} \frac{(1 - m_e^2/m_\mu^2)^2}{(1 - m_\mu^2/m_\pi^2)^2} (1 + \delta R_{e/\mu})$$

- Modern SM calculations:  
 $R_{e/\mu}^\pi = \frac{\Gamma(\pi \rightarrow e\bar{\nu}(\gamma))}{\Gamma(\pi \rightarrow \mu\bar{\nu}(\gamma))}^{\text{CALC}} =$   
$$\begin{cases} 1.2352(5) \times 10^{-4} & \text{Marciano and Sirlin, [PRL 71 (1993) 3629]} \\ 1.2354(2) \times 10^{-4} & \text{Finkemeier, [PL B 387 (1996) 391]} \\ 1.2352(1) \times 10^{-4} & \text{Cirigliano and Rosell, [PRL 99 (2007) 231801]} \end{cases}$$



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- $R_{e/\mu}^\pi$  tests **lepton universality**: in SM **e,  $\mu$ ,  $\tau$**  differ by Higgs couplings only; there could also be new **S or PS bosons** with non-universal couplings (New Physics); repercussions also in the neutrino sector, **SUSY, ALPS** ...

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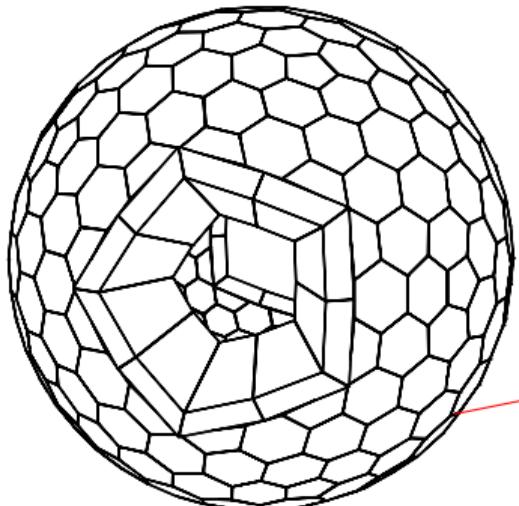
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- Experimental world average is **23 $\times$**  less accurate than SM calculations!  $[1.2327(23) \times 10^{-4}]$

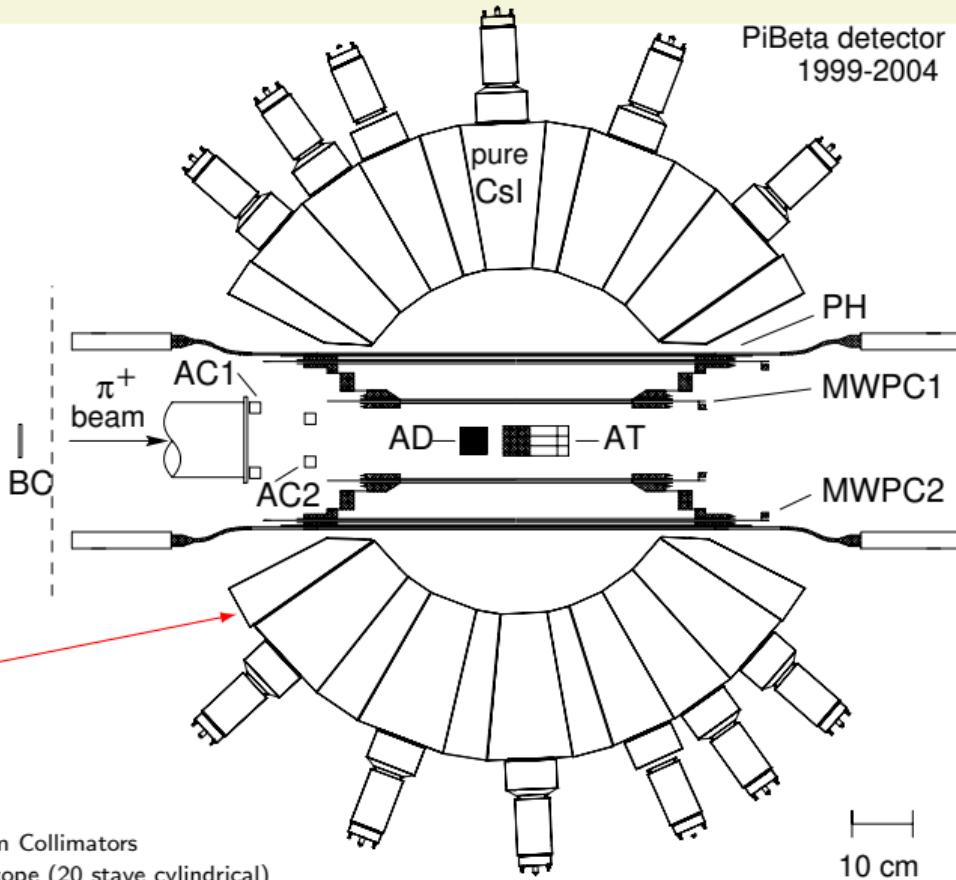


# The PiBeta apparatus

- $\pi^-$ E1 beam at PSI
- stopped  $\pi^+$  beam
- 9-elem. active tgt
- 240-elem.  $12X_0$  spherical pure-CsI calo.
- tightly controlled temp/humidity/gains
- central tracking
- beam tracking
- fast-digitized wf's

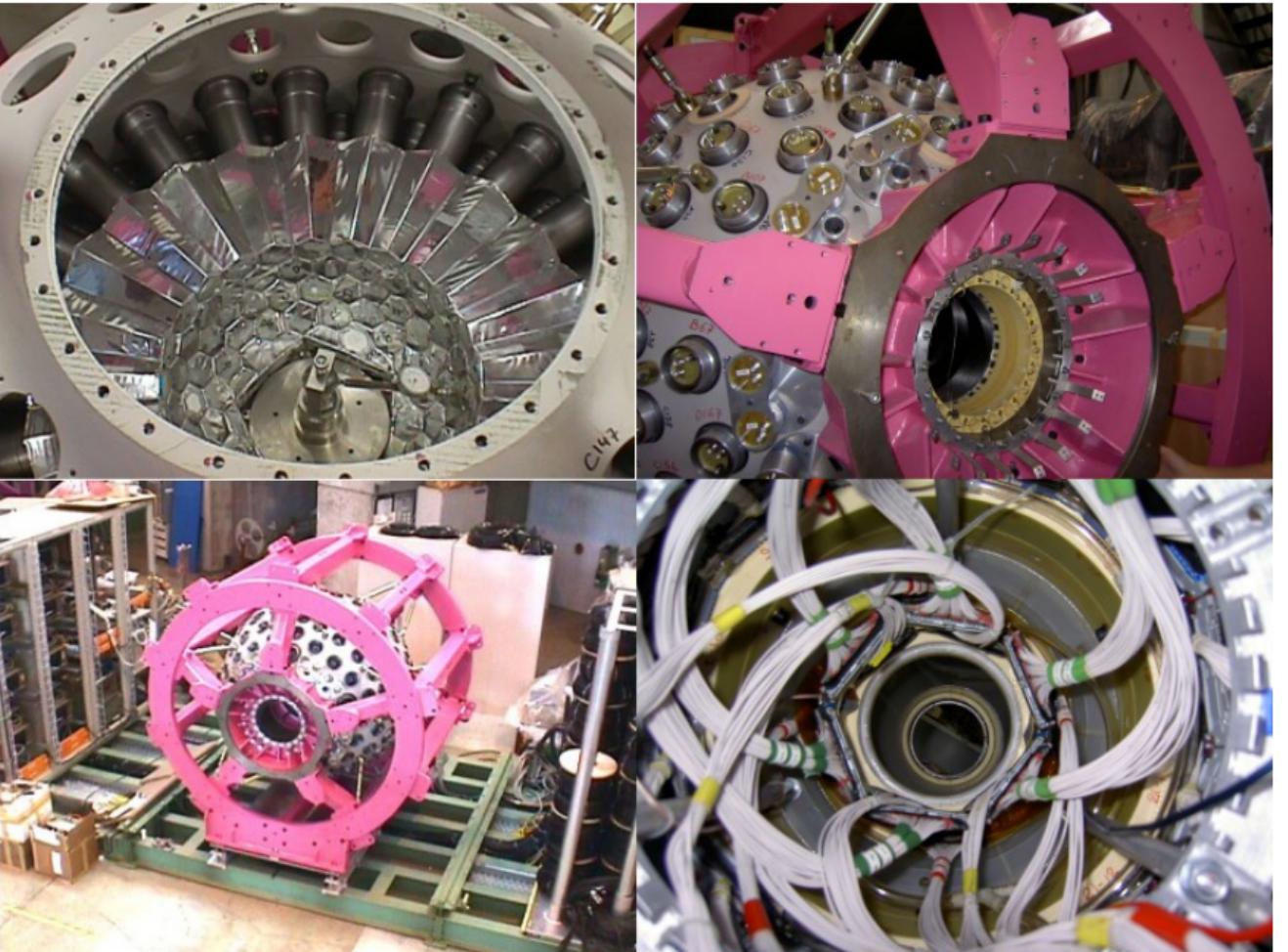


BC: Beam Counter  
AD: Active Degrader  
AT: Active Target



AC1,2: Active beam Collimators  
PH: Plastic Hodoscope (20 stave cylindrical)  
MWPC: Multi-Wire Proportional Chamber (cylindrical)

A few photos of the  
PiBeta apparatus:

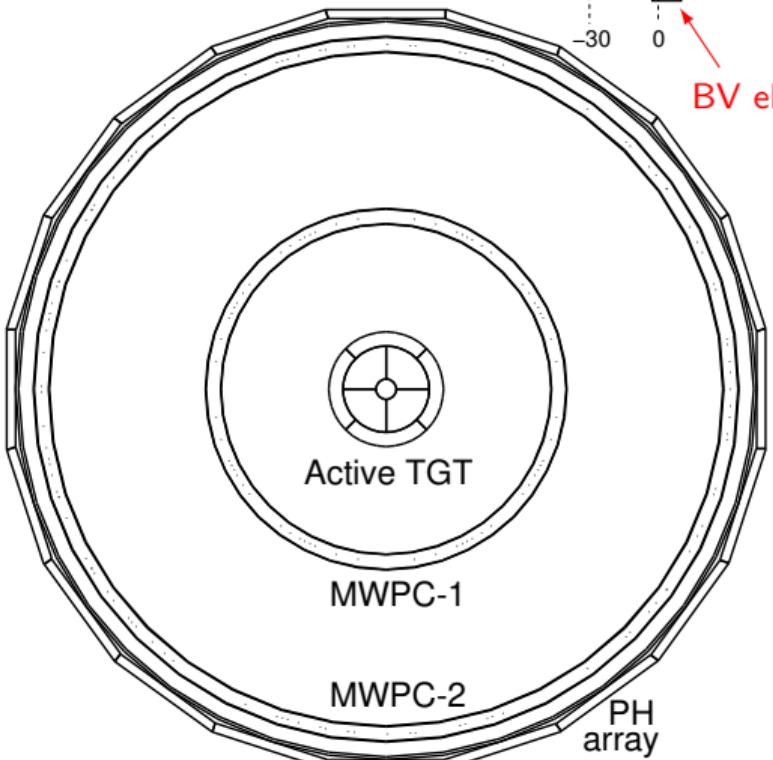


PiBeta/PEN lessons: Apparatus and method

5 Nov '20/DND 2020

## PiBeta central detector region

TGT stopping rate:  $\geq 10^6 \pi/\text{s}$ ;  
9-pc. AT: 5 inner (fiducial stop)  
4 guard/tracking ring;



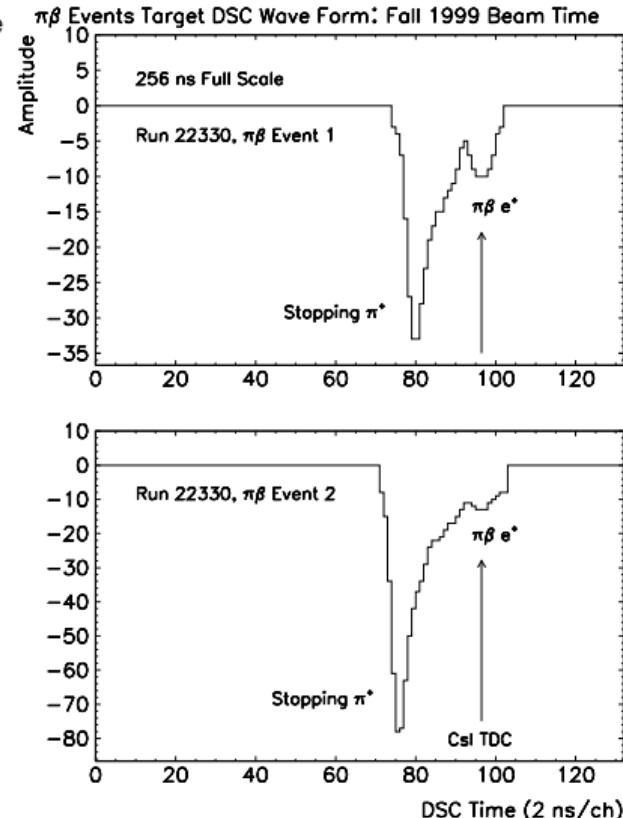
BV eliminated in PEN!

Beam  $p \simeq 113 \text{ MeV}/c$   
(to achieve  $\pi_{\text{stop}}$  rate)

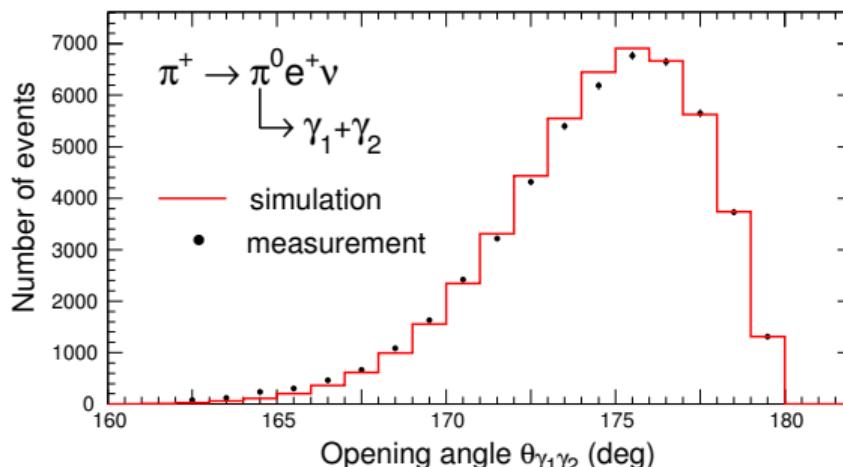
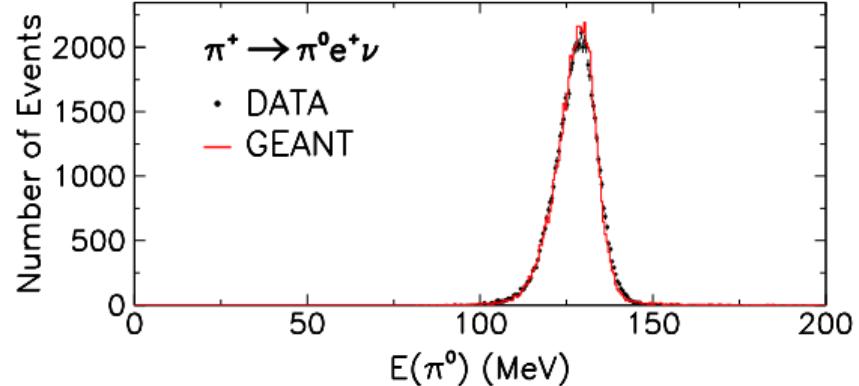
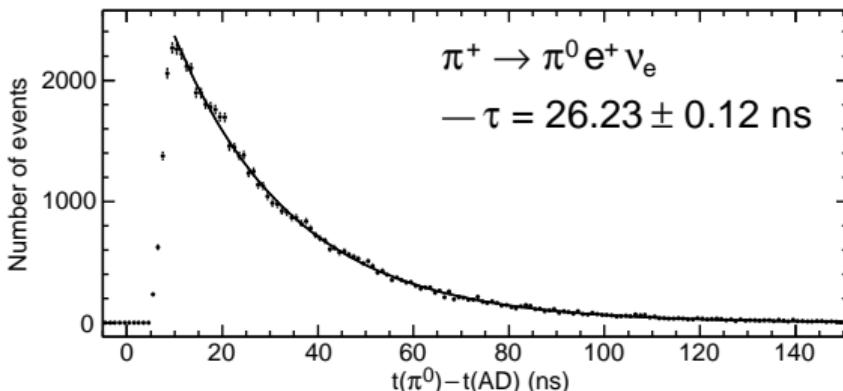
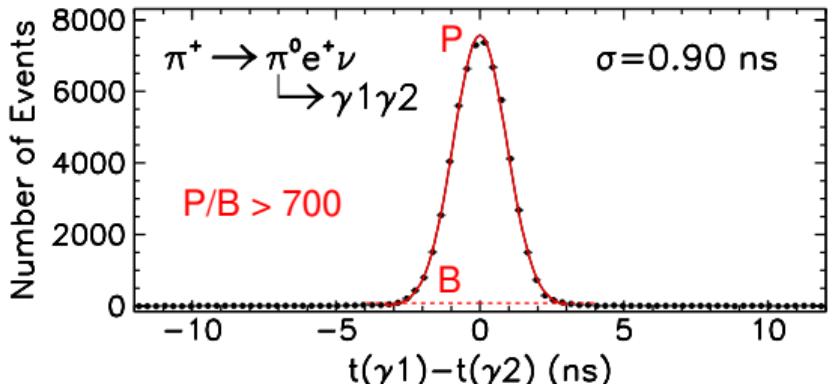
9-piece AT provides  
rudimentary beam  
stop tracking

Note: AT was replaced  
for each annual run due  
to radiation damage.

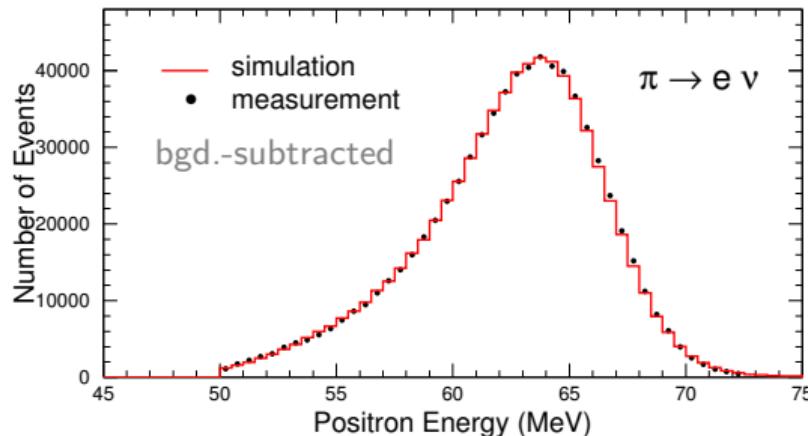
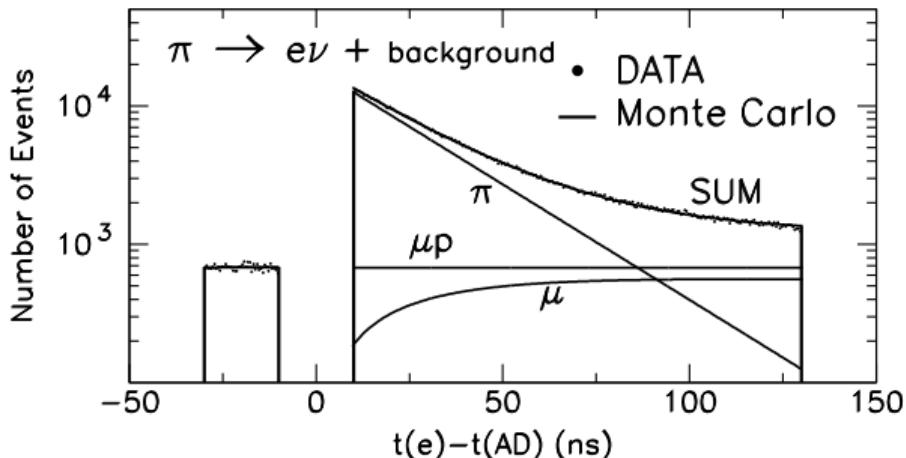
Digitized AT signal waveforms:



# Key PiBeta spectra: $\pi_{e3}$ decay (2004)

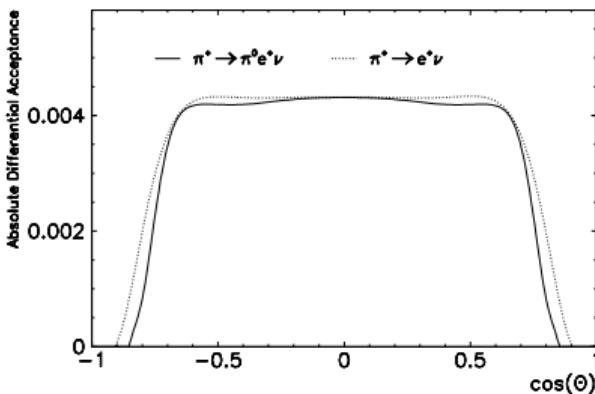


# PiBeta normalization spectra: $\pi_{e2}$ decay (2004)



Notes:

- $\pi_{e3}$  signals are clean, w/low bgd. levels (previous slide);
- large background in  $\pi_{e2}$  from  $\pi \rightarrow \mu \rightarrow e$  decay chain,
- ... also from pile-up  $\mu$ 's in target;
- $\sim 15$  ns vetoed around  $t = 0$  to suppress prompt hadr. bkgd.;
- excellent agreement with Geant3 MC simulations;
- $\pi_{e2}$ : large subtraction of  $\pi \rightarrow \mu \rightarrow e$  events below  $\sim 55$  MeV;
- well matched acceptances for  $\pi_{e3}$ ,  $\pi_{e2}$  decays (shown);
- even closer for  $\pi_{e2}$  and  $\pi \rightarrow \mu \rightarrow e$  channels (not shown).



PiBeta result for  $\pi^+ \rightarrow \pi^0 e^+ \nu$  ( $\pi_\beta$ ) decay [PRL 93, 181803 (2004)]

Pion beta decay yield normalized to measured  $\pi \rightarrow e\nu$  events:

$$B_{\pi\beta}^{\text{exp-t}} = [1.040 \pm 0.004 \text{ (stat)} \pm 0.004 \text{ (syst)}] \times 10^{-8},$$

$$B_{\pi\beta}^{\text{exp-e}} = [1.036 \pm 0.004 \text{ (stat)} \pm 0.004 \text{ (syst)} \pm 0.003 \text{ ( $\pi_{e2}$ )}] \times 10^{-8},$$

McFarlane et al. [PRD 1985]:  $B = (1.026 \pm 0.039) \times 10^{-8}$

SM Prediction (PDG):

$$B = 1.038 - 1.041 \times 10^{-8} \quad (90\% \text{ C.L.})$$
$$(1.005 - 1.007 \times 10^{-8} \quad \text{excl. rad. corr.})$$

⇒ Most sensitive test of CVC/radiative corr. in a meson to date!

PDG 2020:  $V_{ud} = 0.97370(14)$

PiBeta:  $V_{ud} = 0.9748(25)$  or  $V_{ud} = 0.9728(30)$ .



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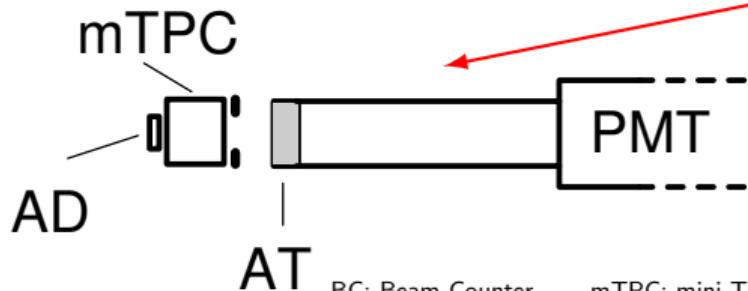
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# The PEN apparatus

New detectors/systems and modifications:

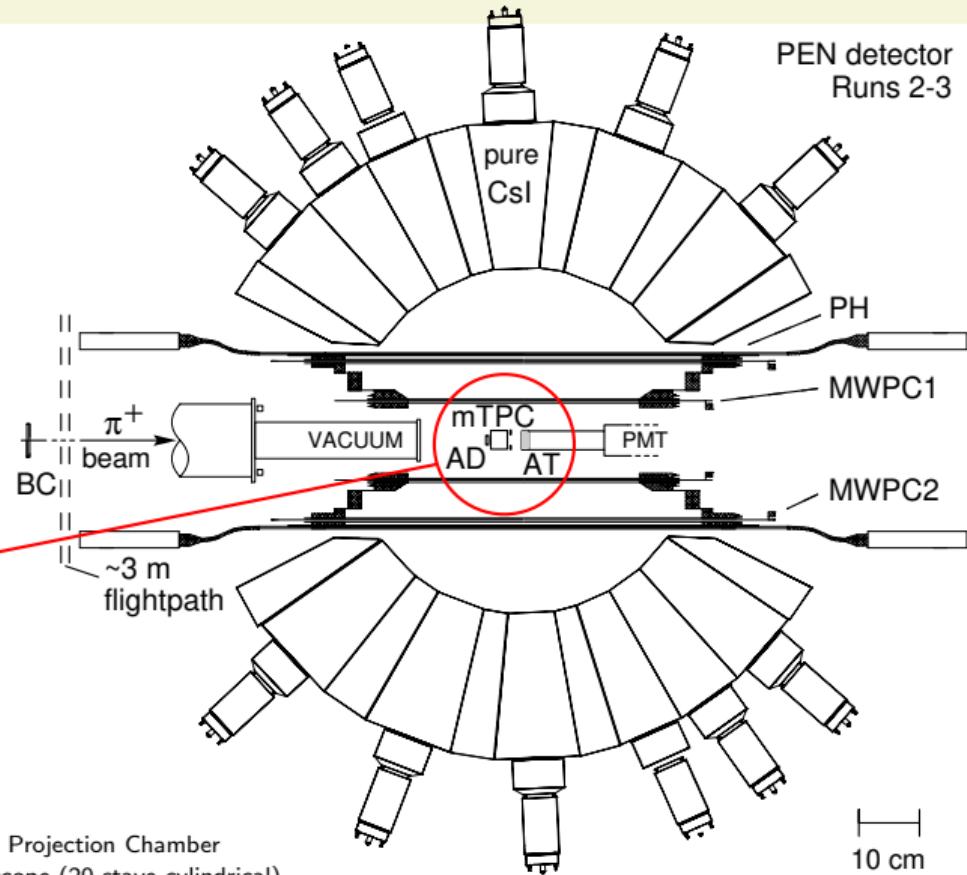
- beam tracking: low mass mini TPC!
- new single-element active target,
- new Aqiris waveform digitizer,
- new single element active target,
- wider  $\pi$ gate: –50 to 220 ns, no BV,
- replaced PH staves (faster, thicker),
- refurbished aged CsI calo PMT's,
- lower beam intensity  $< 10^5$ /s,
- lower beam mom.: 71–75 MeV/c;



BC: Beam Counter  
AD: Active Degrader  
AT: Active Target

mTPC: mini-Time Projection Chamber  
PH: Plastic Hodoscope (20 stave cylindrical)  
MWPC: Multi-Wire Proportional Chamber (cylindrical)

PiBeta/PEN lessons: Exp. method: PEN



# PEN measurement principles for $R_{e/\mu}^\pi$ ; key challenges

Basic principle: record pion decays at rest in a beam stopping target<sup>1</sup> and count each:

- (a)  $\pi_{e2(\gamma)}: \pi^+ \rightarrow e^+ \nu_e(\gamma)$ , and (b)  $\pi_{\mu 2(\gamma)}: \pi^+ \rightarrow \mu^+ \nu_\mu(\gamma)$  decay event

during an observation time window, and evaluate the yield ratio (a)/(b), applying appropriate corrections. Since (a) and (b) cannot be identified sufficiently reliably in the stopping target alone, an e-m calorimeter and tracking detectors are used, identifying (b) through the subsequent decay  $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu(\gamma)$ .

**Key challenges** in achieving sub- $10^{-3}$ , or sub- $10^{-4}$  precision are of **systematic** nature:

- ▶ accurately **identify** processes (weak decay, hadronic interaction, etc.) for each event,
- ▶ accurately **count** and **sort** each type of decay event (without missing/mislabeling any).

In practice this means that beam and decay particles must be **tracked**, and their interactions with matter **detected** and **recorded**, until the final stop of the detectable decay products in the calorimeter.

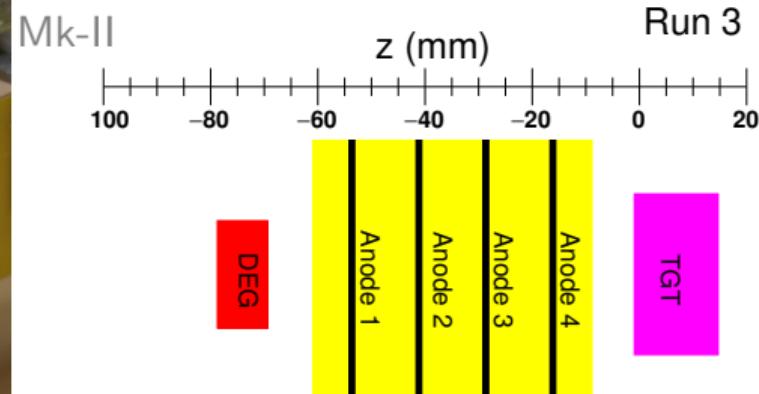
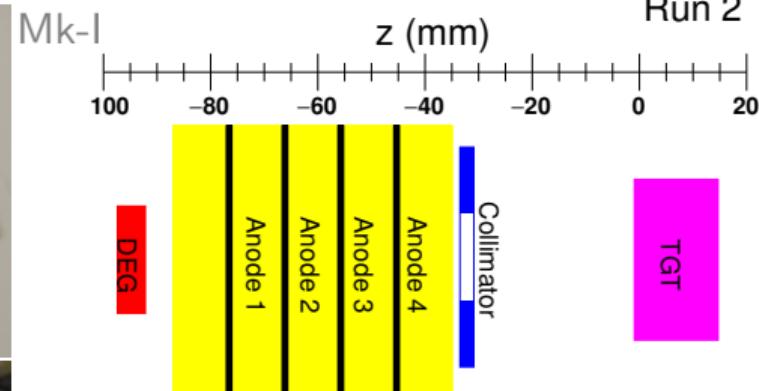
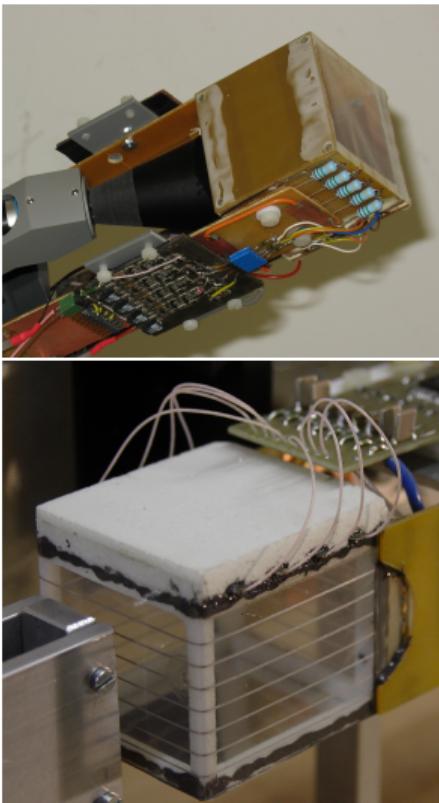
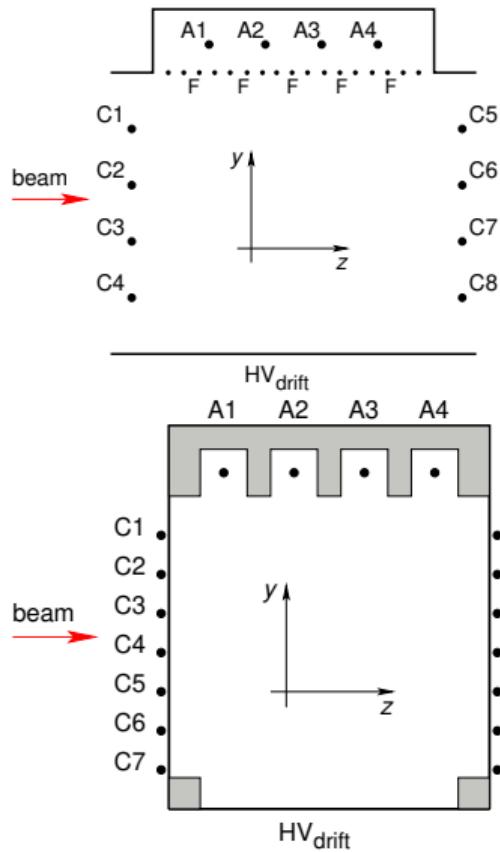
Key **design requirements** include **minimizing mass** in the particle path to target/calorimeter, while **maximizing detection efficiency** and **resolution**:  $E$ ,  $t$  and spatial.

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<sup>1</sup>Here we do not discuss decays in flight which present a wholly different set of challenges.



# PEN beam tracking: the mini TPC's (Runs 2 and 3; JINR Dubna designed and built)

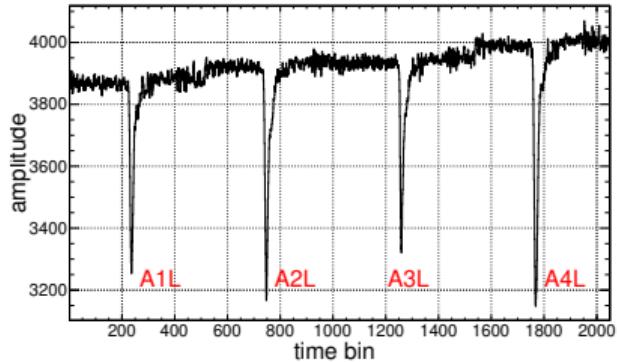


# PEN mTPC performance

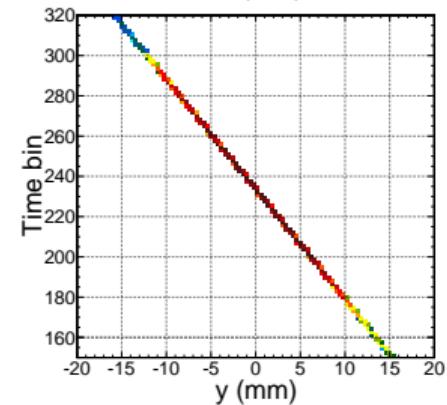
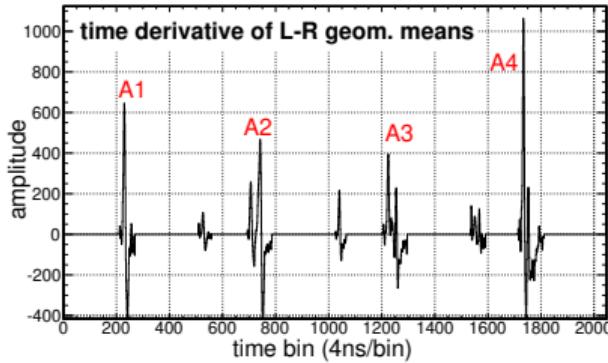
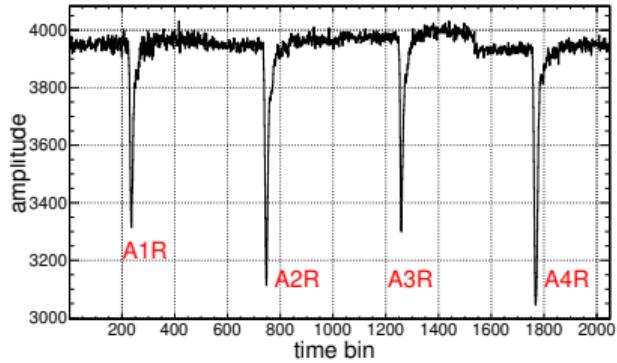
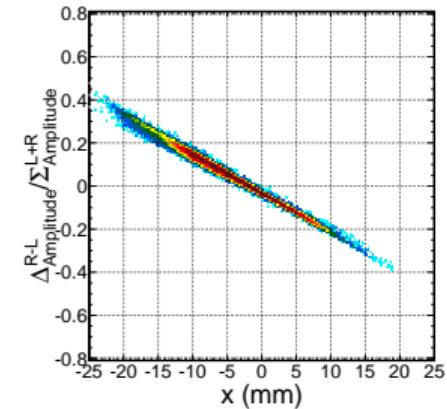
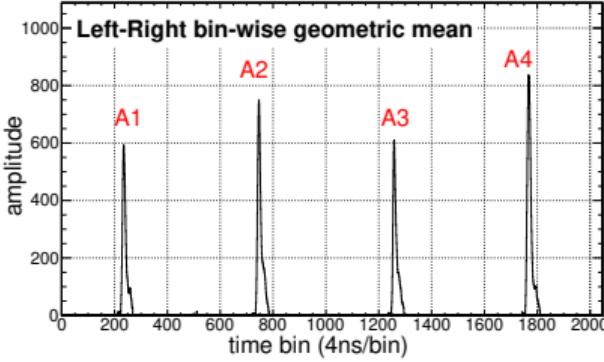
(Mk-I and II performed similarly)

Beam tracking:  $x$ : (resistive) anode L/R amplitude asymmetry;  $y$ : anode mean time vs. AD.

multiplexed anode waveforms:

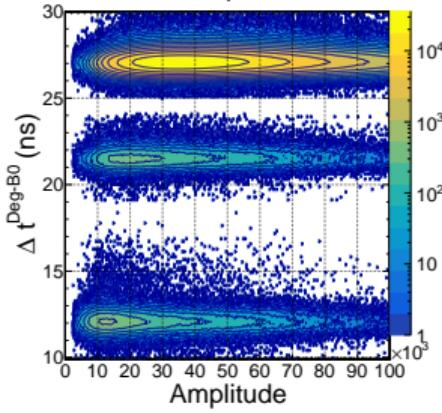
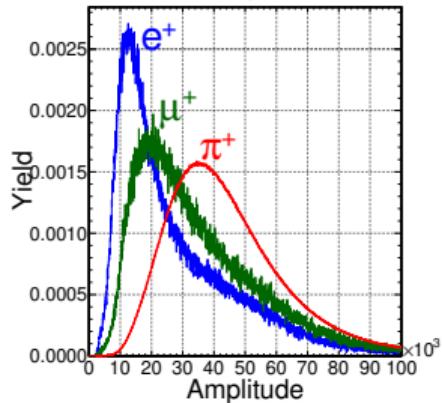


amplitude & timing data:

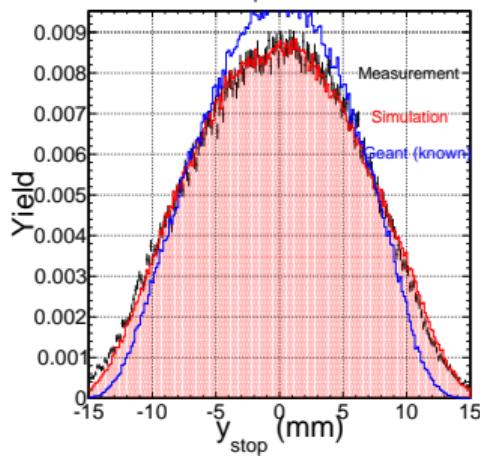
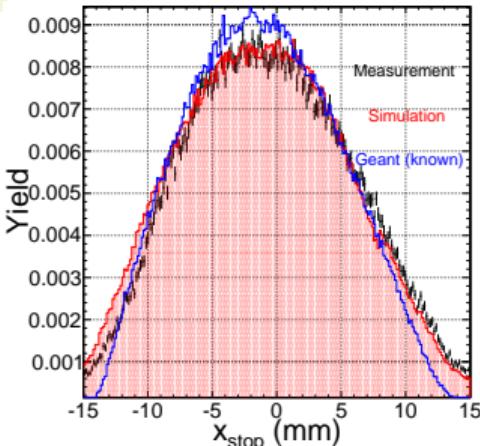


## More on mTPC performance

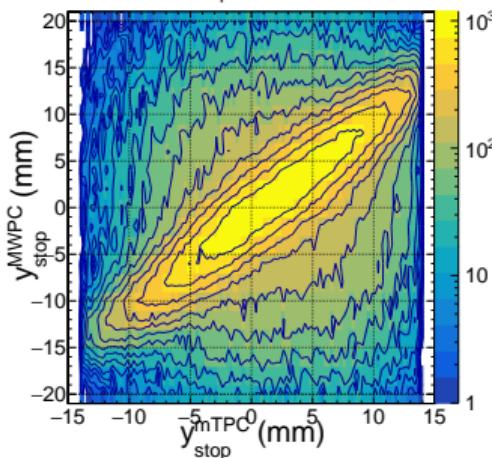
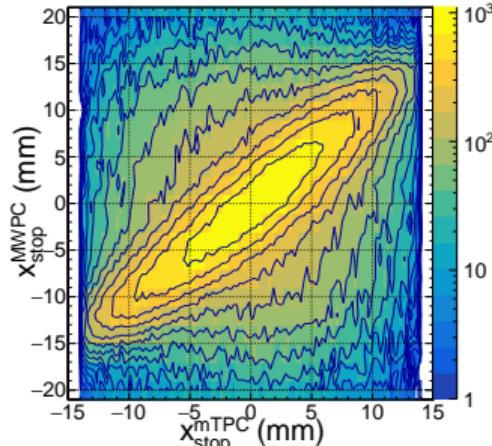
mTPC beam particle ID:



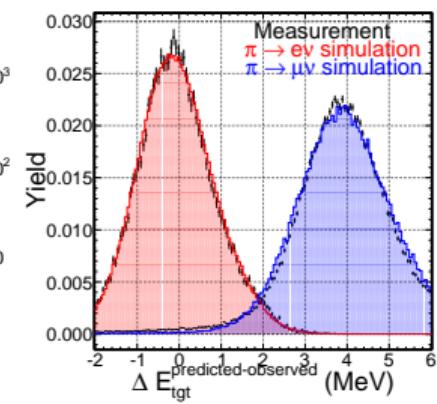
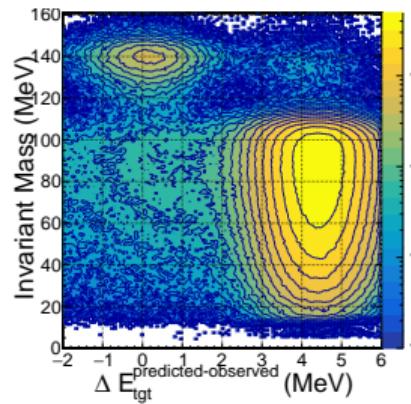
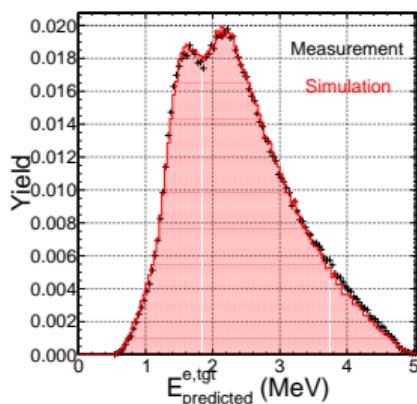
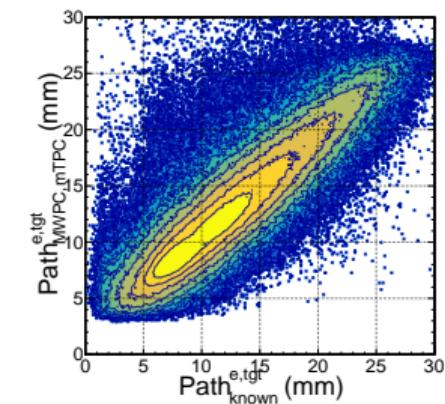
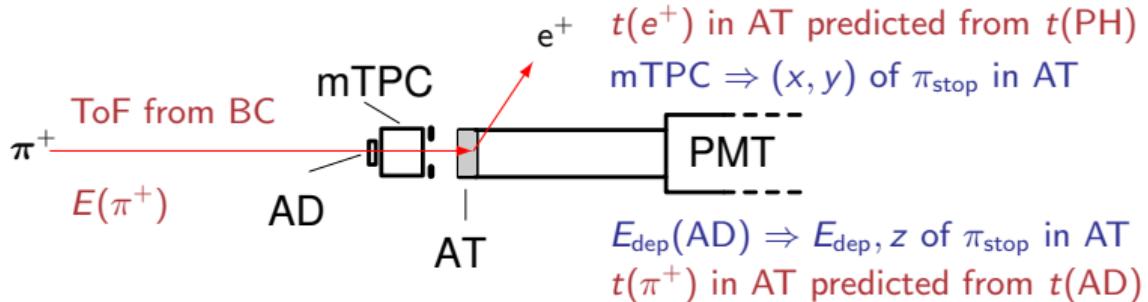
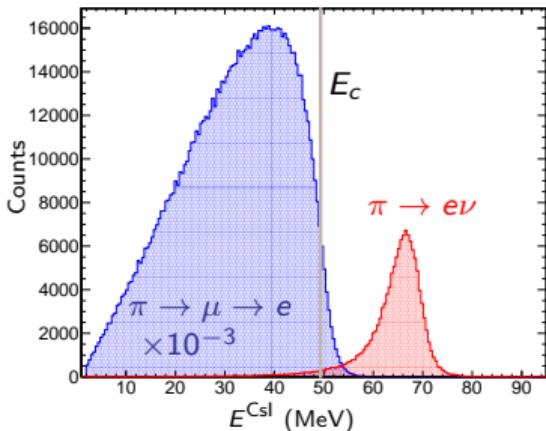
mTPC stopping distr.:



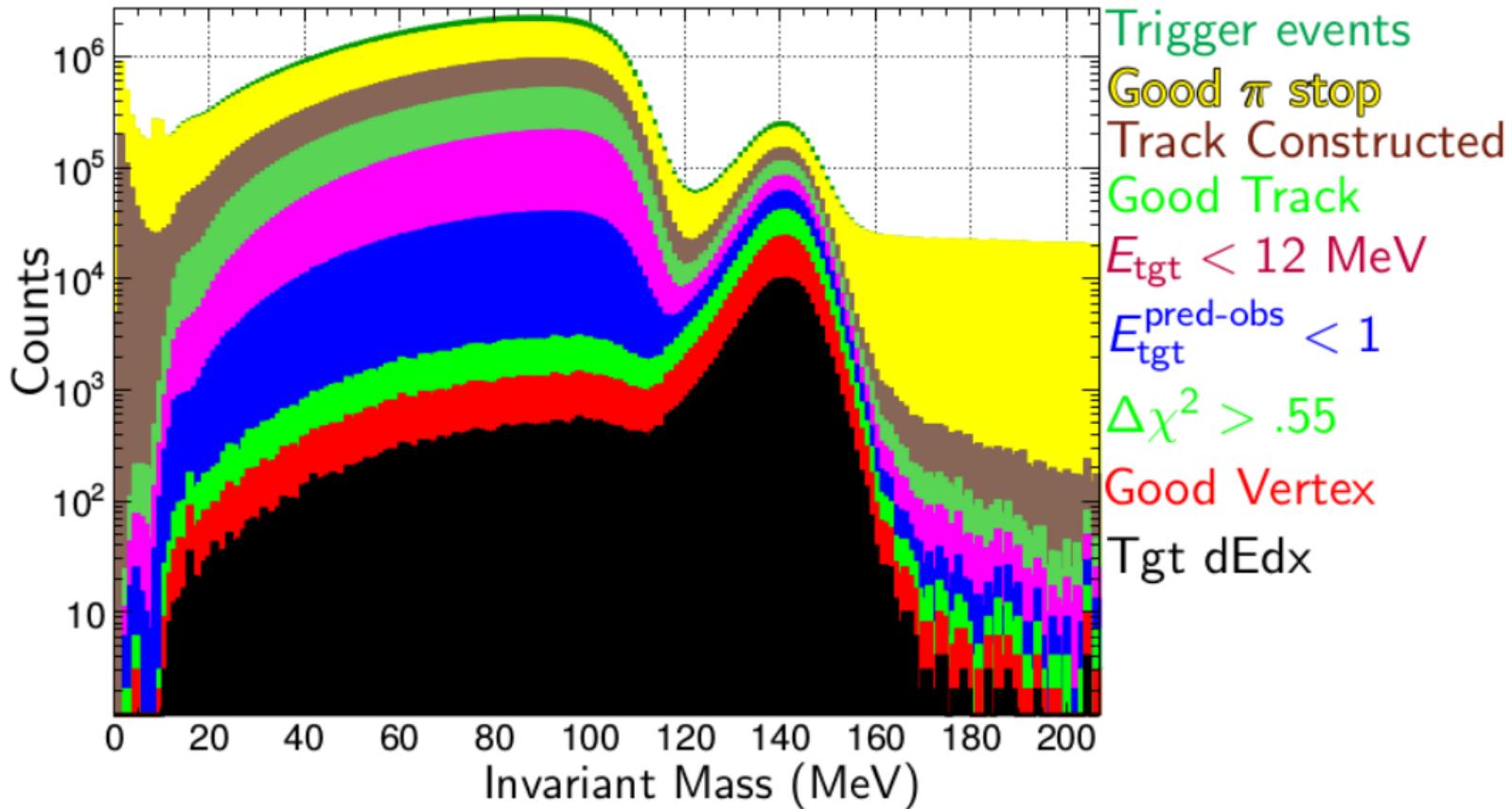
$(x, y)_{\text{stop}}$ : mTPC vs. MWPC



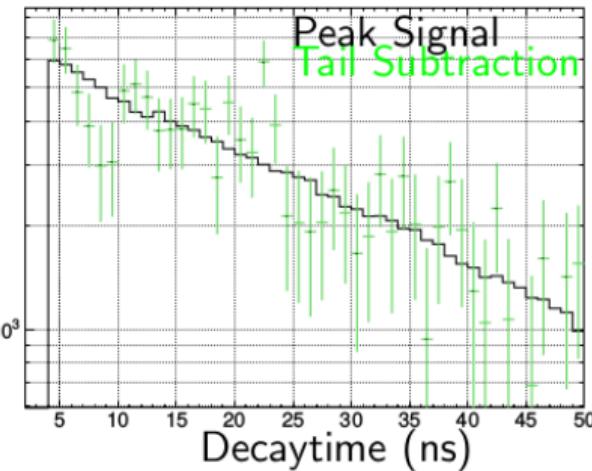
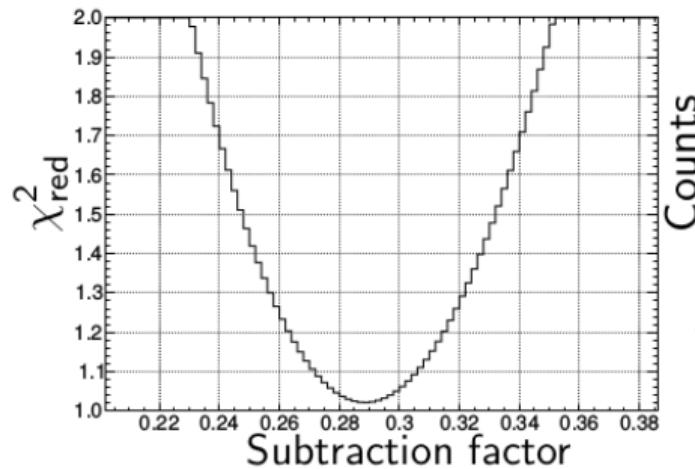
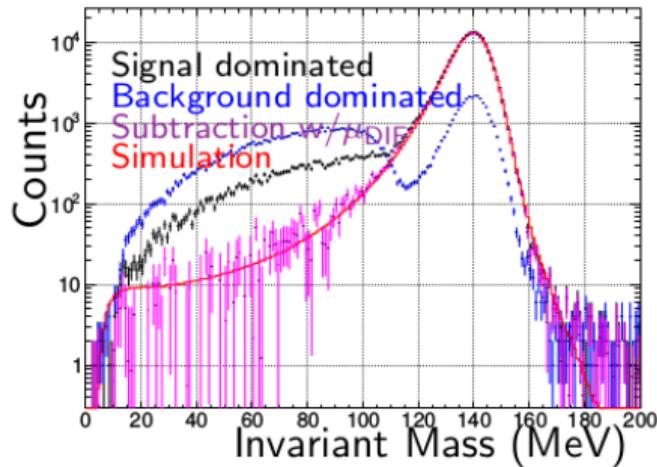
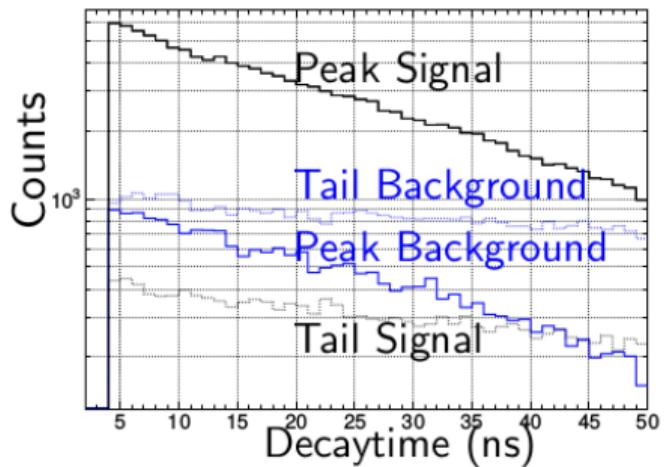
# Discriminating $\pi_{e2}$ and $\pi_{\mu 2}$ in TGT



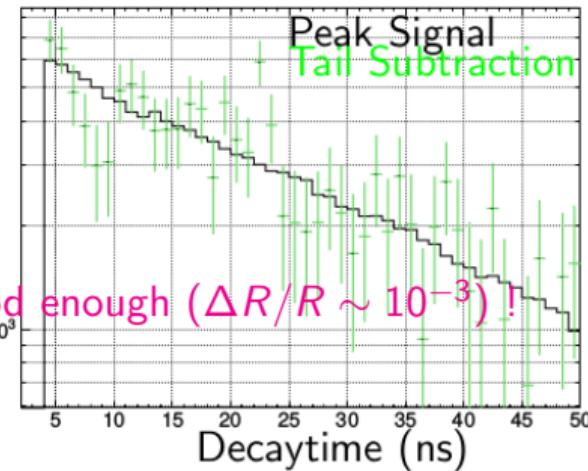
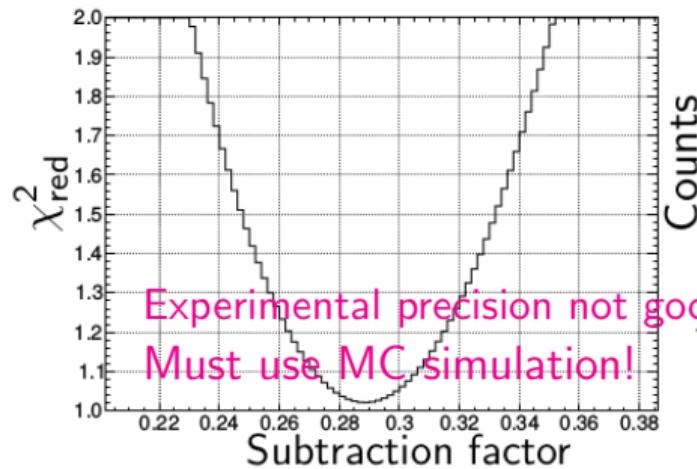
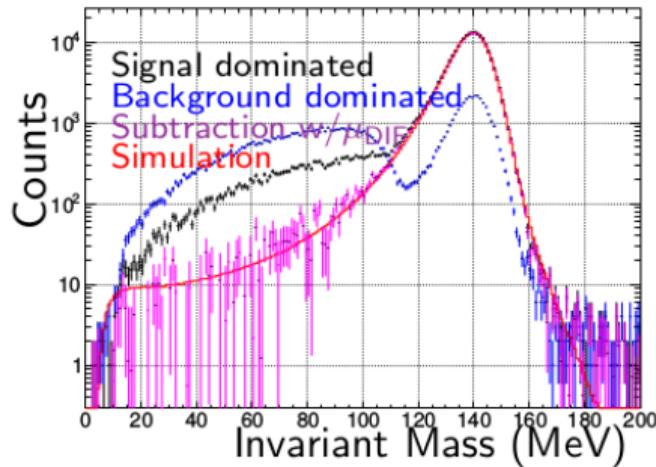
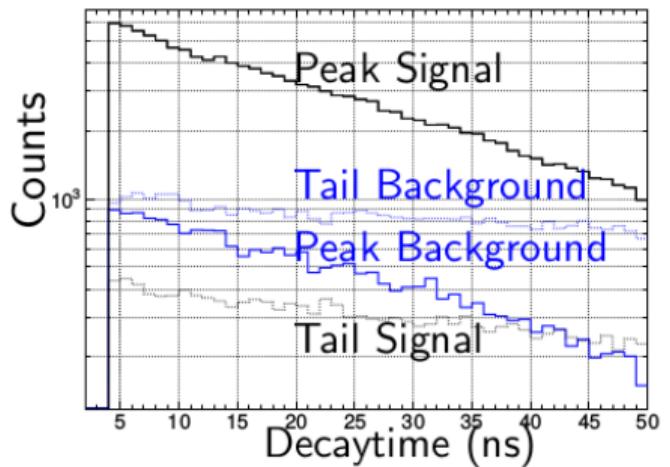
# Tail trigger



Main trigger:  
measured 'tail'  
after backgd.  
subtraction  $\Rightarrow$

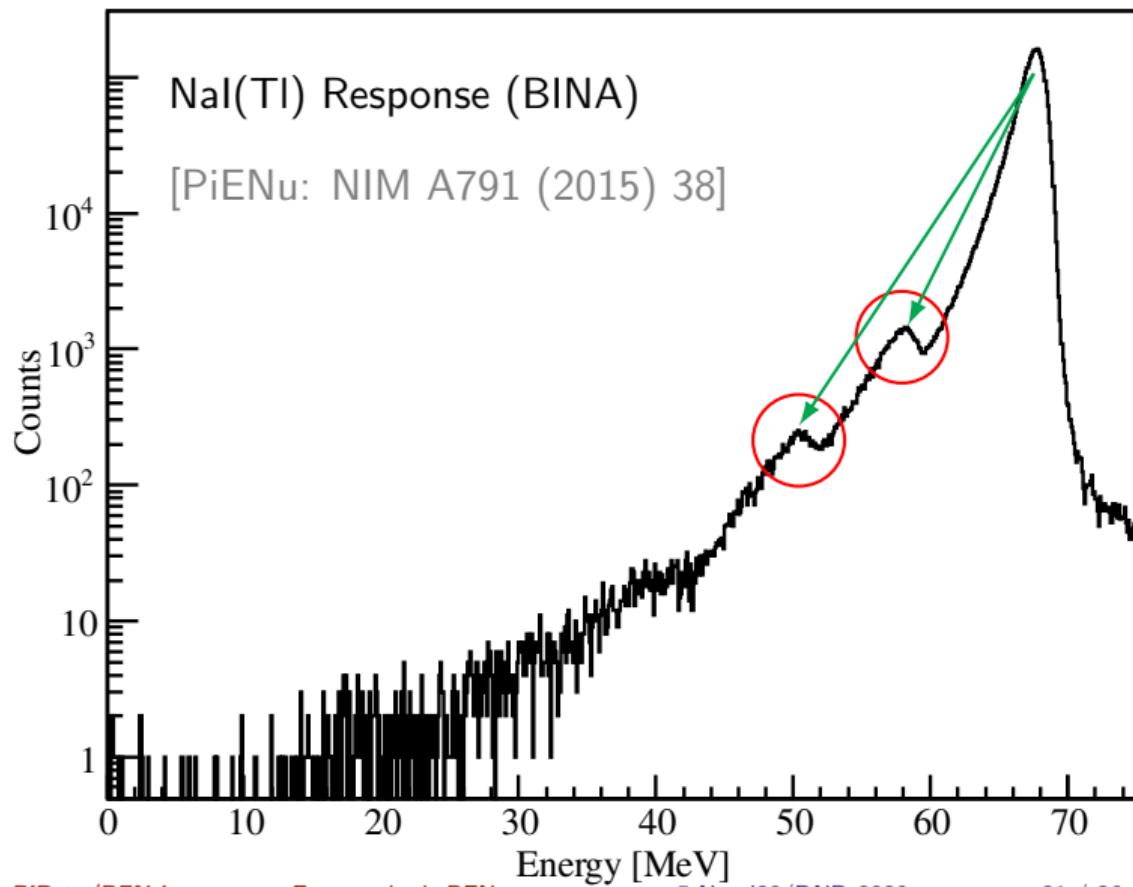


Main trigger:  
measured 'tail'  
after backgd.  
subtraction  $\Rightarrow$



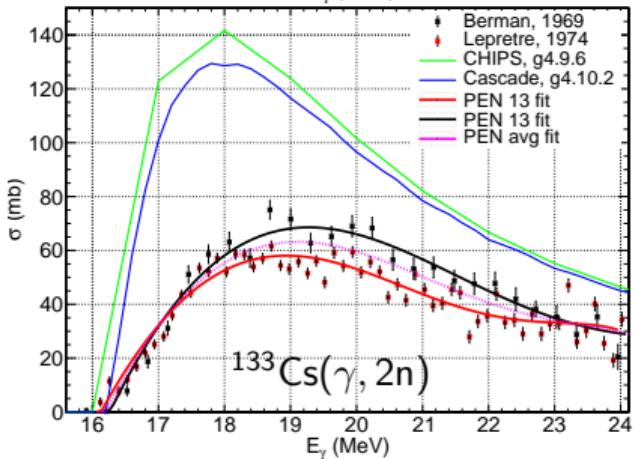
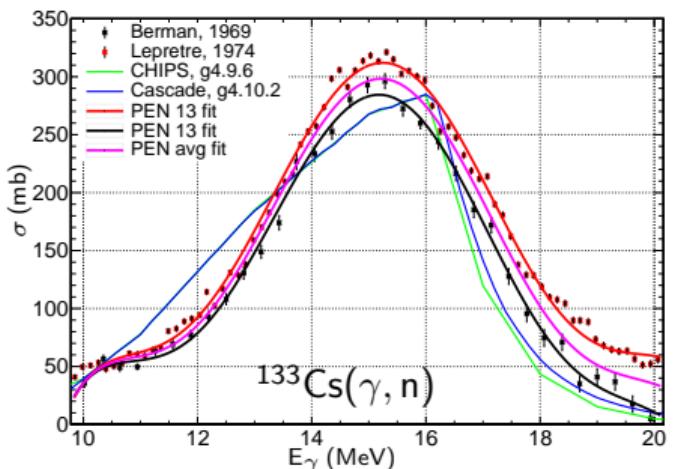
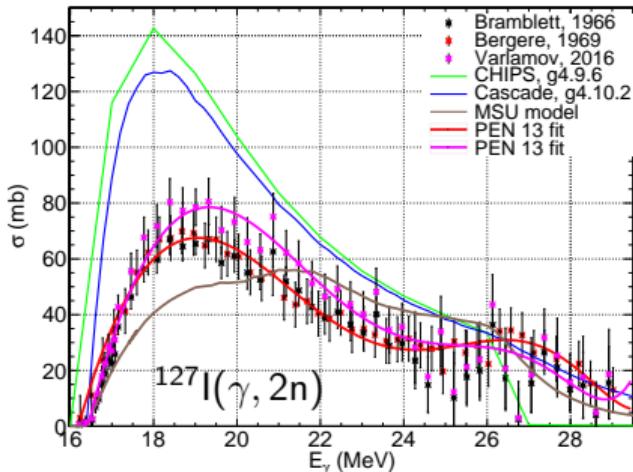
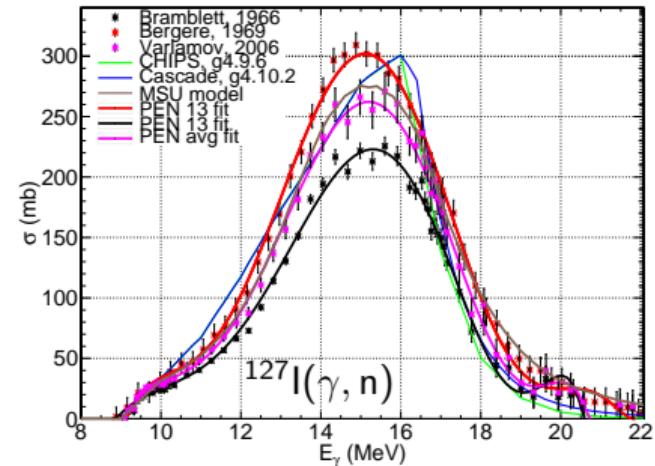
# Tail fraction: photoneutron reactions

$(\gamma, n)$  reactions on calorimeter nuclei, Cs and I, shift counts from the main peak to the “tail” region if the neutron is undetected.



## Photoneutron cross sections, $\sigma(\gamma, xn)$

- ▶ Many inconsistencies among the data sets;
- ▶ Geant4 descriptions inadequate, often miss data by a wide margin.
- ▶ PEN was forced to implement its own parametrization in Geant4 (C. Glaser).
- ▶ This procedure works at the PEN goal precision, but would be inadequate at higher precision.



# Current status of PEN analysis

$$R_{e/\mu}^{\pi} = \frac{N_{\pi \rightarrow e\nu}^{\text{peak}}}{N_{\pi \rightarrow \mu\nu}} (1 + \epsilon_{\text{tail}}) \frac{A_{\pi-\mu-e}}{A_{\pi-\mu-e}} \frac{\epsilon(E_{\mu \rightarrow e\nu\bar{\nu}})_{\text{MWPC}}}{\epsilon(E_{\pi \rightarrow e\nu})_{\text{MWPC}}} \frac{f_{\pi-\mu-e}(T_e)}{f_{\pi-\mu-e}(T_e)}$$

	$r_A$	$r_\epsilon$	$r_f$
Systematics	Value	$\Delta R_{e/\mu}^{\pi}/R_{e/\mu}^{\pi}$	
$\epsilon_{\text{tail}}$	0.032	$3.5 \times 10^{-4}$	
$r_f$	0.04292034	$5 \times 10^{-6}$	
$* r_A r_\epsilon$	$\simeq 0.98$	$\sim 3 \times 10^{-4}$	
Statistical:			
$\Delta N_{\pi \rightarrow e\nu}/N_{\pi \rightarrow e\nu}$		$5.15 \times 10^{-4}$	(Runs 2 <sup>†</sup> &3)
Goal		$5 \times 10^{-4}$	

\* Blinded

† incomplete

Work is currently ongoing on the systematic analysis of the remaining steps and checks.



## Lessons for a next generation experiment

- ▶ One can never know too much about an event. **Redundancy** in the measured observables is essential.
- ▶ **Precision tracking** of beam and decay product particles is critically important.
- ▶ There is no substitute for **resolution ( $E$ ,  $t$ , spatial)**, especially in the calorimeter. Calorimeter thickness, though expensive, is essential.
- ▶ Calorimeter must be **separable** so that its response can be studied directly with beam in a controlled manner.
- ▶ **Calorimeter segmentation** is critical. The PiBeta calorimeter was designed to provide sufficient angular resolution for photon-induced showers, and delivered. Calorimeter segmentation enables use of high beam stopping rates with ease.
- ▶ **Low mass** everywhere in the path of particles (beam and decay products) is essential.
- ▶ Highly realistic **simulation** of the apparatus and processes is a given.
- ▶ Handling the **high target rate** for an ultimate  $R_{e3(\gamma)}^\pi$  measurement is a **challenge**.



## A caveat: radiative decays

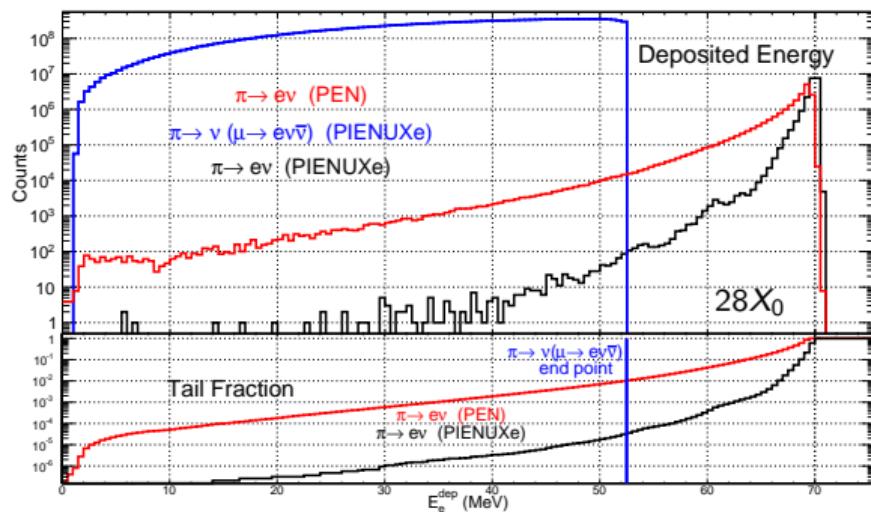
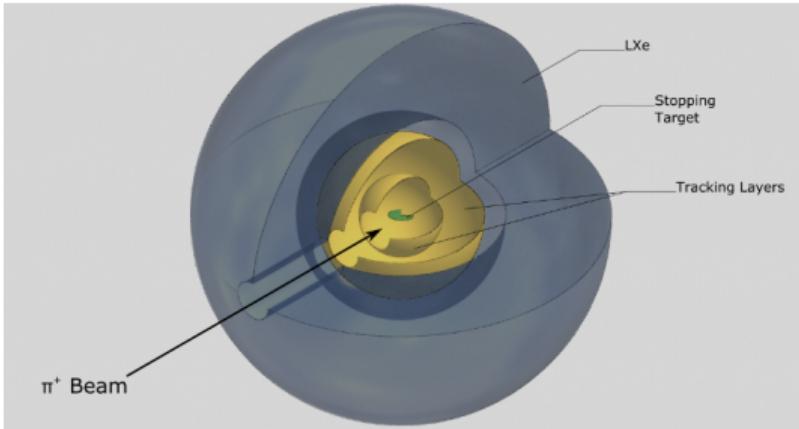
I have not discussed the study of radiative decays:

1.  $\pi^+ \rightarrow e^+ \nu_e \gamma$ , and
2.  $\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu \gamma$ .

These are rich in physics and interesting to study, and accessible with the apparatus discussed here.

Arguably our most impactful result to date is the high precision measurement of  $R_{e2\gamma}^\pi$  and limit on  $F_T$  that has provided the best constraint on  $\epsilon_T$ , the weak **tensor** coupling.





## Concept for an improved RarePi experiment

Goals:

1.  $(\Delta R/R)_{e/\mu}^\pi < 10^{-4}$  (to match theory),
2.  $(\Delta R/R)_{e3}^\pi \sim 2 - 3 \times 10^{-3}$  (per W. Marciano).

### A possible setup:

- ▶ stopped  $\pi^+$  in active target with full tracking,
- ▶ main detector: liquid Xe,
- ▶  $\langle r_{\text{stop}}^\pi \rangle \sim 1.5 - 2 \times 10^6 \text{ s}^{-1}$ ,
- ▶ with  $T_{\text{run}}^{\text{live}} \sim 3 \times 10^7 \text{ s}$  ( $> 2$  calendar years):
- ▶  $N_{e2(\gamma)}^\pi > 5 \times 10^9$ :  $(\Delta R_{e/\mu}^\pi / R)_{\text{stat}} < 2 \times 10^{-5}$ ;
- ▶  $N_{e3(\gamma)}^\pi \geq 4 \times 10^5$ :  $(\Delta R_{e3}^\pi / R)_{\text{stat}} < 2 \times 10^{-3}$ .

Matching the theoretical precision in  $\pi_{e3}$  decay would require substantially higher beam stop rates and further attention to the target and central tracking detectors.



## Current and former PIBETA and PEN collaborators

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<http://pen.phys.virginia.edu>